

University Of Alberta



0 0002 83866 47

# Investigating School Mathematics

**Extending  
the Ideas**

QA

36.5

E34

1973

BK.4

ENR•WKBK

CURR

Accompanying  
AV material  
at  
QA 36.5  
E3415 1969  
CURR AV



# Investigating School Mathematics

ROBERT E. EICHOLZ

PHARES G. O'DAFFER

CHARLES R. FLEENOR

 ADDISON-WESLEY PUBLISHING COMPANY  
Menlo Park, California • Reading, Massachusetts

EX LIBRIS  
UNIVERSITATIS  
ALBERTAENSIS



For Table of Contents,  
see the inside back cover.

## This Book Is the Property of:

State \_\_\_\_\_ Book No. \_\_\_\_\_  
Province \_\_\_\_\_  
County \_\_\_\_\_  
Parish \_\_\_\_\_  
School District \_\_\_\_\_  
Other \_\_\_\_\_

Enter information  
in spaces to the  
left as instructed.

Issued to	Year Used	Condition	
		Issued	Returned

**PUPILS to whom this textbook is issued must not write on any page or mark any part of it in any way; consumable textbooks excepted.**

- Teachers should see that the pupil's name is clearly written in ink in the spaces above in every book issued.
- The following terms should be used in recording the condition of the book: New; Good; Fair; Poor; Bad.

Copyright © 1974 by Addison-Wesley Publishing Company, Inc.  
Philippines Copyright 1974  
All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, without the prior permission of the publisher. Printed in the United States of America. Published simultaneously in Canada.













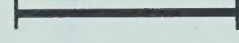

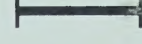

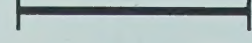

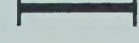
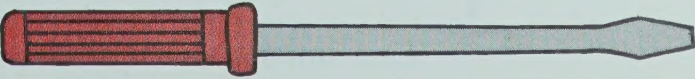
ISBN 0-201-09547-5

ABCDEFGHIJKL—WC—787654

LIBRARY  
UNIVERSITY OF ALBERTA



Complete the table.

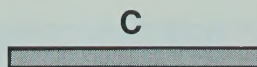
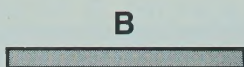
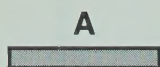
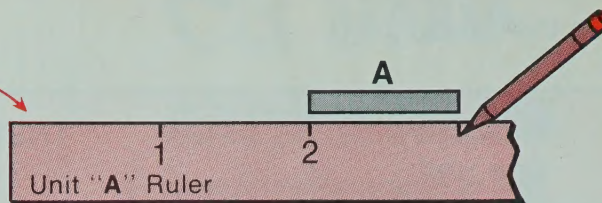
	IF this is one unit	THEN the length of this object is	
1.			units
2.			units
3.			units
4.			units
5.			units
6.			units
7.			units
8.			units
9.			units
10.			units



# ● Making a Ruler

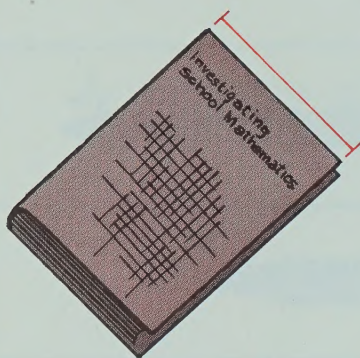
Make a ruler.

Use one of the units—A, B, or C, shown below.



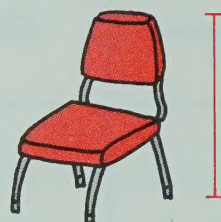
Use your ruler to measure some of the objects suggested in the pictures.

1.



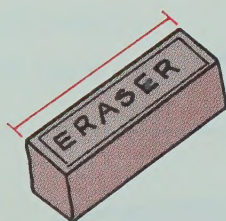
\_\_\_\_\_ units

2.



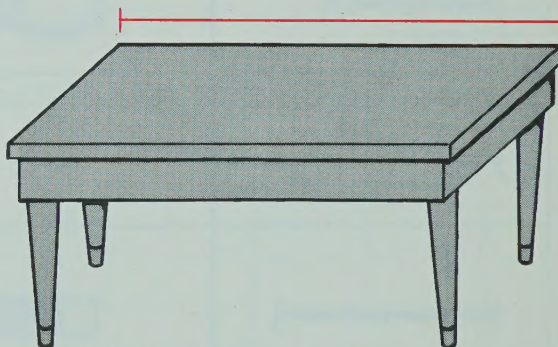
\_\_\_\_\_ units

3.



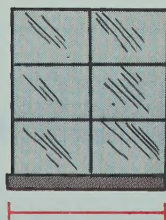
\_\_\_\_\_ units

4.



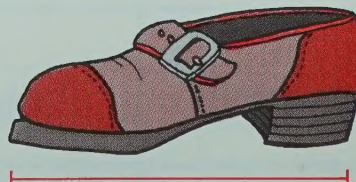
\_\_\_\_\_ units

5.



\_\_\_\_\_ units

6.



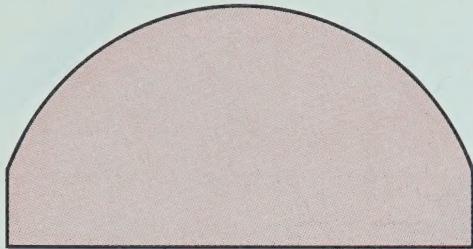
\_\_\_\_\_ units



## ● Finding the Distance Around

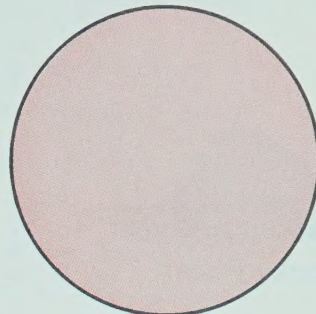
1. Can you find a way to measure the distance around these figures? Use centimeter units.

A



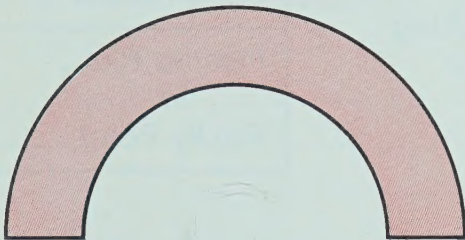
About \_\_\_\_ cm

B



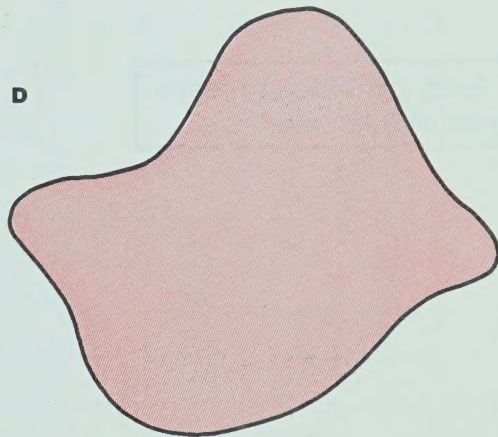
About \_\_\_\_ cm

C



About \_\_\_\_ cm

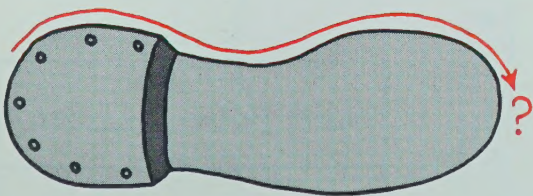
D



About \_\_\_\_ cm

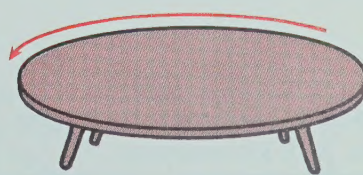
2. Can you find the distance around some objects such as the ones suggested by these pictures?

A



A Shoe: about \_\_\_\_ cm

B

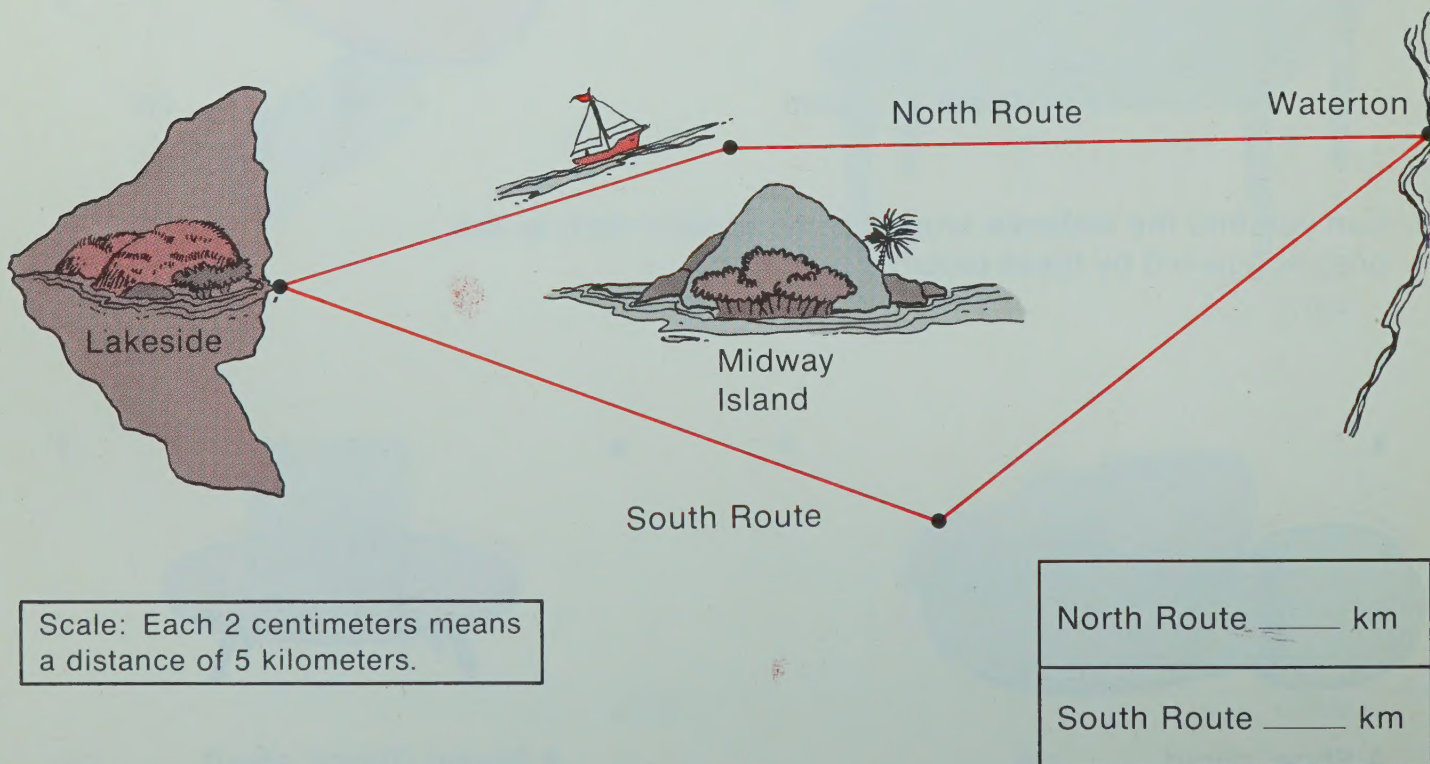
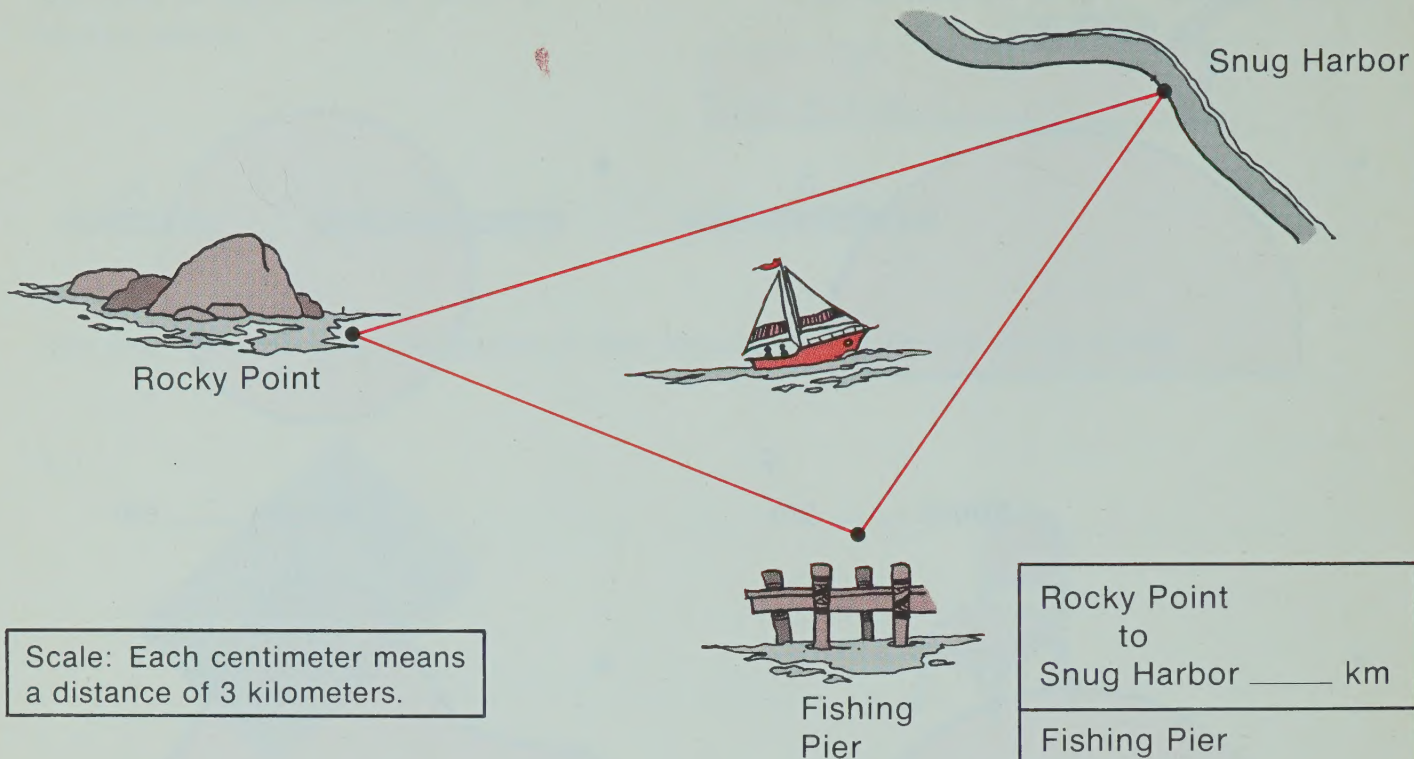


A Round Object: about \_\_\_\_ cm



## ● Distance on a Map

Use the map and scale to give the distances in kilometers.





## ● Area

1. Can you draw regions that have the given areas?  
Use the graph paper unit.

Square

Rectangle

A

B

Area: 36 square units

Area: 30 square units

Triangle

Triangle

C

D

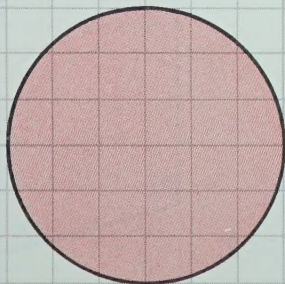
Area: 18 square units

Area: 24 square units

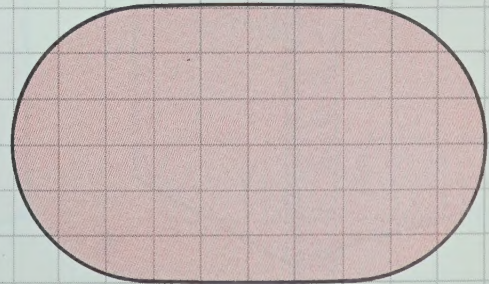
2. Estimate the area of each region.

A

B



\_\_\_\_\_ square units

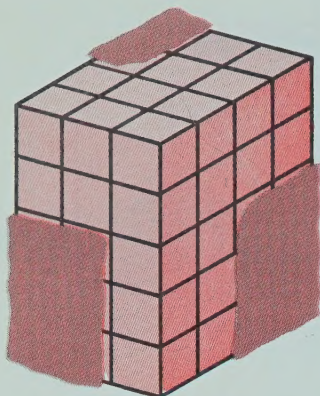


\_\_\_\_\_ square units



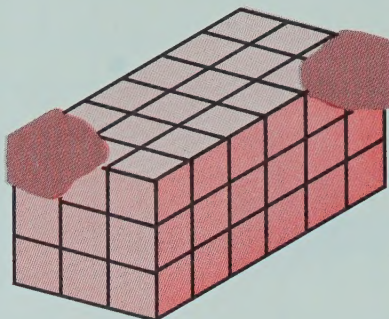
# ●Volume

Find the volume of each figure.



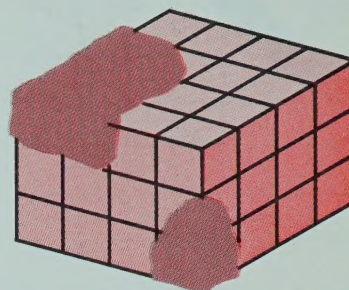
1.

\_\_\_\_\_ cubic units



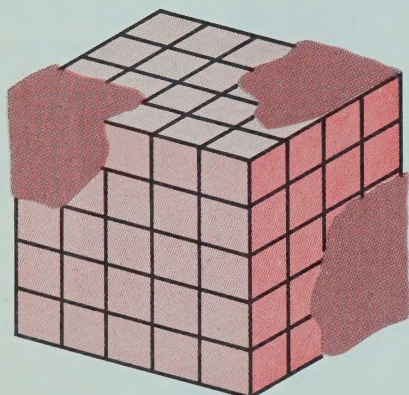
2.

\_\_\_\_\_ cubic units



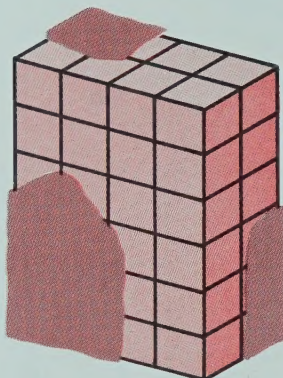
3.

\_\_\_\_\_ cubic units



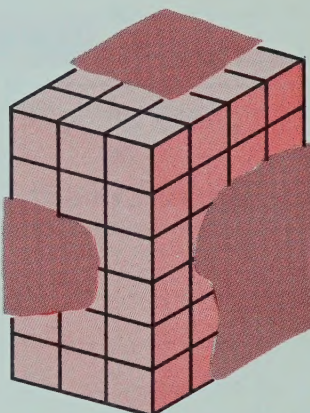
4.

\_\_\_\_\_ cubic units



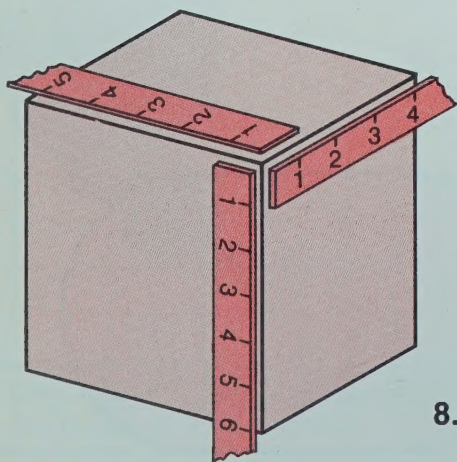
5.

\_\_\_\_\_ cubic units



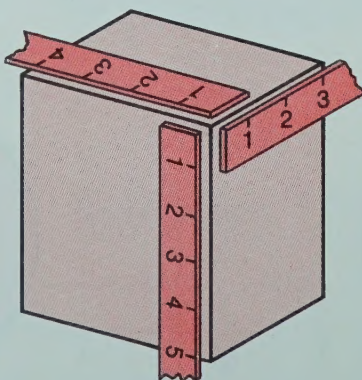
6.

\_\_\_\_\_ cubic units



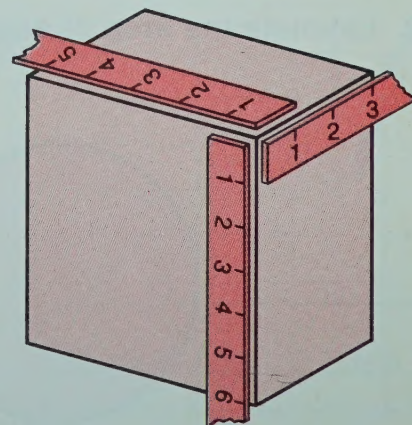
7.

\_\_\_\_\_ cubic units



8.

\_\_\_\_\_ cubic units



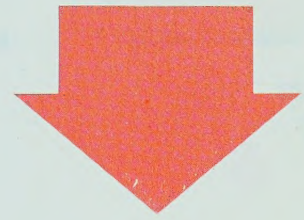
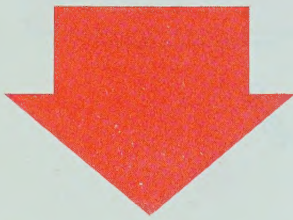
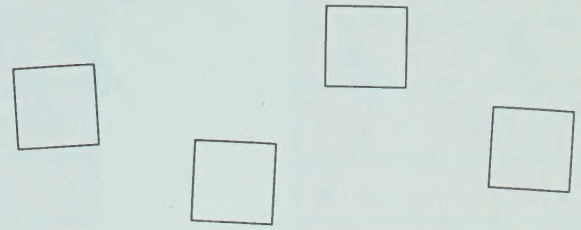
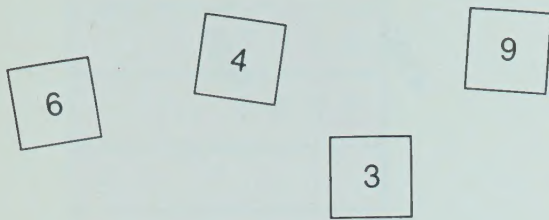
9.

\_\_\_\_\_ cubic units



The numbers below were built with the digits 6, 3, 4, 9. Complete the matching.

Choose your own set of digits. Use your digits to build numbers to match with the colored boxes.



9 3 6 4 •

9 6 4 3 •

3 4 6 9 •

6 4 9 3 •

4 9 6 3 •

• Largest •

• Fewest number of hundreds •

• Closest to 5000 •

• Largest number of tens •

• Smallest •

• □ □ □ □

• □ □ □ □

• □ □ □ □

• □ □ □ □

• □ □ □ □

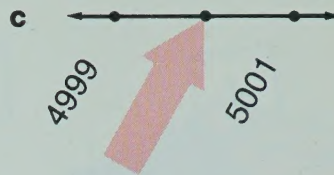
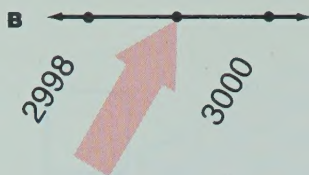
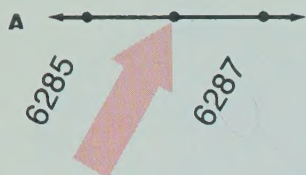


## ● Order of Numbers

Give the missing numbers.

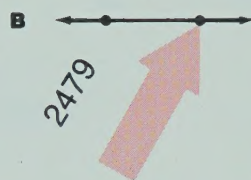
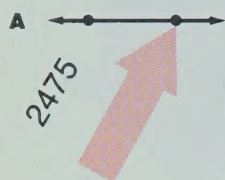
1.

Between



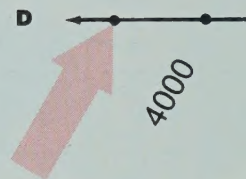
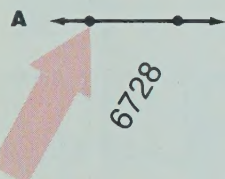
2.

After



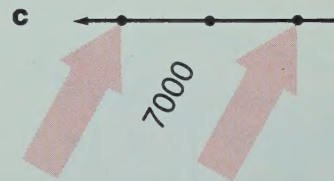
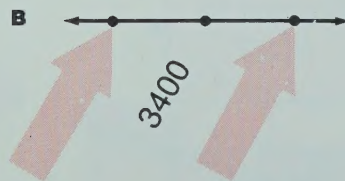
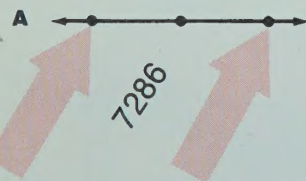
3.

Before



4.

Before and After



5.

Make some of your own





## Sequences with Large Numbers

Give the next three numbers in each table.

1.

3 2 6 5
3 2 6 6
3 2 6 7
<b>A</b>
<b>B</b>
<b>C</b>

2.

4 5 9 6
4 5 9 7
4 5 9 8
<b>A</b>
<b>B</b>
<b>C</b>

3.

2 9 9 7
2 9 9 8
2 9 9 9
<b>A</b>
<b>B</b>
<b>C</b>

4.

1 6,4 5 2
1 6,4 5 4
1 6,4 5 6
<b>A</b>
<b>B</b>
<b>C</b>

5.

3 5,6 2 7
3 5,7 2 7
3 5,8 2 7
<b>A</b>
<b>B</b>
<b>C</b>

6.

2 5,3 8 4
3 0,3 8 4
3 5,3 8 4
<b>A</b>
<b>B</b>
<b>C</b>

7.

2 6 8,4 8 3
2 7 8,4 8 3
2 8 8,4 8 3
<b>A</b>
<b>B</b>
<b>C</b>

8.

7 4 8,4 8 9
7 4 8,6 8 9
7 4 8,8 8 9
<b>A</b>
<b>B</b>
<b>C</b>

9.

6 0 3,1 2 3
6 5 3,1 2 3
7 0 3,1 2 3
<b>A</b>
<b>B</b>
<b>C</b>



## ● Large Numbers

1. With the numerals on these cards, you can “write” six different large numbers. How many of them can you write?

302

475

961

A 302, 475, 961

B \_\_\_\_\_

C \_\_\_\_\_

D \_\_\_\_\_

E \_\_\_\_\_

F \_\_\_\_\_

2. A Which of the six numbers above is largest? \_\_\_\_\_

B Which is smallest? \_\_\_\_\_

3. Give the correct sign  $>$  or  $<$  for each .

A 32,645,794  33,000,000


K 1,000,000,000  99,999,999

B 500,000,000  498,634,259

L 212,341,003  78,867,948

C 6,137,000  5,879,000

M 367,482,531  367,482,529

D 364,287,512  400,000,000

N 675,835,609  675,834,609

E 98,463,217  642,123,012

O 407,826,742  407,816,742

4. Make up six 9-digit numbers of your own.

A \_\_\_\_\_

B \_\_\_\_\_

C \_\_\_\_\_

D \_\_\_\_\_

E \_\_\_\_\_

F \_\_\_\_\_

5. Arrange your numbers above in order from smallest to largest.

A \_\_\_\_\_  
smallest

B \_\_\_\_\_

C \_\_\_\_\_

D \_\_\_\_\_

E \_\_\_\_\_

F \_\_\_\_\_  
largest



## ● Which Number is Larger?

Part of each slip of paper is missing. Each slip had two 8-digit numbers on it. When you can decide which of the two numbers is greater, ring it. When you can't decide, ring both numbers.

1.

3 8,2 8
3 4,3 0

2.

4,9 8 7
1 7,6 2 5

3.

6 8,	,7 8 3
6 8,4	,1 3 2

4.

,2 8 7,0 0 0
,3 0 0,0 0 0

5.

2 6,4 8 9,3 4 7
2 6,4 9 0,3 4

6.

7 5,4 8 9,6 5
7 5,4 8 9,6 5 3

7.

3 9,	,4 2 7
4 1,	,2 0 4

8.

7 6
6 9,8 4 7,

9.

8
8 2,3 4 7,6 4

10.

7 8 4,6 4 2
3 1,7 8 4,6 4 2

11.

6 8,2 3	4 4
6 8,2 3	4 3

12.

7 5,2 8 7,6 4 2
3,2 8 7,6 4 2

13.

9 9,9 9 9,9 9 9	
9 9,	9 8

14.

1 0,	1 0
1 0,0 0 0,0 0 0	

15.

8,6 4 3,2 8 7
9 2,6 4 3,2 8 7

16.

9 6,2 3 0,0 0 0
5,2 3 0,0 0 0

17.


3 6,4 0 7,
3 6,4 1 7,3 2

18.













9 8,3	2 7
9 8,4 6	,2 7 0



## ● Using Powers of 10 in Place Value

1. Study the chart. Then give the correct sign  $>$  or  $<$  for each 

$10^2 = 100$	$10^6 = 1,000,000$
$10^3 = 1000$	$10^7 = 10,000,000$
$10^4 = 10,000$	$10^8 = 100,000,000$
$10^5 = 100,000$	

- |  |   |
|--|---|
| <b>A</b> 98,765  $10^5$     | <b>G</b> $10^8$  111,111,111   |
| <b>B</b> 98,765  $10^6$     | <b>H</b> 100,000,001  $10^8$ |
| <b>C</b> $10^8$  34,178,654 | <b>I</b> 999,999,999  $10^8$ |
| <b>D</b> $10^7$  34,178,654 | <b>J</b> 99,999,999  $10^8$  |
| <b>E</b> $10^6$  9,999,999  | <b>K</b> $10^7$  88,888,888    |
| <b>F</b> $10^6$  999,999    | <b>L</b> $10^6$  8,888,888     |

2. **A** What number is one more than  $10^5$ ? \_\_\_\_\_
- B** What number is 675 more than  $10^3$ ? \_\_\_\_\_
- C** What number is one less than  $10^7$ ? \_\_\_\_\_
- D** What number is 7463 more than  $10^6$ ? \_\_\_\_\_
- E** What number is one less than  $10^8$ ? \_\_\_\_\_

3. **A** Write the number for  $10^9$ . \_\_\_\_\_
- B** Write the number that is one less than  $10^9$ . \_\_\_\_\_

4. Find the sums.

EXAMPLE:  $10^4 + 10^2 = 10,100$

- |  |  |
|--|--|
| <b>A</b> $10^3 + 10^2$ _____               | <b>F</b> $10^8 + 10^6 + 10^4 + 10^2$ _____ |
| <b>B</b> $10^4 + 10^3$ _____               | <b>G</b> $10^2 - 1$ _____                  |
| <b>C</b> $10^5 + 10^3$ _____               | <b>H</b> $10^3 - 1$ _____                  |
| <b>D</b> $10^4 + 10^3 + 10^2$ _____        | <b>I</b> $10^6 - 1$ _____                  |
| <b>E</b> $10^5 + 10^4 + 10^3 + 10^2$ _____ |  |



Give the missing numbers or function rule.

**1.**      Function Rule

Double and Add 4

Input	Output
5	14
3	10
7	18
<b>A</b> 6	
<b>B</b> 8	
<b>C</b> 9	

**2.**      Function Rule

Double and Subt 3

Input	Output
2	1
7	11
6	9
<b>A</b> 5	
<b>B</b> 4	
<b>C</b> 9	

**3.**      Function Rule

**A**

Input	Output
7	4
13	10
6	3
3	0
<b>B</b> 8	
<b>C</b> 5	

**4.**      Function Rule

**A**

Input	Output
6	12
8	16
7	14
<b>B</b> 9	
<b>C</b> 5	
<b>D</b> 4	

**5.**      Function Rule

**A**

Input	Output
6	13
5	11
7	15
<b>B</b> 9	
<b>C</b> 3	
<b>D</b> 4	

**6.**      Function Rule

**A**

Input	Output
2	0
4	4
7	10
<b>B</b> 6	
<b>C</b> 8	
<b>D</b> 9	

**7.**      Function Rule


**A**








Input	Output
6	18
2	6
5	15
<b>B</b> 4	
<b>C</b> 3	
<b>D</b> 0	


**8.**      Function Rule








Input	Output
7	1
4	0
5	1
8	0
9	1
2	0

Give the missing number pair for each row.

**9.**      Sum  Difference

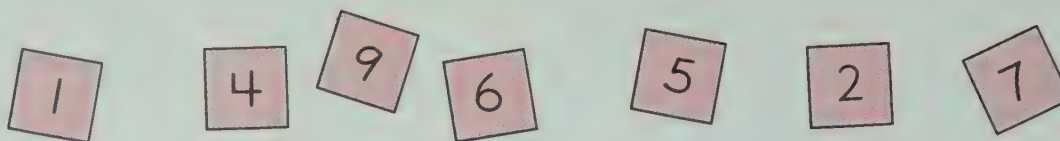
	11	6		5	1
	12	9		3	6
<b>A</b>	13				1
<b>B</b>	17				1
<b>C</b>	15				1
<b>D</b>	14				2
<b>E</b>	13				3

**10.**      Sum  Difference

<b>A</b>	12				0
<b>B</b>	18				0
<b>C</b>	16				0
<b>D</b>	14				0
<b>E</b>	10				8
<b>F</b>	9				7
<b>G</b>	8				6



## ● Adding and Checking



Can you find 3 numbers on the cards whose sum is this number?

Your first equation is correct if the sum of the numbers on the other cards is this number. Check to see.



1. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 15$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 19$

Try it again with these sums.

2. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 17$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 17$

3. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 16$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 18$

Try it with a new set of cards.



First Equation:

Check:

4. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 17$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 14$

5. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 12$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 19$

6. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 16$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 15$

7. **A**  $\underline{\quad} + \underline{\quad} + \underline{\quad} = 13$

**B**  $\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = 18$

Make a set of cards and equation pairs of your own. Try them on a classmate.



## ● Finding Sums

1. Find the sums.

**A**    3 7  
+ 8 5  
-----

**B**    6 8  
+ 9 2  
-----

**C**    7 6 4  
+ 8 4 9  
-----

**D**    9 6 7  
+ 8 6 8  
-----

**E**    7 6 4 3  
+ 4 8 2 9  
-----

**F**    7 6 3  
8 4 2  
+ 9 7 6  
-----

**G**    9 3 4  
8 2 1  
+ 1 0 9  
-----

**H**    8 4 6  
7 3 8  
+ 4 2 6  
-----

**I**    7 4 2 7  
8 3 6 8  
+ 7 2 1 0  
-----

**J**    6 2 4 3  
9 6 0 5  
+ 7 8 7 6  
-----

**K**    6 3 7 4  
8 6 7 5  
+ 3 2 9 4  
-----


**L**    8 4 6 7  
5 3 9 6  
+ 9 8 1 0  
-----


**M**    7 6 5 4  
8 3 3 9  
7 4 6 5  
+ 8 3 7 6  
-----

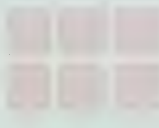
**N**    9 4 6 2  
8 4 8 7  
6 5 3 8  
+ 9 5 6 7  
-----


**O**    3 5,6 7 8  
9 7,6 0 5  
3 8,7 6 5  
+ 9 2,7 6 8  
-----


2. Make some addition problems of your own that have these sums.  
Have a classmate check your problems.

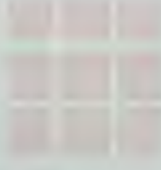
**A**      
+  
-----  
1 3 4


**B**      
+  
-----  
1 4 6 3


**C**      
+  
-----  
1 9 6 2

**D**      
+  
-----  
1 5, 0 3 0

**E**      
+  
-----  
1 9 2

**F**      
+  
-----  
2 3 6 4

**G**      
+  
-----  
2 8 6 5

**H**      
+  
-----  
2 9, 0 3 0

## ● Magic Squares

1. Complete each square to make it a magic square.

**A**

8	9	4
3		11
	5	

**B**

12		
7		
8	13	

**C**

		14
	11	7
		12

**D**

14	9	13	
4		7	16
3	12		15
17	6	10	

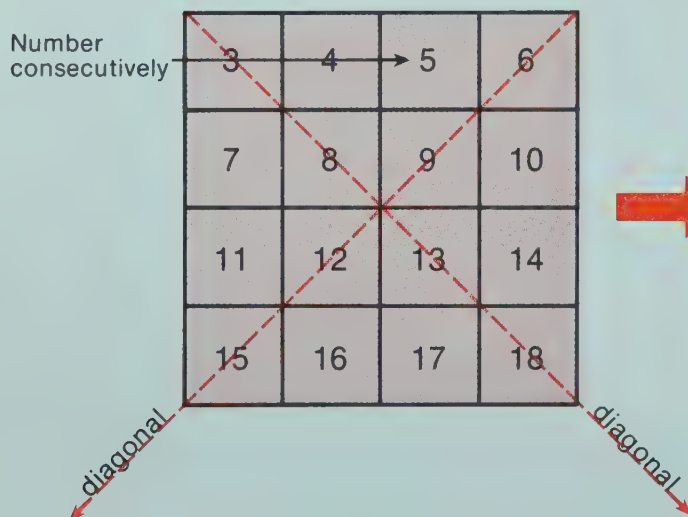
**E**

8	13	9	20
18		15	6
19			
	16	12	

**F**

		2	
4		9	7
8			11
3	13	14	0

2. Follow directions to make your own 4 by 4 magic square.



18	4	5	15
7	13	12	10
11	9	8	14
6	16	17	3

Start with a blank square

- A** Put in the numbers not on the colored lines (shown in black above).
- B** Reverse the diagonals as shown in red above.

3. Now you make a magic square using a different set of consecutive numbers.



# Subtracting

1. Find the differences.

**A** 
$$\begin{array}{r} 72 \\ - 37 \\ \hline \end{array}$$

**B** 
$$\begin{array}{r} 346 \\ - 179 \\ \hline \end{array}$$

**C** 
$$\begin{array}{r} 6302 \\ - 1445 \\ \hline \end{array}$$

**D** 
$$\begin{array}{r} 7435 \\ - 896 \\ \hline \end{array}$$

**E** 
$$\begin{array}{r} 30,265 \\ - 17,283 \\ \hline \end{array}$$

**F** 
$$\begin{array}{r} 1000 \\ - 6 \\ \hline \end{array}$$

**G** 
$$\begin{array}{r} 10,000 \\ - 1 \\ \hline \end{array}$$

**H** 
$$\begin{array}{r} 100,000 \\ - 100 \\ \hline \end{array}$$

**I** 
$$\begin{array}{r} 100,000 \\ - 900 \\ \hline \end{array}$$

**J** 
$$\begin{array}{r} 100,000 \\ - 10,101 \\ \hline \end{array}$$

**K** 
$$\begin{array}{r} 604 \\ - 138 \\ \hline \end{array}$$

**L** 
$$\begin{array}{r} 700 \\ - 248 \\ \hline \end{array}$$

**M** 
$$\begin{array}{r} 6003 \\ - 5276 \\ \hline \end{array}$$

**N** 
$$\begin{array}{r} 70,304 \\ - 13,678 \\ \hline \end{array}$$

**O** 
$$\begin{array}{r} 60,003 \\ - 7,438 \\ \hline \end{array}$$

**P** 
$$\begin{array}{r} 50,901 \\ - 12,493 \\ \hline \end{array}$$

2. Solve the equations.

**A**  $3465 - 1783 = n$

**B**  $6204 - 3466 = n$

**C**  $7004 - 838 = n$

**D**  $9682 - 99 = n$

**E**  $4003 - 764 = n$

**F**  $7765 - 693 = n$

3. Make some subtraction problems of your own that have these differences.  
Have a classmate check your problems.

**A** 
$$\begin{array}{r} \phantom{0000} \\ \hline 344 \end{array}$$

**B** 
$$\begin{array}{r} \phantom{0000} \\ \hline 28 \end{array}$$

**C** 
$$\begin{array}{r} \phantom{0000} \\ \hline 73 \end{array}$$

**D** 
$$\begin{array}{r} \phantom{0000} \\ \hline 1642 \end{array}$$

**E** 
$$\begin{array}{r} \phantom{0000} \\ \hline 307 \end{array}$$

**F** 
$$\begin{array}{r} \phantom{0000} \\ \hline 2834 \end{array}$$

**G** 
$$\begin{array}{r} \phantom{0000} \\ \hline 3076 \end{array}$$

**H** 
$$\begin{array}{r} \phantom{0000} \\ \hline 4369 \end{array}$$

## ● Reconstruction Problems

1. Fill in the missing digits.

$$\begin{array}{r} \text{A} \quad 7 \quad \square \quad 3 \\ - 1 \quad 5 \quad 8 \\ \hline 5 \quad 6 \quad 5 \end{array}$$

$$\begin{array}{r} \text{B} \quad \square \quad \square \quad 1 \quad 6 \\ - 3 \quad 4 \quad 2 \\ \hline 7 \quad 4 \end{array}$$

$$\begin{array}{r} \text{C} \quad 7 \quad 8 \quad 2 \quad 3 \\ - 1 \quad 5 \quad 6 \quad \square \\ \hline 6 \quad 2 \quad 6 \quad 3 \end{array}$$

$$\begin{array}{r} \text{D} \quad 6 \quad 2 \quad 5 \quad 2 \\ - 1 \quad 3 \quad 4 \quad \square \\ \hline 4 \quad 9 \quad 0 \quad 3 \end{array}$$

$$\begin{array}{r} \text{E} \quad 3 \quad \square \quad 2 \\ - 1 \quad 0 \quad 6 \\ \hline 2 \quad 3 \quad 6 \end{array}$$

$$\begin{array}{r} \text{F} \quad \square \quad \square \quad 5 \\ - \quad 3 \quad 8 \\ \hline 6 \quad 6 \quad 7 \end{array}$$

$$\begin{array}{r} \text{G} \quad 5 \quad \square \quad 3 \quad 8 \\ - \quad 1 \quad 5 \quad 9 \\ \hline 5 \quad 4 \quad \square \quad 9 \end{array}$$


$$\begin{array}{r} \text{H} \quad 3 \quad 6 \quad \square \quad \square \\ - 1 \quad \square \quad 6 \quad 4 \\ \hline \quad 9 \quad 4 \quad 0 \end{array}$$

$$\begin{array}{r} \text{I} \quad \square \quad \square \quad 0 \quad 0 \\ - 1 \quad 0 \quad 5 \\ \hline 5 \quad \square \quad 5 \end{array}$$

$$\begin{array}{r} \text{J} \quad \square \quad 4 \quad \square \\ - \quad 5 \quad 9 \\ \hline 6 \quad \square \quad 4 \end{array}$$

$$\begin{array}{r} \text{K} \quad \square \quad 0 \quad \square \quad 0 \\ - \quad 4 \quad 8 \quad \square \\ \hline 6 \quad \square \quad 7 \quad 2 \end{array}$$

$$\begin{array}{r} \text{L} \quad 9 \quad \square \quad \square \quad 1 \\ - \quad 8 \quad 3 \quad \square \\ \hline \quad 1 \quad 6 \quad 8 \end{array}$$

2. Can you decide whether the problem is addition or subtraction, without seeing the missing digits? Put the correct sign (+) or (−) in the .

$$\begin{array}{r} \text{A} \quad \square \quad \square \\ \square \quad \square \\ \hline \square \quad \square \end{array}$$

$$\begin{array}{r} \text{B} \quad \square \quad \square \quad \square \\ \square \quad \square \quad \square \\ \hline \square \quad \square \end{array}$$

$$\begin{array}{r} \text{C} \quad \square \quad \square \quad \square \\ \square \quad \square \quad \square \\ \hline \square \quad \square \quad \square \end{array}$$

$$\begin{array}{r} \text{D} \quad \square \quad \square \quad \square \quad \square \\ \square \quad \square \quad \square \quad \square \\ \hline \square \quad \square \quad \square \quad \square \end{array}$$

$$\begin{array}{r} \text{E} \quad \square \quad \square \quad \square \\ \square \quad \square \quad \square \\ \hline 9 \quad \square \quad \square \end{array}$$

$$\begin{array}{r} \text{F} \quad \square \quad \square \quad \square \\ \square \quad \square \quad \square \\ \hline 1 \quad \square \quad \square \end{array}$$

$$\begin{array}{r} \text{G} \quad \square \quad 6 \quad \square \\ \square \quad 0 \quad 8 \\ \hline \square \quad 5 \quad 3 \end{array}$$

$$\begin{array}{r} \text{H} \quad 9 \quad \square \quad \square \\ 7 \quad \square \quad \square \\ \hline \square \quad \square \quad \square \end{array}$$



## Solving Problems

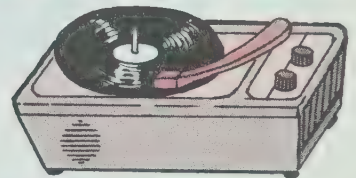
Read the problem carefully. Then put in numbers that make sense.  
Solve your problem.

1. Jefferson School has \_\_\_\_\_ members in the band. Lincoln School has \_\_\_\_\_. How many more does Lincoln School have?

2. Ted had \_\_\_\_\_ tickets to sell for the school play.  
Lynn had \_\_\_\_\_. How many did they have in all?



3. Ginny had \_\_\_\_\_ records. She bought \_\_\_\_\_ new ones and gave away \_\_\_\_\_. How many does she have now?



4. Joe had \_\_\_\_\_ baseball cards. He gave \_\_\_\_\_ to Fred and \_\_\_\_\_ to Jerry. How many does he have left?



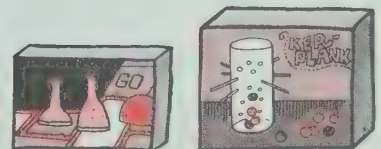
5. Mary had \_\_\_\_\_ dollars. She spent \_\_\_\_\_ for socks and \_\_\_\_\_ for gloves. How much does she have left?



6. Harry earned \_\_\_\_\_ for mowing a lawn and \_\_\_\_\_ cleaning the garage. He spent \_\_\_\_\_ for a snack. How much does he have left from his earnings?

7. Ann earned \_\_\_\_\_ in one week for baby sitting. She earned \_\_\_\_\_ the next week and \_\_\_\_\_ the third week. How much did she earn in three weeks?

8. Larry had \_\_\_\_\_ dollars. How much change should he get if he bought 2 games at \_\_\_\_\_ each?



## ● Writing Your Own Problems

Write and solve your own story problem for each picture.

1.



---

---

---

---

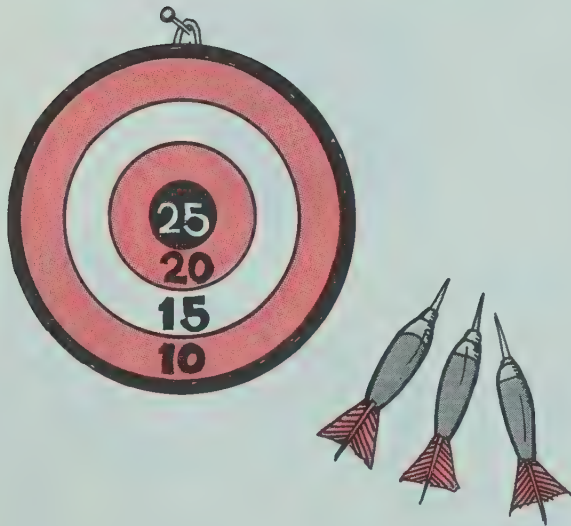
---

---

---

---

2.



---

---

---

---

---

---

---

---

3.

Population Figures	
City	Pop.
Marysville	23,487
Greensbury	56,103
Middletown	7,286
Rockton	103,785

---

---

---

---

---

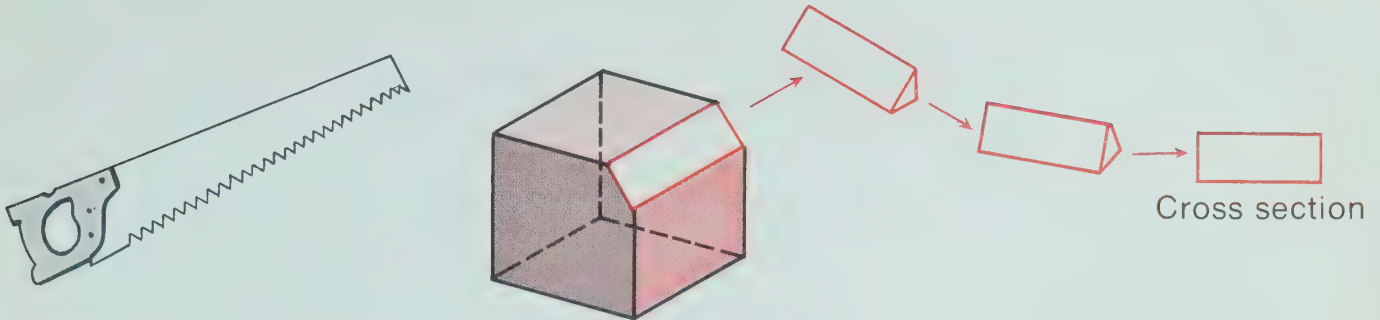
---

---

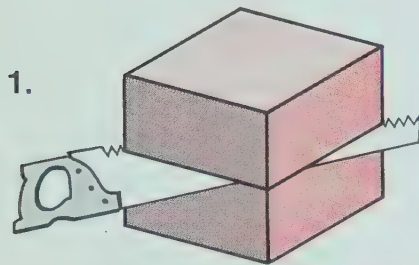
---



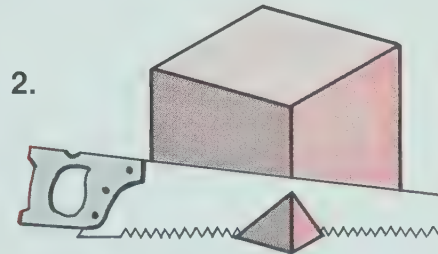
The figure below explains a cross section.  
Think of cutting a piece off of a cube.



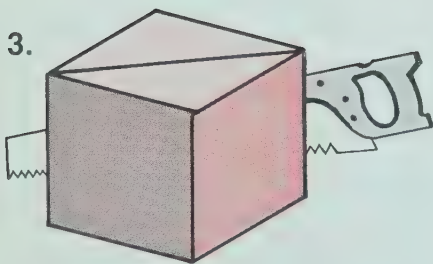
Draw a picture of the cross section for each cut shown below.  
Part 1 is an example.



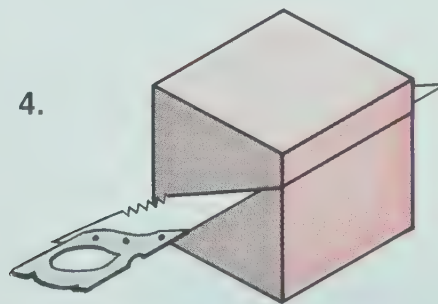
Cross section



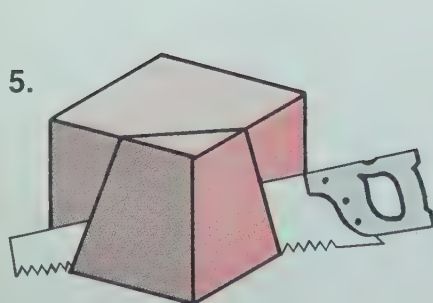
Cross section



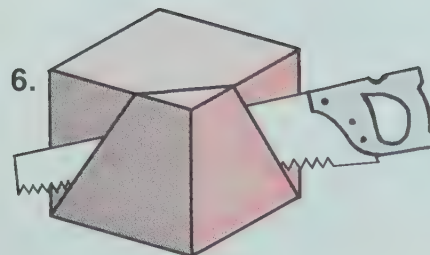
Cross section



Cross section



Cross section



Cross section

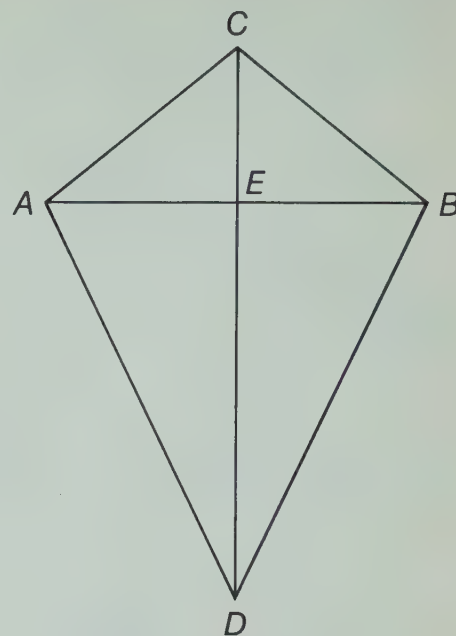
## ● Segments, Rays, and Angles

1. How many segments can you find and name on this figure?

\_\_\_\_\_

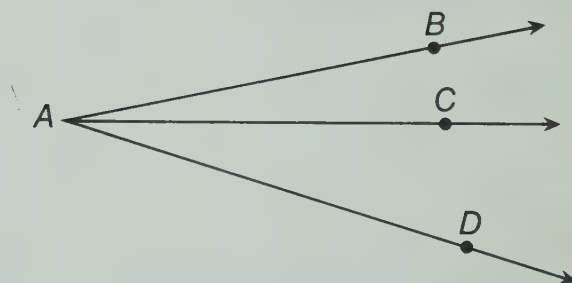
\_\_\_\_\_

\_\_\_\_\_



2. This figure shows 3 angles,  $BAC$ ,  $BAD$ , and  $CAD$ . Draw another ray from point  $A$ . Put a point  $E$  on your ray. Name as many "new" angles as you can.

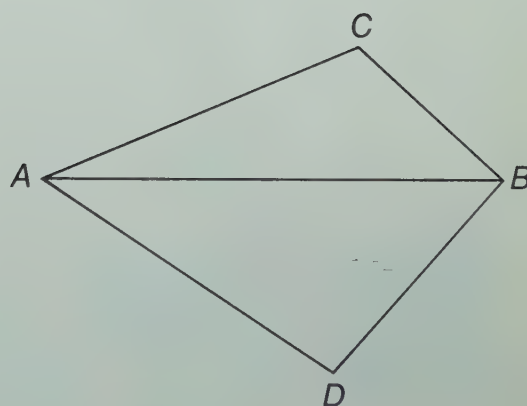
\_\_\_\_\_



3. How many angles can you find and name on this figure?

\_\_\_\_\_

\_\_\_\_\_





## ● Parallel Lines

1. The symbol for parallel is  $\parallel$ .

We write

$\ell \parallel m$

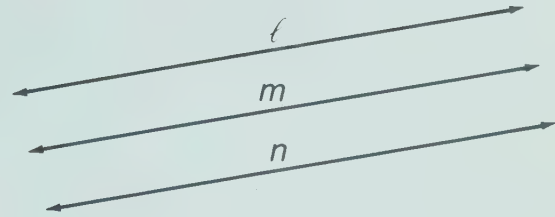


and read

$\ell$  is parallel to  $m$

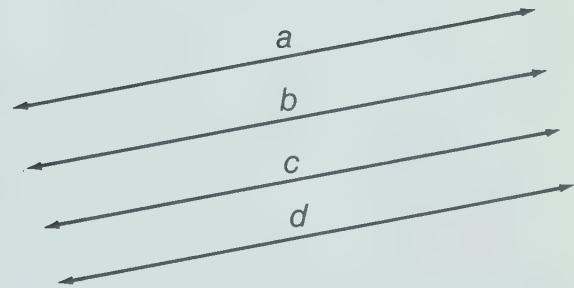
What other pairs of parallel lines can you find and record in the picture?

\_\_\_\_\_



2. How many pairs of parallel lines can you name in this figure?

\_\_\_\_\_  
\_\_\_\_\_



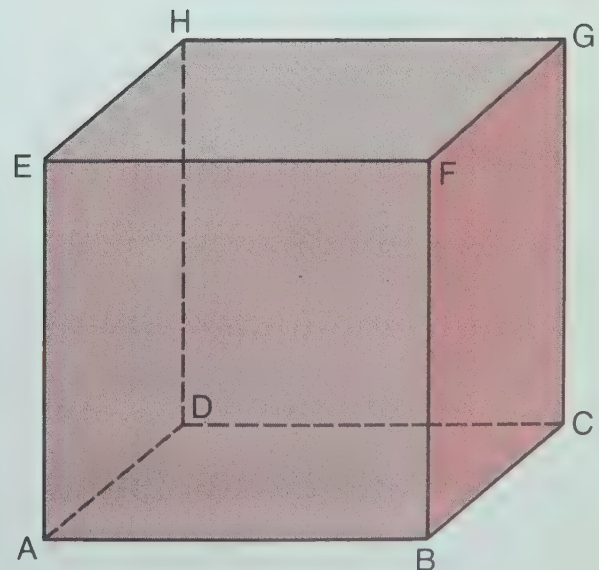
3. How many pairs of parallel edges can you find on the cube? Three of them are given below.

$AB \parallel EF$

$AB \parallel HG$

$AB \parallel DC$

\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_  
\_\_\_\_\_



## ● Space Figures

Here are two interesting geometric figures. You can make them with the patterns shown below. Can you give the number of faces, edges, and vertices of each figure?

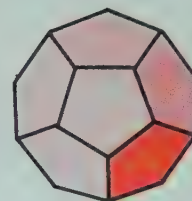


Icosahedron

Faces \_\_\_\_\_

Edges \_\_\_\_\_

Vertices \_\_\_\_\_

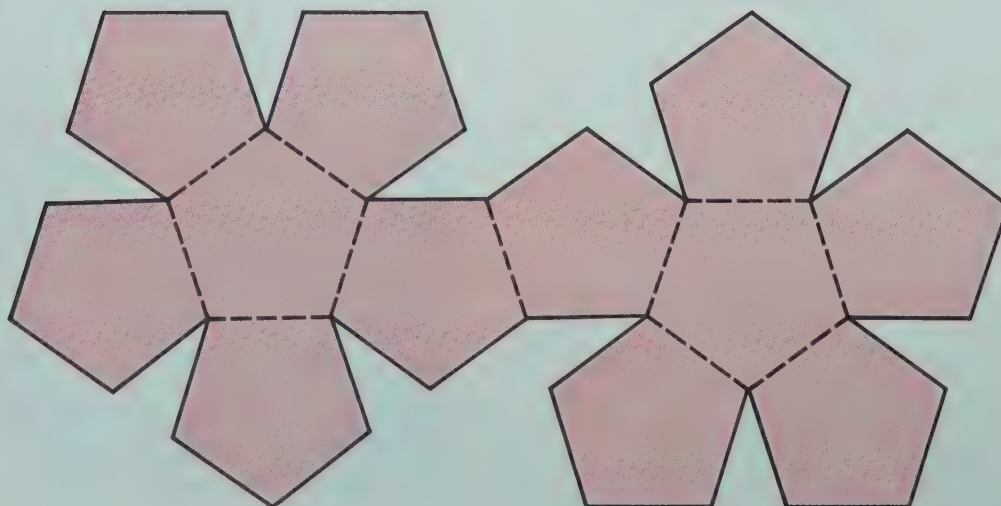
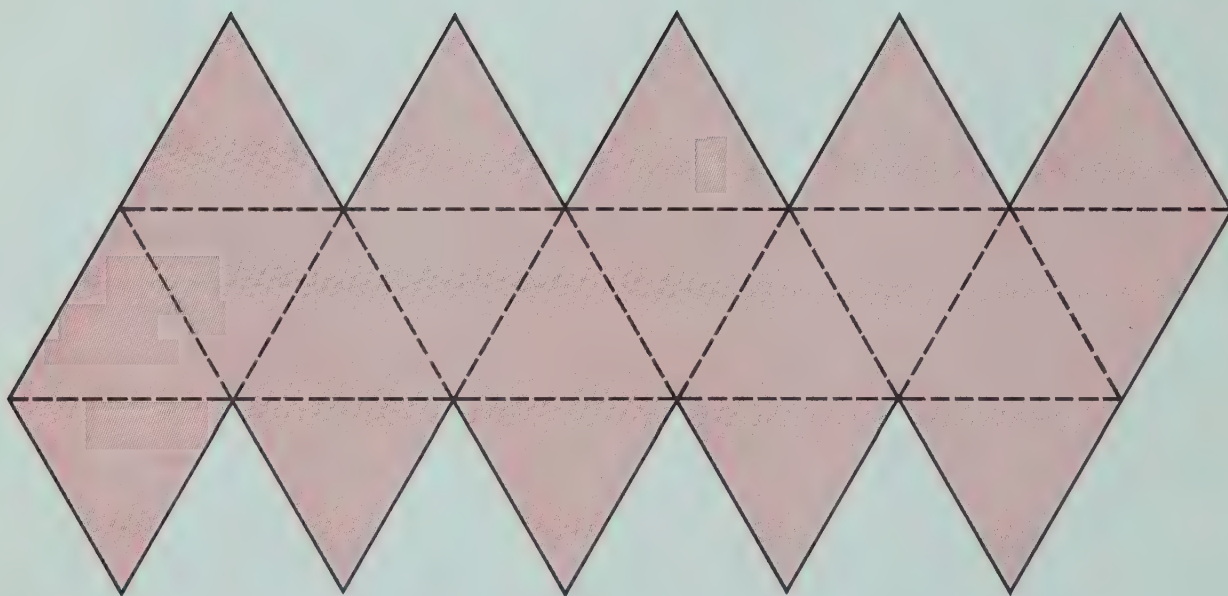


Dodecahedron

Faces \_\_\_\_\_

Edges \_\_\_\_\_

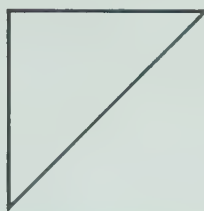
Vertices \_\_\_\_\_



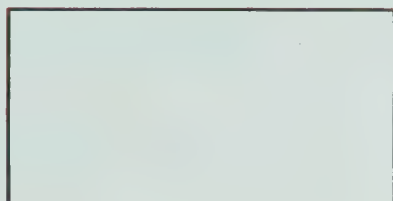


## ● Polygons

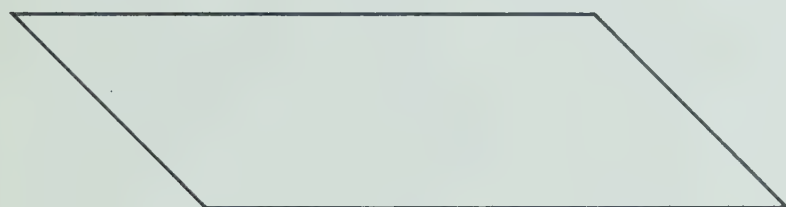
Trace and cut out two of each triangle.  
Use some or all of your triangles to make these special polygons. Draw lines inside the figures to show how you placed the triangles.



Square



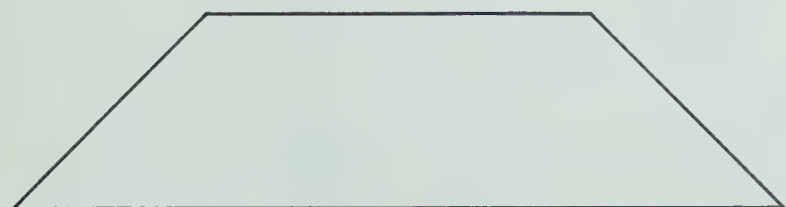
Rectangle



Parallelogram



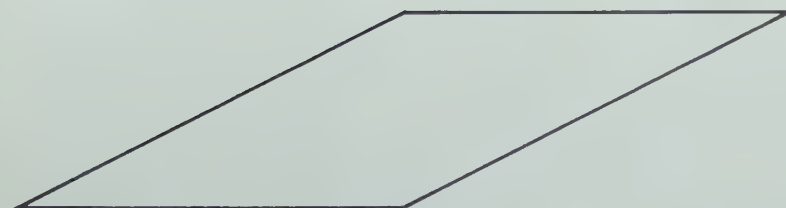
Pentagon



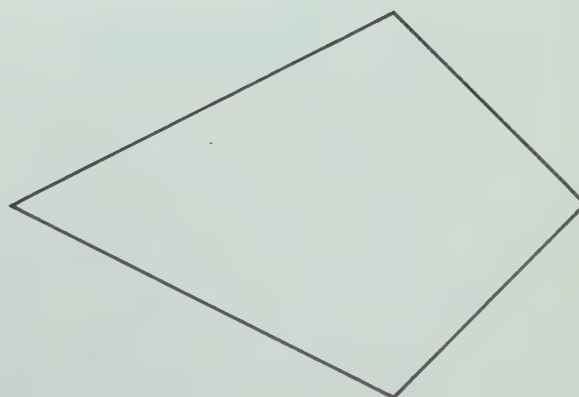
Trapezoid



Triangle



Parallelogram



Quadrilateral

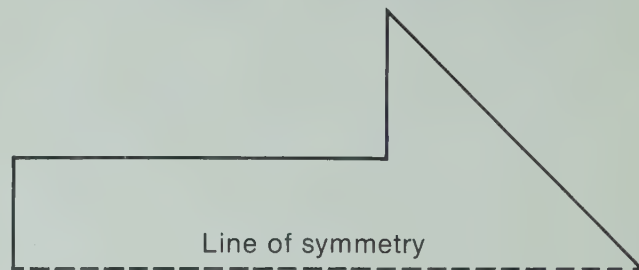
## Symmetric Figures

Without cutting out or folding this page, can you find a way to draw “the other half” of each figure so you have a symmetric figure.

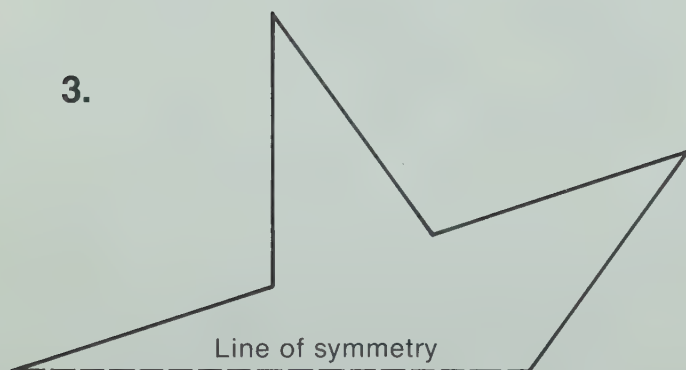
1.



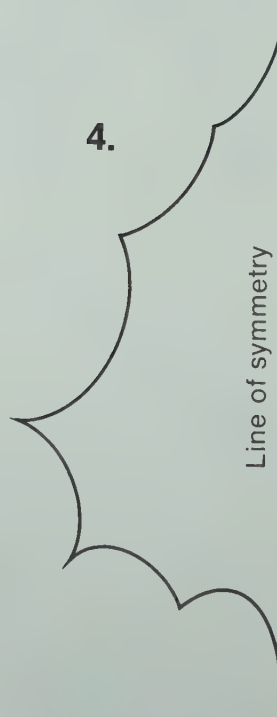
2.



3.



4.





1. Complete each sequence.

A 0, 2, 4, 6, , , , , ,

B 0, 3, 6, 9, , , , , ,

C 0, 4, 8, 12, , , , , ,

D 0, 5, 10, 15, , , , , ,

E 0, 6, 12, 18, , , , , ,

F 0, 7, 14, 21, , , , , ,

G 0, 8, 16, 24, , , , , ,

H 0, 9, 18, 27, , , , , ,

2. Solve the equations. The sequences above may help you.

A  $6 \times 2 =$  \_\_\_\_\_

$8 \times 2 =$  \_\_\_\_\_

$18 \div 2 =$  \_\_\_\_\_

B  $7 \times 3 =$  \_\_\_\_\_

$5 \times 3 =$  \_\_\_\_\_

$24 \div 3 =$  \_\_\_\_\_

C  $9 \times 4 =$  \_\_\_\_\_

$6 \times 4 =$  \_\_\_\_\_

$28 \div 4 =$  \_\_\_\_\_

D  $8 \times 5 =$  \_\_\_\_\_

$7 \times 5 =$  \_\_\_\_\_

$45 \div 5 =$  \_\_\_\_\_

E  $9 \times 6 =$  \_\_\_\_\_

$5 \times 6 =$  \_\_\_\_\_

$48 \div 6 =$  \_\_\_\_\_

F  $4 \times 7 =$  \_\_\_\_\_

$8 \times 7 =$  \_\_\_\_\_

$63 \div 7 =$  \_\_\_\_\_

G  $7 \times 8 =$  \_\_\_\_\_

$9 \times 8 =$  \_\_\_\_\_

$64 \div 8 =$  \_\_\_\_\_

H  $6 \times 9 =$  \_\_\_\_\_

$8 \times 9 =$  \_\_\_\_\_

$45 \div 9 =$  \_\_\_\_\_

## ● Using Logic to Find Products

1. Use the table to help you find these products.

**A**  $8 \times 8286 =$  \_\_\_\_\_

**B**  $6 \times 8286 =$  \_\_\_\_\_

**C**  $4 \times 7654 =$  \_\_\_\_\_

**D**  $6 \times 7654 =$  \_\_\_\_\_

**E**  $7 \times 9847 =$  \_\_\_\_\_

**F**  $5 \times 9847 =$  \_\_\_\_\_

**G**  $3 \times 7385 =$  \_\_\_\_\_

**H**  $5 \times 7385 =$  \_\_\_\_\_

$7 \times 8286 = 58,002$

$5 \times 7654 = 38,270$

$6 \times 9847 = 59,082$

$4 \times 7385 = 29,540$

$8 \times 3485 = 27,880$

$6 \times 7856 = 47,136$

**I**  $9 \times 3485 =$  \_\_\_\_\_

**J**  $7 \times 3485 =$  \_\_\_\_\_

**K**  $5 \times 7856 =$  \_\_\_\_\_

**L**  $7 \times 7856 =$  \_\_\_\_\_

2. Use this table to help you find these products.

**A**  $8 \times 786 =$  \_\_\_\_\_

**B**  $6 \times 786 =$  \_\_\_\_\_

**C**  $14 \times 786 =$  \_\_\_\_\_

**D**  $12 \times 786 =$  \_\_\_\_\_

**E**  $9 \times 963 =$  \_\_\_\_\_

**F**  $11 \times 963 =$  \_\_\_\_\_

**G**  $12 \times 963 =$  \_\_\_\_\_

**H**  $8 \times 963 =$  \_\_\_\_\_

**I**  $15 \times 3468 =$  \_\_\_\_\_

**J**  $17 \times 3468 =$  \_\_\_\_\_

**K**  $16 \times 3468 =$  \_\_\_\_\_

$3 \times 786 = 2358$

$5 \times 786 = 3930$

$9 \times 786 = 7074$

$7 \times 3468 = 24,276$

$8 \times 3468 = 27,744$

$9 \times 3468 = 31,212$

$4 \times 963 = 3852$

$5 \times 963 = 4815$

$7 \times 963 = 6741$

$12 \times 638 = 7656$

$13 \times 638 = 8294$

$16 \times 638 = 10,208$

**L**  $18 \times 3468 =$  \_\_\_\_\_

**M**  $25 \times 638 =$  \_\_\_\_\_

**N**  $28 \times 638 =$  \_\_\_\_\_

**O**  $29 \times 638 =$  \_\_\_\_\_

**P**  $32 \times 638 =$  \_\_\_\_\_



## ● Multiplication Facts

Complete the table.

×	0	1	2	3	4	5	6	7	8	9
0										
1										
2										
3										
4										
5										
6										
7										
8										
9										

- Which products are in the table just one time? \_\_\_\_\_
- Some of the products are in the table exactly 3 times. How many of them can you find? \_\_\_\_\_
- No product other than zero appears more than 4 times. How many products can you find that appear 4 times? \_\_\_\_\_

- Choose one of your numbers from exercise 3. How many different multiplication equations can you write for your number?

_____	_____
_____	_____
_____	_____
_____	_____

## ● Multiplication Tables

1. Here is a multiplication chart with the numbers mixed up. Can you give the missing products?

×	8	2	5	9
6				
4				
7			35	
3	24			

2. These multiplication tables have both missing products and missing factors. Can you find the missing numbers in each one?

A

×				
		36		28
6			18	
	10			14
	20		12	

B

×		5		
	36			32
			6	
		10		16
	27		3	

C

×				
	18			
	6		7	
		12		8
			35	20

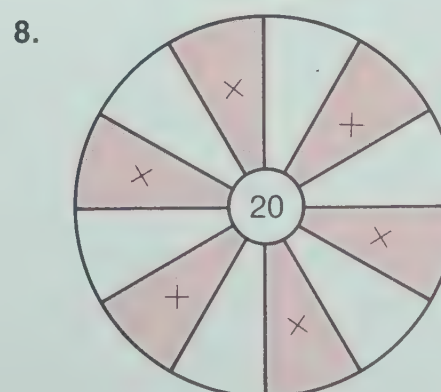
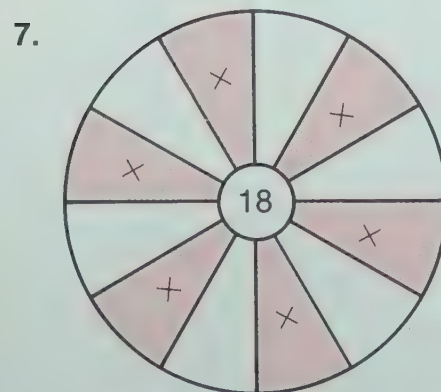
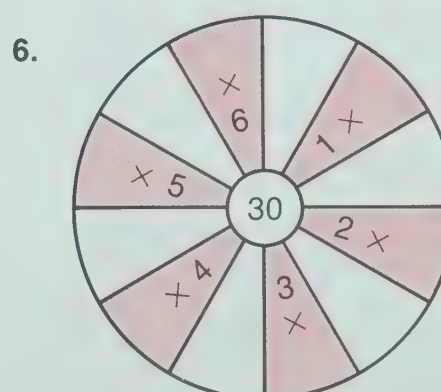
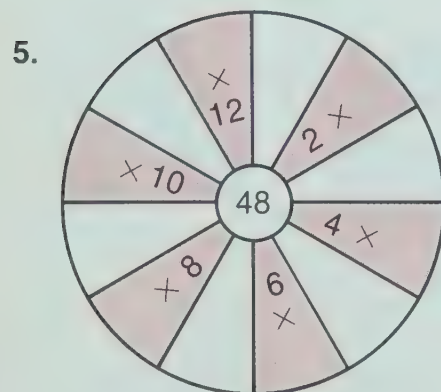
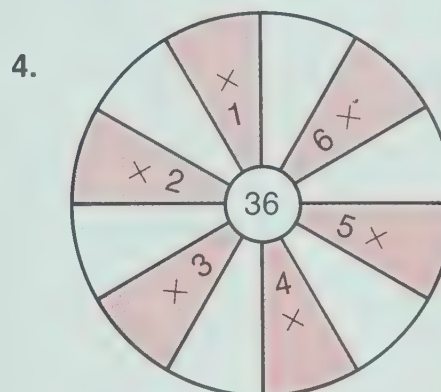
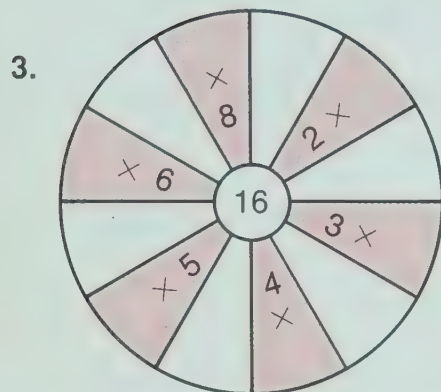
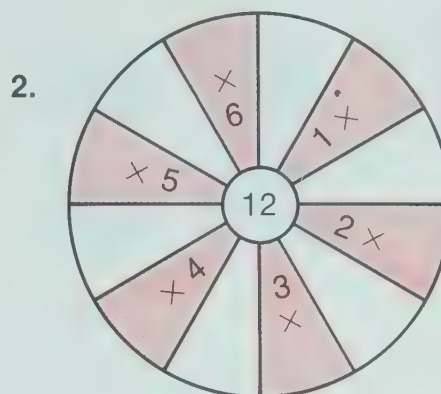
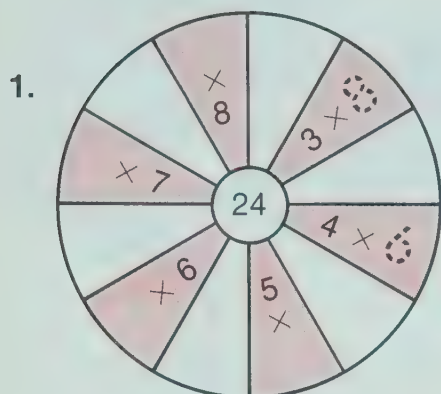
D

×				
		42	14	
	8			
		18		12
	9		18	



## ● Finding Missing Factors

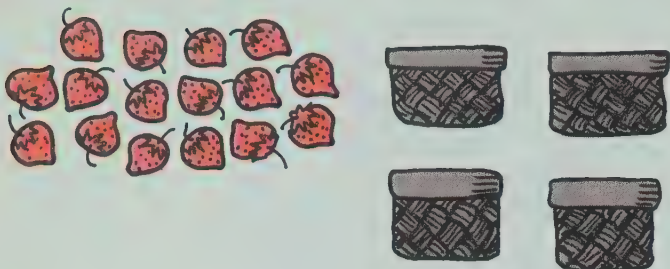
The number in the center should be the product of the two numbers on the spokes. Give as many missing spoke numbers as you can find. Some of the spokes can't be completed with whole numbers.



## ● Division and Sets

Write and solve a short story problem for each picture.

1.




---

---

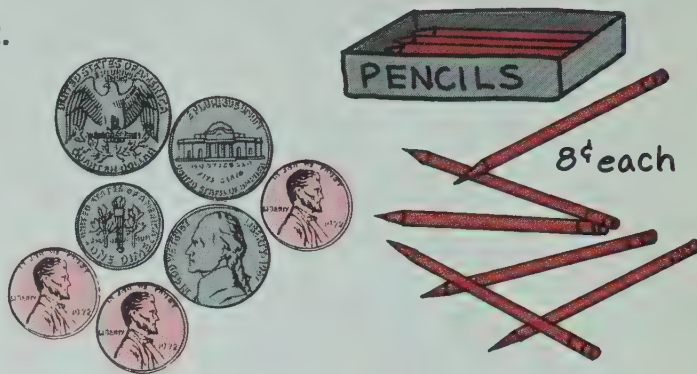
---

---

---

---

2.




---

---

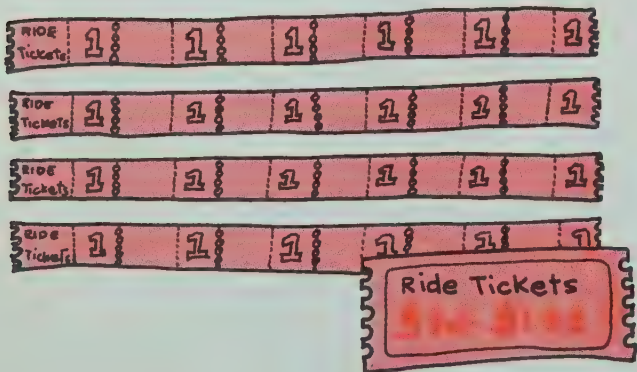
---

---

---

---

3.




---

---

---

---

---

---

4.




---

---

---

---

---

---

## ● Problem Solving



1. There were 17 boys and 18 girls going on the picnic. If 5 children ride in each car, how many cars are needed? \_\_\_\_\_

2. Put numbers in this problem that make sense. Then solve your problem.

Tam had \_\_\_\_\_ photographs. She put \_\_\_\_\_ on each page of her album.

How many pages did she use? \_\_\_\_\_

3. Make up a multiplication problem using these numbers: 4 and 7. Then solve your problem.

---

---

---

---

---

---

---

---

---

---

4. Write a division problem using numbers of your own choosing. Solve your problem.

---

---

---

---

---

---

---

---

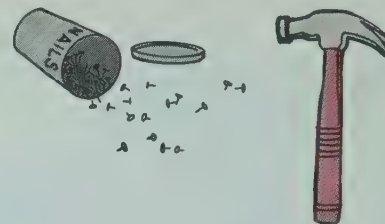
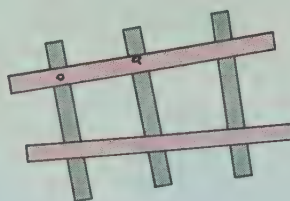
---

---

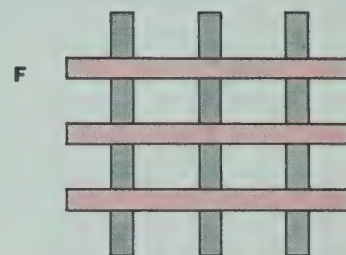
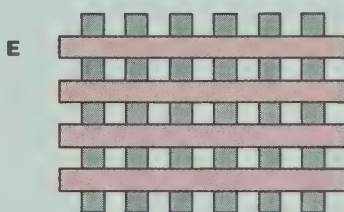
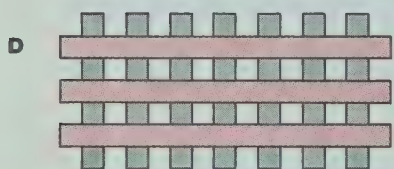
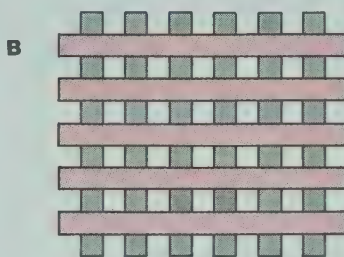
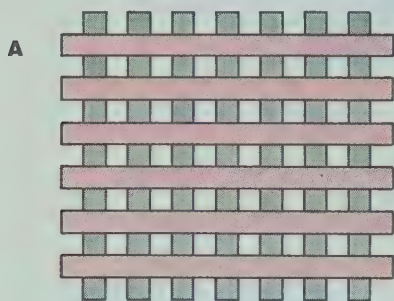


## ● Pairing and Multiplication

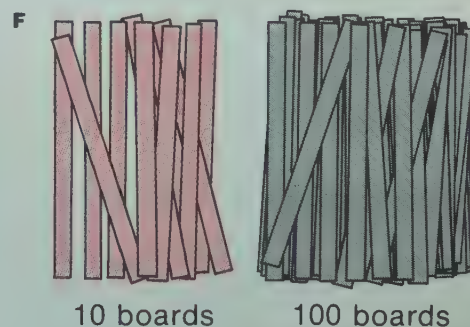
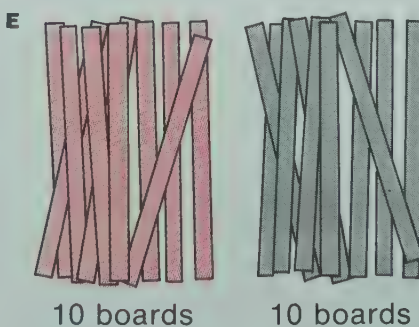
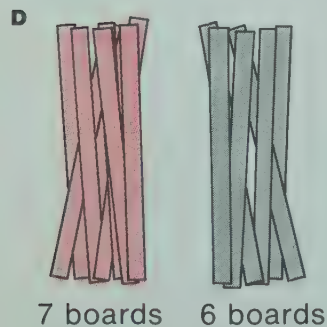
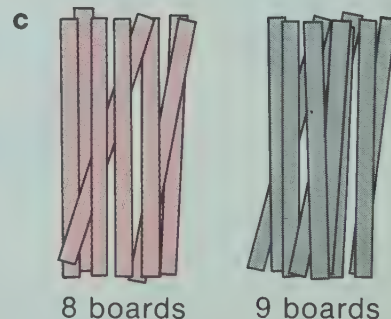
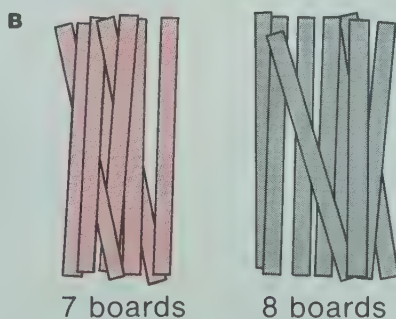
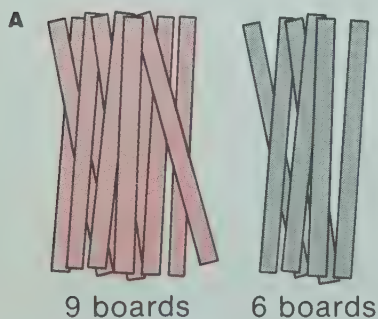
1. How many nails would it take to nail 5 boards together if you put one at each crossing?



2. Give the number of nails for each of these sets of boards.



3. Give the number of nails for each of these sets of boards if they are nailed together like those above.



1. Find the products.

A  $5 \times 70 =$  \_\_\_\_\_

F  $7 \times 80 =$  \_\_\_\_\_

B  $5 \times 700 =$  \_\_\_\_\_

G  $7 \times 800 =$  \_\_\_\_\_

C  $5 \times 7000 =$  \_\_\_\_\_

H  $7 \times 8000 =$  \_\_\_\_\_

D  $5 \times 70,000 =$  \_\_\_\_\_

I  $7 \times 80,000 =$  \_\_\_\_\_

E  $5 \times 700,000 =$  \_\_\_\_\_

J  $7 \times 800,000 =$  \_\_\_\_\_

2. Solve the equations.

A  $6 \times 8000 = n$

$n =$  48,000

B  $5 \times 3000 = n$

$n =$  \_\_\_\_\_

C  $4 \times 9000 = n$

$n =$  \_\_\_\_\_

D  $9 \times 30,000 = n$

$n =$  \_\_\_\_\_

E  $8 \times 40,000 = n$

$n =$  \_\_\_\_\_

F  $7 \times 90,000 = n$

$n =$  \_\_\_\_\_

G  $6 \times 500,000 = n$

$n =$  \_\_\_\_\_

H  $3 \times 700,000 = n$

$n =$  \_\_\_\_\_

I  $8 \times 200,000 = n$

$n =$  \_\_\_\_\_

3. Use the table to help you solve these equations.

$10^2 = 100$	$10^4 = 10,000$
$10^3 = 1000$	$10^5 = 100,000$

A  $6 \times 10^3 =$  6000

D  $9 \times 10^4 =$  \_\_\_\_\_

G  $7 \times 10^3 =$  \_\_\_\_\_

B  $7 \times 10^2 =$  \_\_\_\_\_

E  $4 \times 10^2 =$  \_\_\_\_\_

H  $6 \times 10^4 =$  \_\_\_\_\_

C  $3 \times 10^5 =$  \_\_\_\_\_

F  $8 \times 10^5 =$  \_\_\_\_\_

I  $5 \times 10^5 =$  \_\_\_\_\_

4. Solve the equations.

A  $6 \times 4 \times 10^4 =$  240,000

E  $9 \times 2 \times 10^3 =$  \_\_\_\_\_

I  $7 \times 8 \times 10^2 =$  \_\_\_\_\_

B  $4 \times 7 \times 10^2 =$  \_\_\_\_\_

F  $6 \times 5 \times 10^5 =$  \_\_\_\_\_

J  $8 \times 6 \times 10^5 =$  \_\_\_\_\_

C  $7 \times 6 \times 10^3 =$  \_\_\_\_\_

G  $2 \times 8 \times 10^4 =$  \_\_\_\_\_

K  $3 \times 7 \times 10^3 =$  \_\_\_\_\_

D  $8 \times 5 \times 10^5 =$  \_\_\_\_\_

H  $5 \times 9 \times 10^3 =$  \_\_\_\_\_

L  $9 \times 3 \times 10^4 =$  \_\_\_\_\_

## ● Finding Missing Factors

1. One of the factors in each equation should end in zero.  
Can you write six different equations for each product?

**A**  $120 \times 120 = 120$

$\times = 120$

$\times = 120$

$\times = 120$

$\times = 120$

$\times = 120$

**B**  $180 \times = 180$

$\times = 180$

$\times = 180$

$\times = 180$

$\times = 180$

$\times = 180$

**C**  $240 \times = 240$

$\times = 240$

$\times = 240$

$\times = 240$

$\times = 240$

$\times = 240$

2. Solve the equations.

**A**  $4 \times n \times 10^3 = 24,000$

**B**  $n \times 8 \times 10^4 = 480,000$

**C**  $2 \times n \times 10^4 = 180,000$

$n = 6$

$n =$

$n =$

**D**  $n \times 8 \times 10^2 = 3200$

**E**  $6 \times n \times 10^2 = 1200$

**F**  $n \times 4 \times 10^3 = 20,000$

$n =$

$n =$

$n =$

**G**  $3 \times n \times 10^3 = 21,000$

**H**  $n \times 3 \times 10^5 = 2,100,000$

**I**  $5 \times n \times 10^5 = 3,000,000$

$n =$

$n =$

$n =$

3. When multiples of ten are expressed as  $10^2$ ,  $10^3$ ,  $10^4$ , and  $10^5$ , they are called **powers of ten**. Give the correct power of ten for each equation.

**A**  $5 \times 7 \times n = 3500$

**B**  $4 \times 8 \times n = 32,000$

**C**  $7 \times 6 \times n = 420,000$

$n = 10^2$

$n =$

$n =$

**D**  $5 \times 9 \times n = 45,000$

**E**  $8 \times 9 \times n = 7200$

**F**  $6 \times 4 \times n = 2,400,000$

$n =$

$n =$

$n =$



## ● Finding Special Quotients

1. Give the correct power of ten for each equation.

**A**  $3500 \div 5 = 7 \times n$

$n = 10^2$

**B**  $24,000 \div 6 = 4 \times n$

$n = \underline{\hspace{2cm}}$

**C**  $4200 \div 7 = 6 \times n$

$n = \underline{\hspace{2cm}}$

**D**  $28,000 \div 4 = 7 \times n$

$n = \underline{\hspace{2cm}}$

**E**  $180,000 \div 6 = 3 \times n$

$n = \underline{\hspace{2cm}}$

**F**  $27,000 \div 3 = 9 \times n$

$n = \underline{\hspace{2cm}}$

2. How many different equations can you write using the symbols on these cards?



EXAMPLES:

$$4 \times 6 \times 10^2 = 2400$$

or

$$2400 \div 8 = 3 \times 10^2$$

---

---

---

---

---



---

---

---

---

---

### ● Factors with Zeros

Put in some zeros so the equations are correct and different.

2.  $7\_\_\_\_\_\_ \times 4\_\_\_\_\_\_ = 2800$

$$7\_\times 4\_=2800$$

$$7\_\_\_\_\_\_ \times 4\_\_\_\_\_\_ = 2800$$

4.  $9\_\_\_\_\_\_ \times 7\_\_\_\_\_\_ = 6300$

$$9 \times 7 = 6300$$

$$9 \times 7 = 6300$$

6.  $8 \underline{\hspace{1cm}} \times 5 \underline{\hspace{1cm}} = 40,000$

$$8\_\_\_\_\_\_ \times 5\_\_\_\_\_\_ = 40,000$$

$$8\_\_\_\_\_\_ \times 5\_\_\_\_\_\_ = 40,000$$

8.  $5\_\_\_\_\_\_ \times 4\_\_\_\_\_\_ = 200,000$

$$5 \times 4 = 200,000$$

$$5 \times 4 = 200,000$$

10.  $5 \times 2 = 1$

$$5 \times 2 = 1$$

$$5 \times 2 = 1$$

$$5 \times 2 = 1$$

$$5 \times 2 = 1$$

## ● Finding Special Quotients

1. Fill in the missing numbers in each multiplication table.

**A**

×	100					
4	400	1200				20,000
6		1800		6000		
5	500	1500	3000		20,000	
7			4200		28,000	

**B**

×						
40	800		1200		3200	
70	1400	2800	2100	4200		
20	400					1000
60	1200	2400				

**C**

×						
50			20,000			
80		24,000		16,000		40,000
30	3000					
90					72,000	

2. Put in some zeros so the equations are different and correct.

**A**  $1400 \div 7$  \_\_\_\_\_ = 2 \_\_\_\_\_

**B**  $3200 \div 4$  \_\_\_\_\_ = 8 \_\_\_\_\_

$1400 \div 7$  \_\_\_\_\_ = 2 \_\_\_\_\_

$3200 \div 4$  \_\_\_\_\_ = 8 \_\_\_\_\_

$1400 \div 7$  \_\_\_\_\_ = 2 \_\_\_\_\_

$3200 \div 4$  \_\_\_\_\_ = 8 \_\_\_\_\_

**C**  $4000 \div 5$  \_\_\_\_\_ = 8 \_\_\_\_\_

**D**  $7200 \div 8$  \_\_\_\_\_ = 9 \_\_\_\_\_

$4000 \div 5$  \_\_\_\_\_ = 8 \_\_\_\_\_

$7200 \div 8$  \_\_\_\_\_ = 9 \_\_\_\_\_

$4000 \div 5$  \_\_\_\_\_ = 8 \_\_\_\_\_

$7200 \div 8$  \_\_\_\_\_ = 9 \_\_\_\_\_

**E**  $45,000 \div 9$  \_\_\_\_\_ = 5 \_\_\_\_\_

**F**  $30,000 \div 5$  \_\_\_\_\_ = 6 \_\_\_\_\_

$45,000 \div 9$  \_\_\_\_\_ = 5 \_\_\_\_\_

$30,000 \div 5$  \_\_\_\_\_ = 6 \_\_\_\_\_

$45,000 \div 9$  \_\_\_\_\_ = 5 \_\_\_\_\_

$30,000 \div 5$  \_\_\_\_\_ = 6 \_\_\_\_\_

$45,000 \div 9$  \_\_\_\_\_ = 5 \_\_\_\_\_

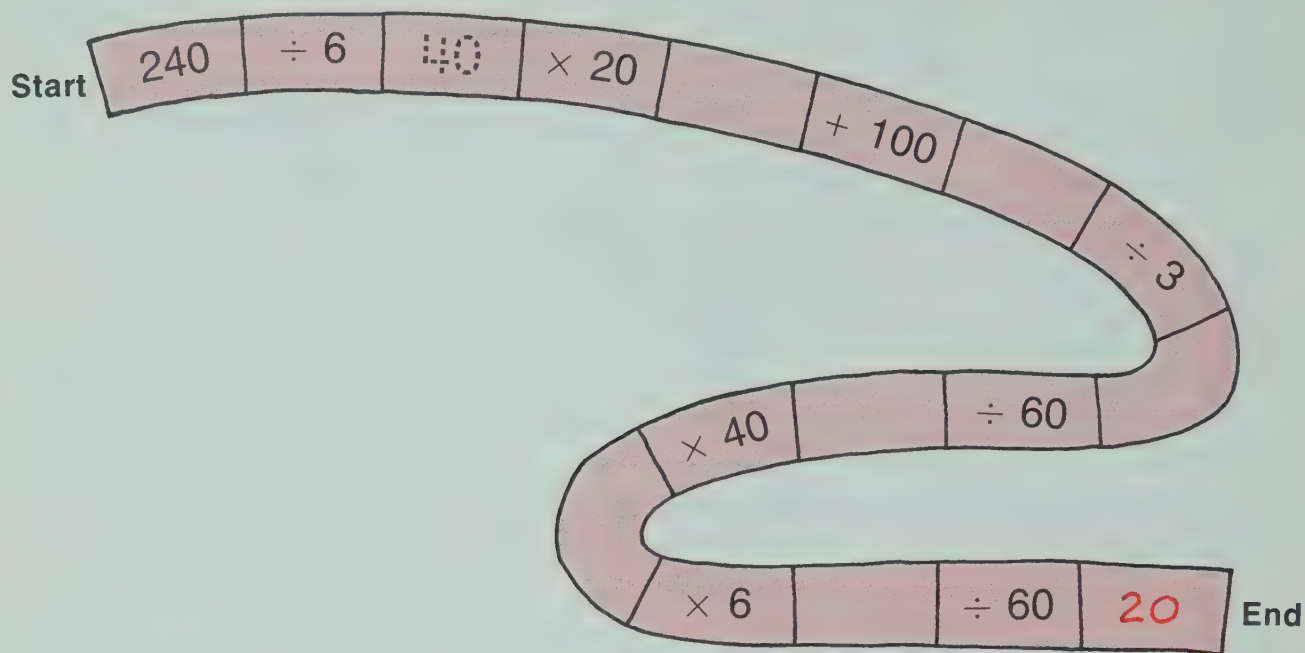
$30,000 \div 5$  \_\_\_\_\_ = 6 \_\_\_\_\_



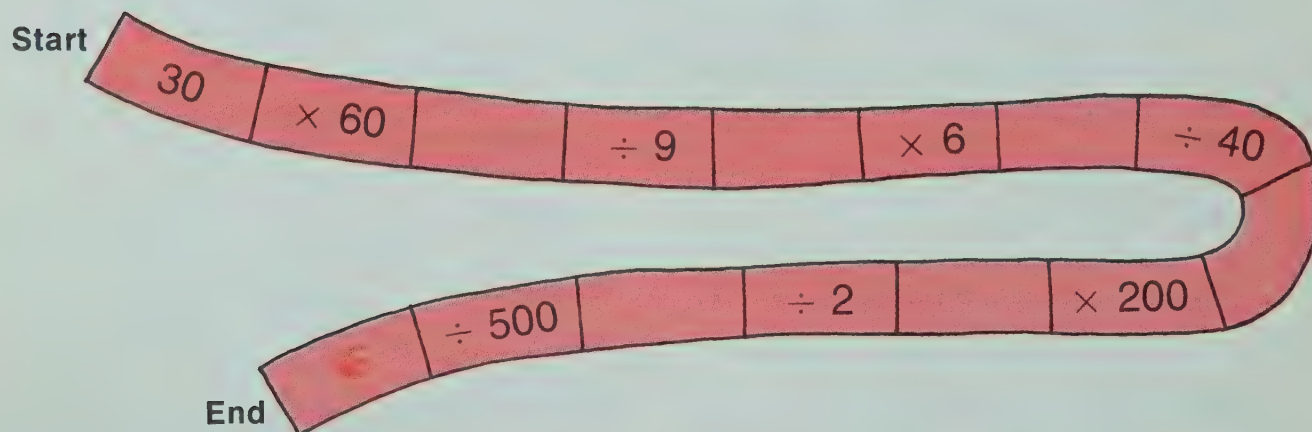
## ● Finding Special Products and Quotients

Fill in the missing numbers. If your work is correct you should end with the number shown in red.

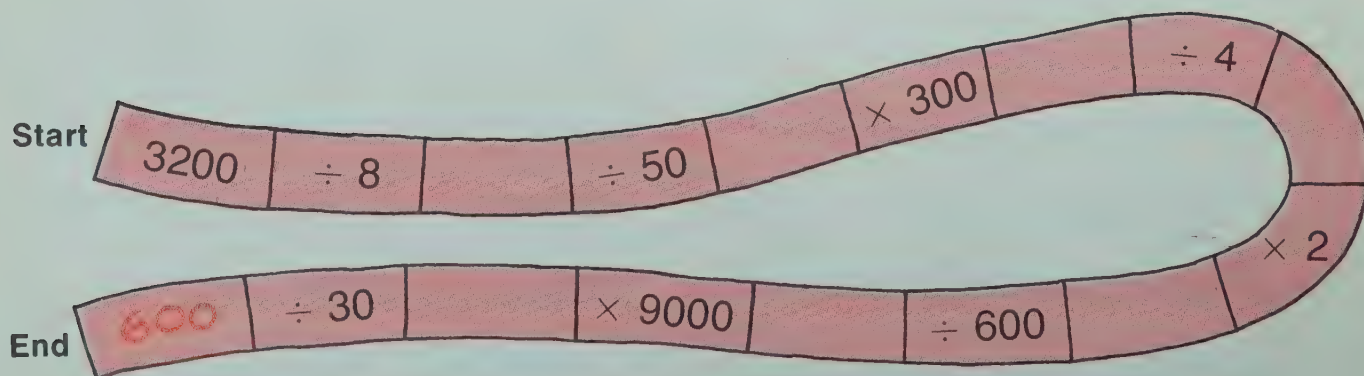
1.



2.



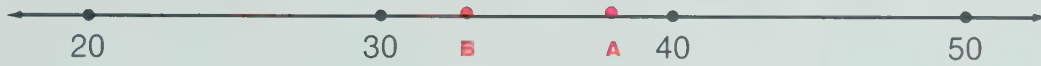
3.



On each number line, estimate the position of the numbers with dots as in the examples for **A** and **B**. Put the letter under each dot.

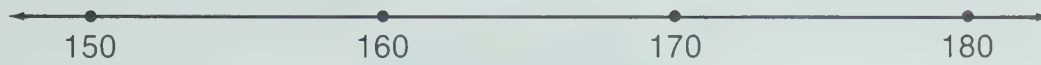
1.

**A** 38      **B** 33      **C** 42      **D** 29      **E** 35



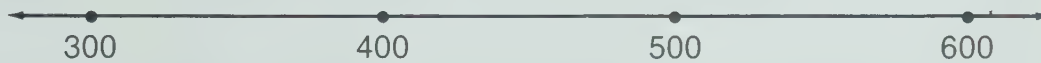
2.

**A** 174      **B** 169      **C** 165      **D** 162      **E** 157



3.

**A** 450      **B** 525      **C** 375      **D** 467      **E** 592



4.

**A** 812      **B** 783      **C** 937      **D** 869      **E** 744



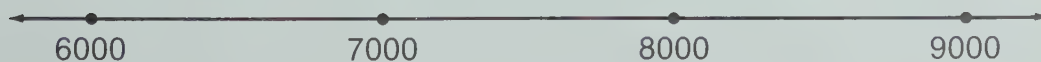
5.

**A** 1850      **B** 1925      **C** 1775      **D** 1733      **E** 1989



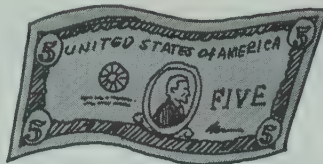
6.

**A** 8512      **B** 7248      **C** 6124      **D** 7896      **E** 6698



## ● Estimating Totals

1. You have this much money. Use estimation to decide which of these totals you'll be able to pay. Write "yes" or "no" on the paper.



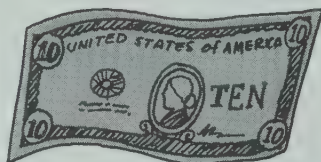
**A** \$ 1.98  
1.89  
1.88  
total: \_\_\_\_\_

**B** \$.99  
.98  
.95  
.89  
.99  
total: \_\_\_\_\_

**C** \$ 1.12  
.95  
1.10  
.98  
total: \_\_\_\_\_

**D** \$ 2.95  
.89  
1.98  
total: \_\_\_\_\_

2. Which of these will you be able to pay with the \$10 bill?



**A** \$ 2.98  
3.95  
1.99  
.96  
total: \_\_\_\_\_

**B** \$ 3.79  
4.88  
2.49  
1.10  
total: \_\_\_\_\_

**C** \$ 1.95  
1.89  
1.99  
1.88  
1.98  
total: \_\_\_\_\_

**D** \$ .89  
4.98  
1.00  
2.95  
.95  
total: \_\_\_\_\_

3. Which of these will you be able to pay with the \$20 bill?



**A** \$ 4.95  
4.95  
4.95  
4.95  
total: \_\_\_\_\_

**B** \$ 5.98  
4.98  
5.98  
4.98  
total: \_\_\_\_\_

**C** \$ 7.00  
3.95  
2.98  
6.95  
total: \_\_\_\_\_

**D** \$ 3.79  
2.89  
2.95  
2.99  
2.98  
2.99  
total: \_\_\_\_\_



## ● Estimating Products

1. Fill in the estimation tables.

**A**

×	9 9	1 9 8	3 9 5	6 1 2	9 9 8	1 0 2 1
3	3 0 0					
4		8 0 0			4 0 0 0	
6	6 0 0		2 4 0 0			
8		1 6 0 0		4 8 0 0		

**B**

×	3 1	3 9	2 2	4 7	7 1	8 9
2 8			6 0 0			
1 9	6 0 0					
4 2		1 6 0 0				
5 8				3 0 0 0		

**C**

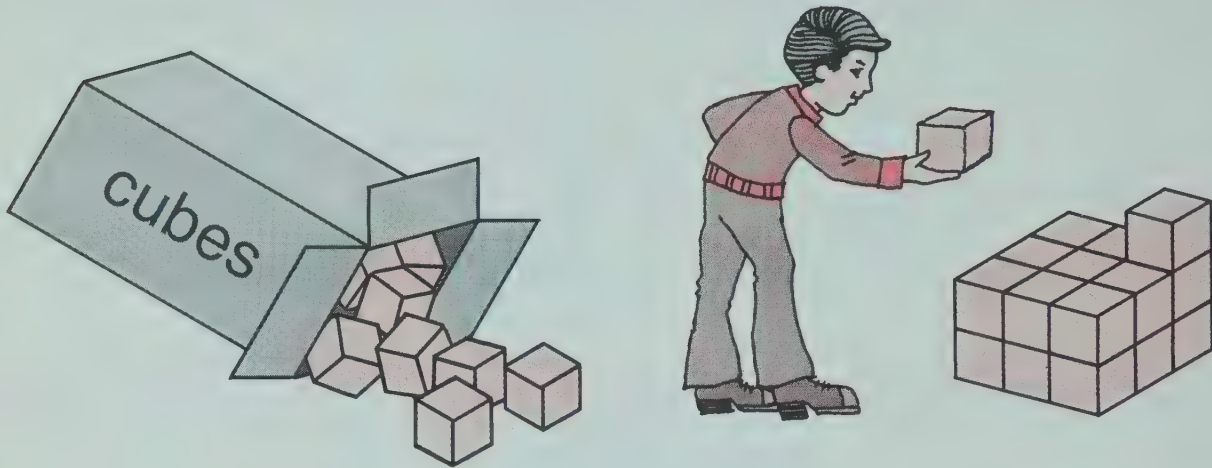
×	9 8	3 1 2	1 9 5	4 8 7	2 0 8	6 9 9
3 2				1 5,0 0 0		
1 8		6 0 0 0				
4 1		1 2,0 0 0				
6 9	7 0 0 0					

2. Put in some numbers of your own so the estimates in the table are “close.” Then complete the tables.

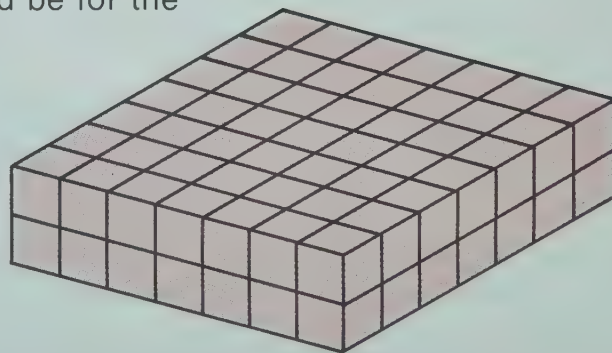
×						
2		1 0 0		1 2 0		6 0 0
7	1 4 0		2 8 0	4 2 0		
2 9		1 5 0 0			3 0 0 0	
5 2	1 0 0 0		2 0 0 0		5 0 0 0	1 5,0 0 0

## ● Estimating Quotients

1. Estimate about how many cubes tall this “building” would be for the different numbers of cubes.



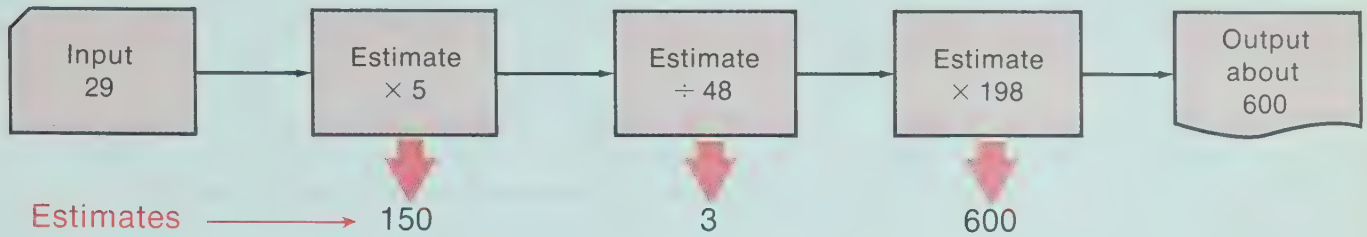
- A 178 cubes. About how tall? \_\_\_\_\_
- B 631 cubes. About how tall? \_\_\_\_\_
- C 358 cubes. About how tall? \_\_\_\_\_
- D 542 cubes. About how tall? \_\_\_\_\_
2. Estimate how tall this “building” would be for the different numbers of cubes.



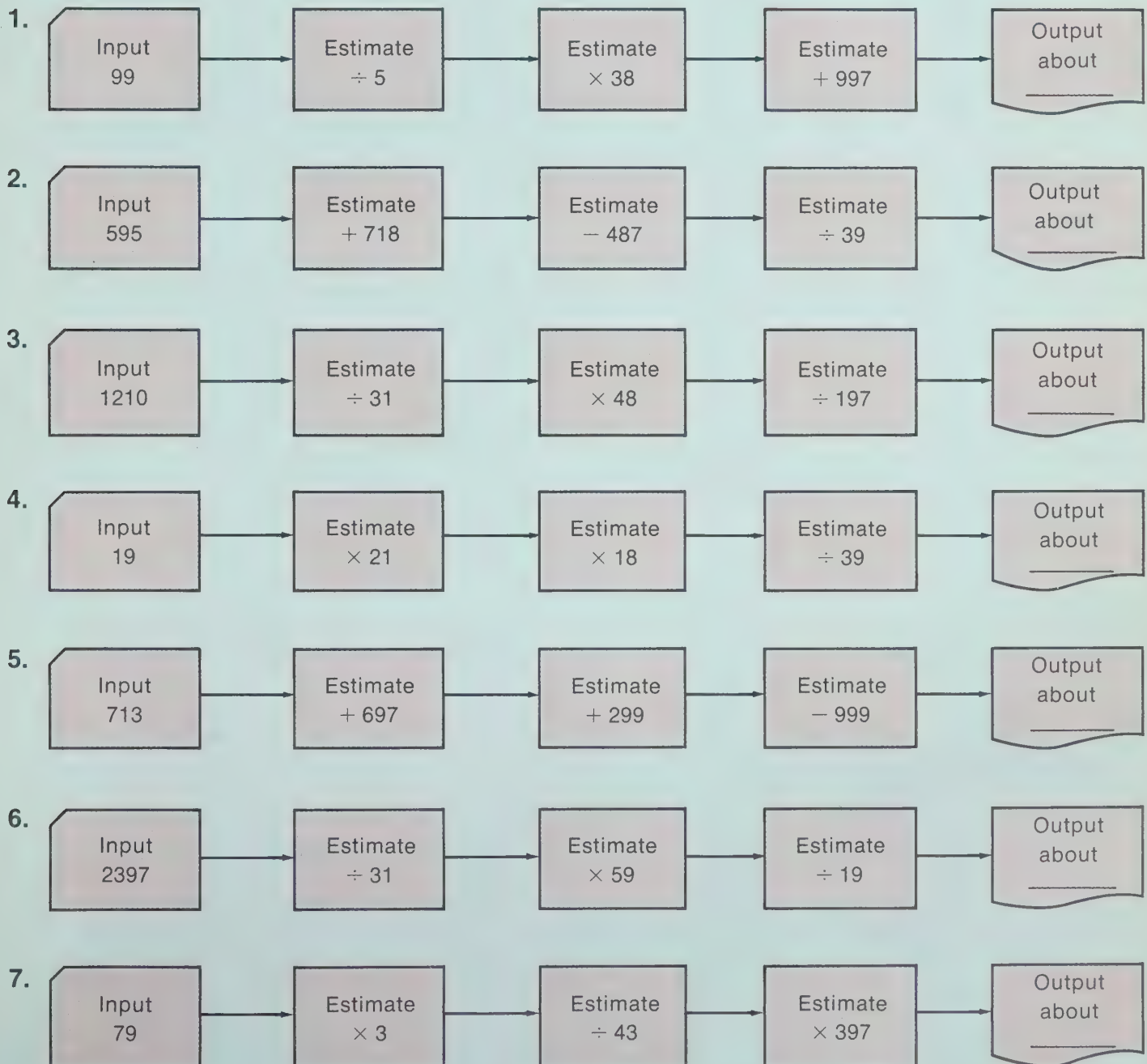
- A 298 cubes. About how tall? \_\_\_\_\_
- B 410 cubes. About how tall? \_\_\_\_\_
- C 1498 cubes. About how tall? \_\_\_\_\_
- D 3018 cubes. About how tall? \_\_\_\_\_

## ● Estimating

Study the flow chart examples using estimates.



Find each output number using estimates.

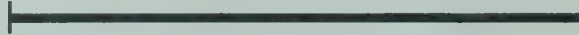




## ● Estimation for Fun

1. 

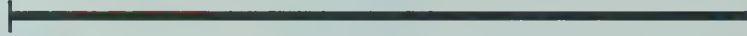
If this length is  
79 units,



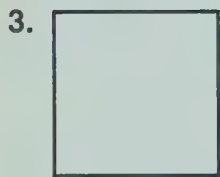
then this length is  
about \_\_\_\_\_ units.

2. 

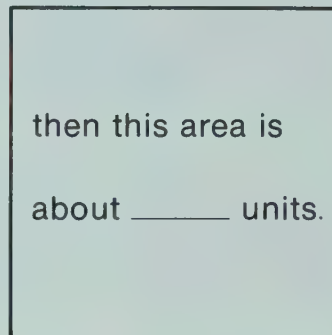
If this length is  
19 units,



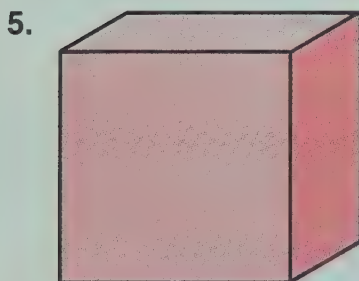
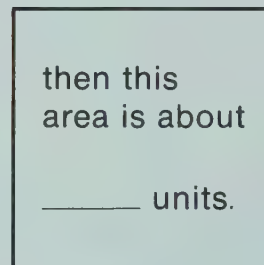
then this length is  
about \_\_\_\_\_ units.



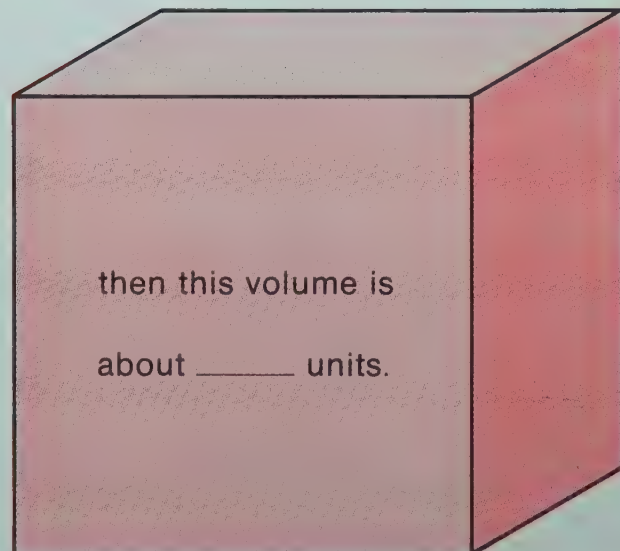
If this area is  
49 units,



If this area is  
21 units,



If this volume is  
29 units,



1. Grade Lisa's paper.

1.	2.	3.	4.	5. <i>LISA</i>
$\begin{array}{r} 38 \\ \times 4 \\ \hline 152 \end{array}$	$\begin{array}{r} 57 \\ \times 2 \\ \hline 114 \end{array}$	$\begin{array}{r} 46 \\ \times 8 \\ \hline 366 \end{array}$	$\begin{array}{r} 92 \\ \times 7 \\ \hline 644 \end{array}$	$\begin{array}{r} 28 \\ \times 6 \\ \hline 166 \end{array}$
6.	7.	8.	9.	10.
$\begin{array}{r} 49 \\ \times 4 \\ \hline 196 \end{array}$	$\begin{array}{r} 83 \\ \times 6 \\ \hline 478 \end{array}$	$\begin{array}{r} 85 \\ \times 4 \\ \hline 340 \end{array}$	$\begin{array}{r} 64 \\ \times 8 \\ \hline 492 \end{array}$	$\begin{array}{r} 18 \\ \times 6 \\ \hline 106 \end{array}$

2. Each mistake Lisa made was for the same reason. Can you tell Lisa what she is doing wrong?

---



---



---

3. Grade Don's paper.

1.	2.	3.	4.	5. <i>Don</i>
$\begin{array}{r} 62 \\ \times 3 \\ \hline 186 \end{array}$	$\begin{array}{r} 73 \\ \times 2 \\ \hline 146 \end{array}$	$\begin{array}{r} 56 \\ \times 4 \\ \hline 204 \end{array}$	$\begin{array}{r} 94 \\ \times 2 \\ \hline 188 \end{array}$	$\begin{array}{r} 47 \\ \times 3 \\ \hline 121 \end{array}$
6.	7.	8.	9.	10.
$\begin{array}{r} 82 \\ \times 2 \\ \hline 164 \end{array}$	$\begin{array}{r} 43 \\ \times 3 \\ \hline 129 \end{array}$	$\begin{array}{r} 65 \\ \times 7 \\ \hline 425 \end{array}$	$\begin{array}{r} 42 \\ \times 3 \\ \hline 126 \end{array}$	$\begin{array}{r} 74 \\ \times 6 \\ \hline 424 \end{array}$

4. Can you tell Don what he is doing wrong?

---



---



---

## ● Multiplying with a 3-Digit Factor

1. First estimate each product. Then find the product. Find the difference between your estimate and the correct product.

**A**     $\begin{array}{r} 376 \\ \times 4 \\ \hline 1600 \\ \text{estimate} \\ 1504 \\ \text{product} \\ 96 \\ \text{difference} \end{array}$

**B**     $\begin{array}{r} 483 \\ \times 6 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**C**     $\begin{array}{r} 725 \\ \times 3 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**D**     $\begin{array}{r} 321 \\ \times 9 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**E**     $\begin{array}{r} 489 \\ \times 5 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**F**     $\begin{array}{r} 7264 \\ \times 5 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**G**     $\begin{array}{r} 5438 \\ \times 3 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**H**     $\begin{array}{r} 6073 \\ \times 6 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**I**     $\begin{array}{r} 9802 \\ \times 4 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

**J**     $\begin{array}{r} 3743 \\ \times 7 \\ \hline \\ \text{estimate} \\ \\ \text{product} \\ \\ \text{difference} \end{array}$

2. Use addition only to complete the multiplication table. (No multiplying allowed.) Hint: 5 sixty-eights is the same as the sum of 2 sixty-eights and 3 sixty-eights.

×	68	237	435	6824	5196	7843
2	136	474	870	13,648	10,392	15,686
3	204	711	1305	20,472	15,588	23,529
5						
7						
8						
9						
17						

3. Find the products below. Check your answers in the table.

**A**     $\begin{array}{r} 68 \\ \times 7 \\ \hline \end{array}$

**B**     $\begin{array}{r} 237 \\ \times 9 \\ \hline \end{array}$

**C**     $\begin{array}{r} 435 \\ \times 9 \\ \hline \end{array}$

**D**     $\begin{array}{r} 6824 \\ \times 8 \\ \hline \end{array}$

**E**     $\begin{array}{r} 5196 \\ \times 5 \\ \hline \end{array}$

**F**     $\begin{array}{r} 7843 \\ \times 9 \\ \hline \end{array}$



## Finding Missing Digits

1. Find the missing digit.

$$\begin{array}{r} \text{A} \quad 37 \\ \times \quad \square \\ \hline 148 \end{array}$$

$$\begin{array}{r} \text{B} \quad 52 \\ \times \quad \square \\ \hline 364 \end{array}$$

$$\begin{array}{r} \text{C} \quad 864 \\ \times \quad \square \\ \hline 4320 \end{array}$$

$$\begin{array}{r} \text{D} \quad 352 \\ \times \quad \square \\ \hline 2816 \end{array}$$

$$\begin{array}{r} \text{E} \quad 349 \\ \times \quad \square \\ \hline 1047 \end{array}$$

$$\begin{array}{r} \text{F} \quad 7283 \\ \times \quad \square \\ \hline 65,547 \end{array}$$

$$\begin{array}{r} \text{G} \quad 2465 \\ \times \quad \square \\ \hline 9860 \end{array}$$

$$\begin{array}{r} \text{H} \quad 5374 \\ \times \quad \square \\ \hline 26,870 \end{array}$$

$$\begin{array}{r} \text{I} \quad 1884 \\ \times \quad \square \\ \hline 3768 \end{array}$$

$$\begin{array}{r} \text{J} \quad 7982 \\ \times \quad \square \\ \hline 47,892 \end{array}$$

2. Find the missing digits.

$$\begin{array}{r} \text{A} \quad \square 3 \\ \times 7 \\ \hline 301 \end{array}$$

$$\begin{array}{r} \text{B} \quad 6 \square \\ \times 5 \\ \hline 345 \end{array}$$

$$\begin{array}{r} \text{C} \quad 53 \square \\ \times 3 \\ \hline 1602 \end{array}$$

$$\begin{array}{r} \text{D} \quad 3 \square 6 \\ \times 9 \\ \hline 3474 \end{array}$$

$$\begin{array}{r} \text{E} \quad \square 49 \\ \times 6 \\ \hline 4494 \end{array}$$

$$\begin{array}{r} \text{F} \quad 24 \square 3 \\ \times 8 \\ \hline 19,704 \end{array}$$

$$\begin{array}{r} \text{G} \quad 7 \square 81 \\ \times 4 \\ \hline 30,324 \end{array}$$

$$\begin{array}{r} \text{H} \quad 6 \square 3 \\ \times 2 \\ \hline 9246 \end{array}$$

$$\begin{array}{r} \text{I} \quad 7 \square 6 \\ \times 4 \\ \hline 31,468 \end{array}$$

$$\begin{array}{r} \text{J} \quad \square 3 \square 4 \\ \times 5 \\ \hline 26,620 \end{array}$$

3. Find the missing digits.

$$\begin{array}{r} \text{A} \quad 384 \\ \times \quad \square \\ \hline 04 \end{array}$$

$$\begin{array}{r} \text{B} \quad \square 479 \\ \times 3 \\ \hline 4 \end{array}$$

$$\begin{array}{r} \text{C} \quad 35 \\ \times 2 \square \\ \hline 245 \\ 0 \\ \hline 45 \end{array}$$

$$\begin{array}{r} \text{D} \quad \square 6 \\ \times \square 3 \\ \hline 138 \\ 2760 \\ \hline 2898 \end{array}$$

$$\begin{array}{r} \text{E} \quad 7 \square \\ \times \square 6 \\ \hline 444 \\ 3700 \\ \hline 4144 \end{array}$$

$$\begin{array}{r} \text{F} \quad \square 28 \\ \times 3 \\ \hline 1640 \\ 9840 \\ \hline 11,480 \end{array}$$

$$\begin{array}{r} \text{G} \quad 4 \square 7 \\ \times 6 \\ \hline 2502 \\ 20850 \\ \hline 23,352 \end{array}$$

$$\begin{array}{r} \text{H} \quad \square 5 \square \\ \times 3 \\ \hline 1956 \\ 52160 \\ \hline 54,116 \end{array}$$

$$\begin{array}{r} \text{I} \quad \square 3 \square \\ \times 1 \square \\ \hline 2133 \\ 2370 \\ \hline 4503 \end{array}$$

$$\begin{array}{r} \text{J} \quad \square 89 \\ \times \square \\ \hline 1467 \\ 14670 \\ \hline 16,137 \end{array}$$

## ● Finding Products – 2 and 3-Digit Factors

1. Complete rows **A**, **B**, and **C** of the table using only addition.  
Put your own factors in rows **D**, **E**, **F**, and **G** so  
you can complete the table using addition.

Remember, no multiplying allowed.

	×	36	58	73	346	582	724
	30	1080	1740	2190	10,380	17,460	21,720
	50	1800	2900	3650	17,300	29,100	36,200
	80	2880	4640	5840	27,680	46,560	57,920
	4	144	232	292	1384	2328	2896
	7	252	406	511	2422	4074	5068
	9	324	522	657	3114	5238	6516
<b>A</b>	54						
<b>B</b>	39						
<b>C</b>	87						
<b>D</b>							
<b>E</b>							
<b>F</b>							
<b>G</b>							

2. Find these products and check your answers in the table.

**A**       $\begin{array}{r} 58 \\ \times 39 \\ \hline \end{array}$

**B**       $\begin{array}{r} 73 \\ \times 87 \\ \hline \end{array}$

**C**       $\begin{array}{r} 346 \\ \times 54 \\ \hline \end{array}$

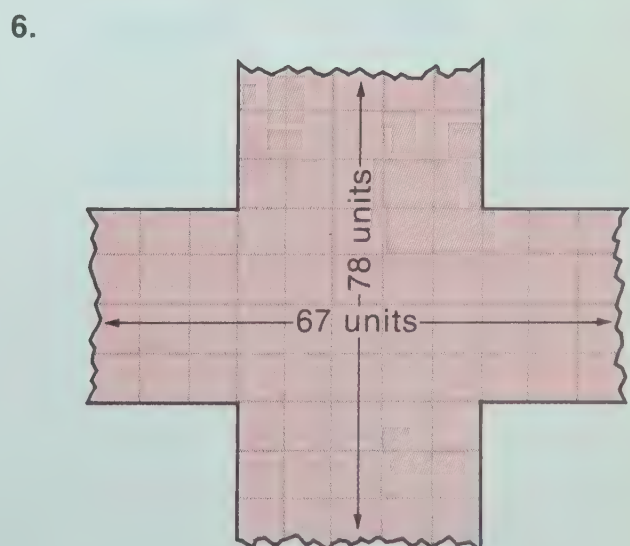
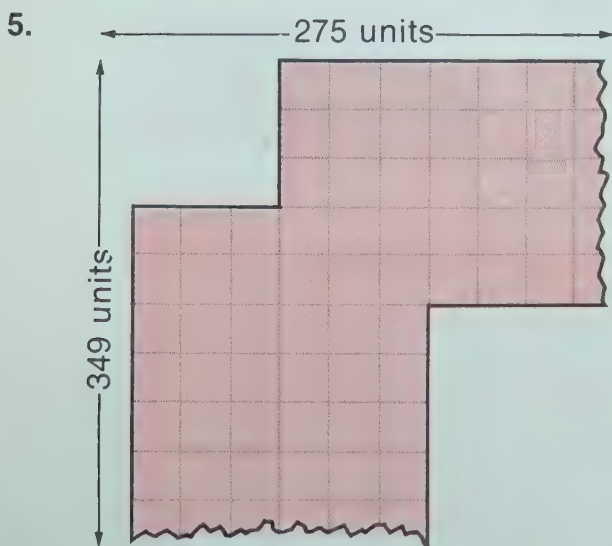
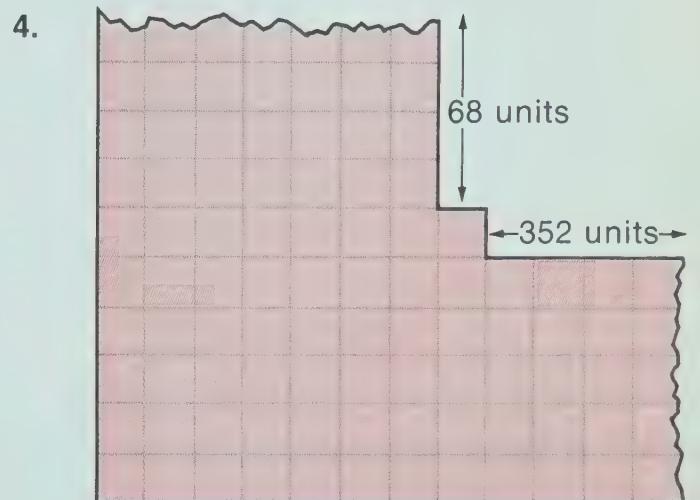
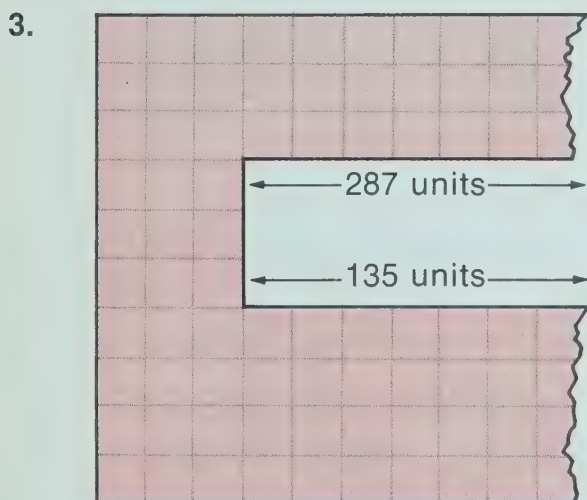
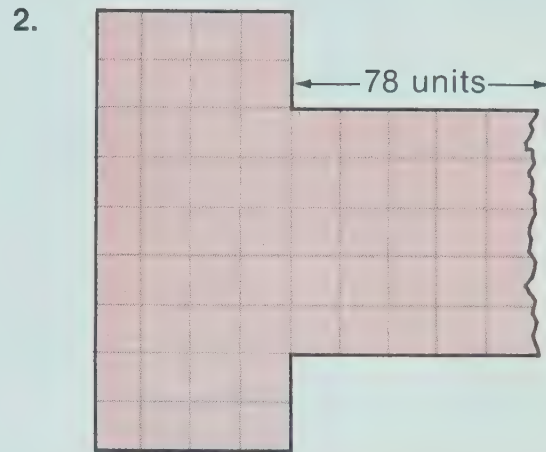
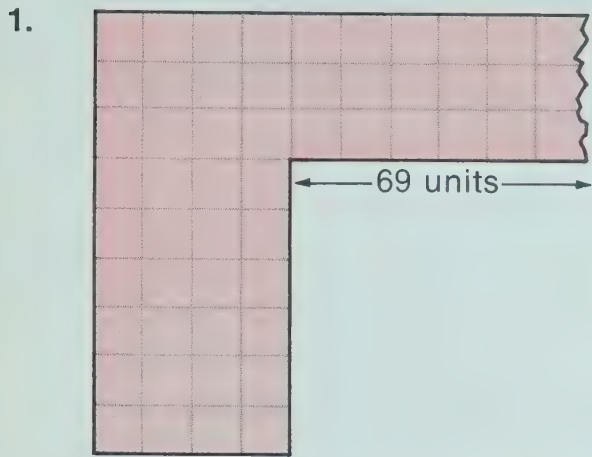
**D**       $\begin{array}{r} 582 \\ \times 87 \\ \hline \end{array}$

**E**       $\begin{array}{r} 724 \\ \times 39 \\ \hline \end{array}$

3. Check some of your own rows in the table by multiplying.

## ● Multiplication and Measurement

Find the area of each figure.





## Solving Problems

1. In each problem, put in numbers of your own that make sense.  
Then solve your problem.

**A** If a car travels \_\_\_\_\_ kilometers  
each hour, how far will

it go in \_\_\_\_\_ hours?

**B** One summer Patty read \_\_\_\_\_ books.  
The average length of the book was

about \_\_\_\_\_ pages. How many pages  
did she read?

**C** The average length of a math

lesson is \_\_\_\_\_ minutes.

Judy's class had \_\_\_\_\_ lessons in  
November. How many minutes of  
math did they have in November?

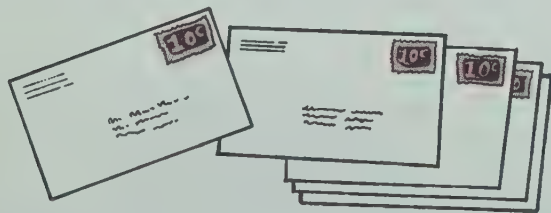
**D** Randy's favorite sports car sells for

about \_\_\_\_\_ dollars. The dealer

said he sold \_\_\_\_\_ of them last year.  
How many dollars is this in all?

2. Write and solve a multiplication problem for each picture.

**A**



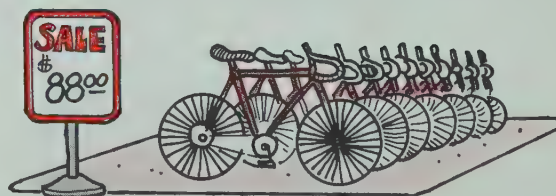
---

---

---

---

**B**



---

---

---

---

## ● Larger Products

- Make up your own multiplication problems so that each has a digit and there are no extra digits.  
Have a classmate check your work.

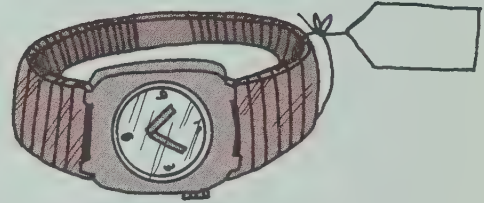
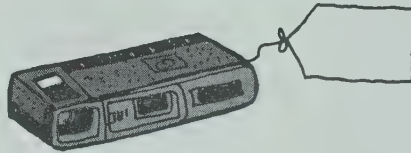
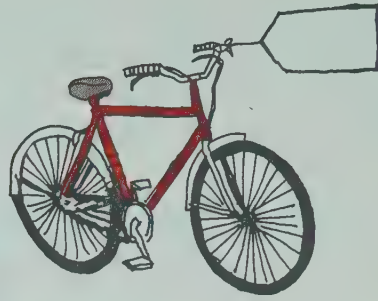
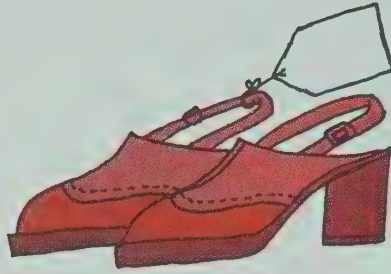
<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>
$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$
<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>	<b>K</b>	
$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	$\begin{array}{r} \times \\ \hline \end{array}$	

- Make your problems as you did above only be sure the given digit is correct.

<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>
$\begin{array}{r} \times \\ \hline 2 \end{array}$	$\begin{array}{r} \times \\ \hline 6 \end{array}$	$\begin{array}{r} \times \\ \hline 8 \end{array}$	$\begin{array}{r} \times \\ \hline 8 \end{array}$	$\begin{array}{r} \times \\ \hline 3 \end{array}$	$\begin{array}{r} \times \\ \hline 8 \end{array}$
<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>	<b>K</b>	
$\begin{array}{r} \times \\ \hline 4 \end{array}$	$\begin{array}{r} \times \\ \hline 0 \end{array}$	$\begin{array}{r} \times \\ \hline 4 \end{array}$	$\begin{array}{r} \times \\ \hline 9 \end{array}$	$\begin{array}{r} \times \\ \hline 3 \end{array}$	

## ●Solving Problems

Put a price on each item that you think is about "right." Then write and solve a problem about these items that uses the operation shown.



---

---

---

---

---

---



---

---

---

---

---

---



---

---

---

---

---

---



---

---

---

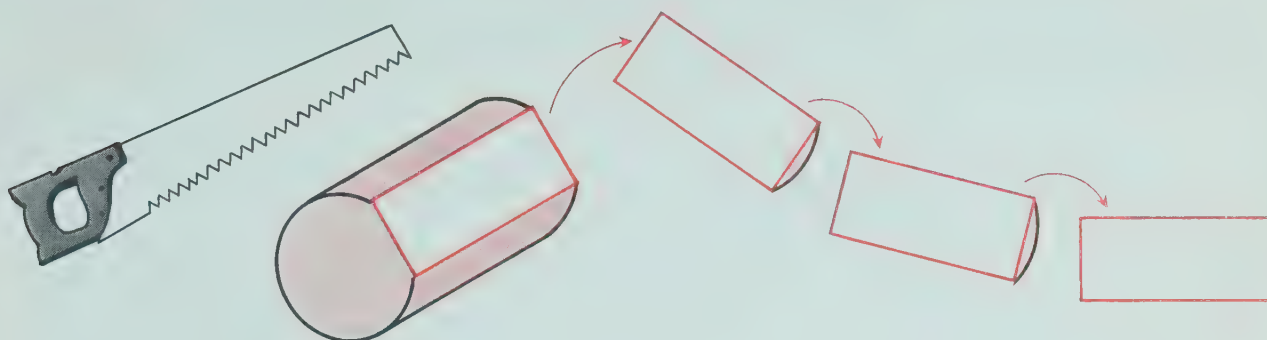
---

---

---

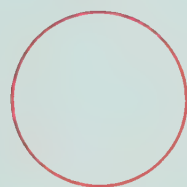
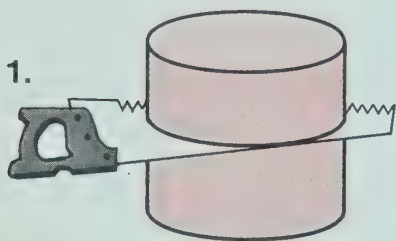


The figure below shows a cross section. Think about cutting the figure.



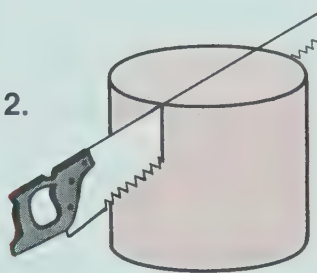
Draw a picture of the cross section for each cut shown below.  
Part 1 is an example.

1.



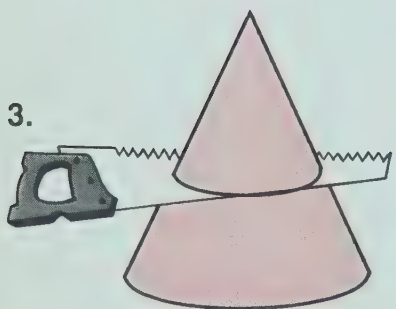
cross section

2.



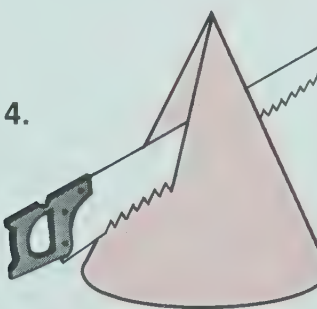
cross section

3.



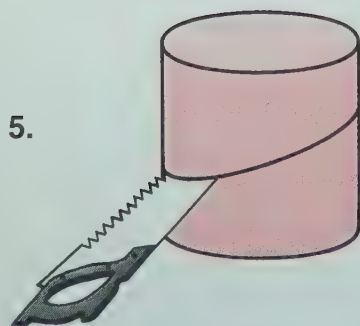
cross section

4.



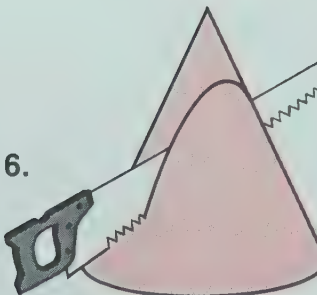
cross section

5.



cross section

6.



cross section

## ● Sketching Circles

When you **sketch** figures, you use **only** your pencil. Can you find a way to mark points on graph paper to help you **sketch** the circles called for below? The red dots are the centers. The black dots are to help you get started.

1.

radius  
3 units

2.

radius  
6 units

3.

radius  
5 units

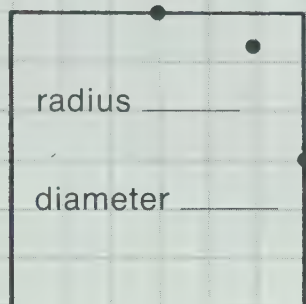
4.

radius  
7 units

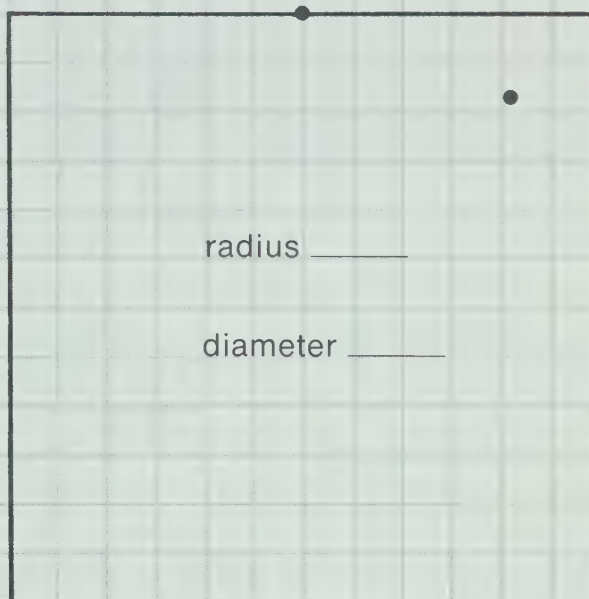
## Circles and Tangents

Sketch a circle inside each square so the sides of the square are tangent to the circle. Your work on page 56 should help you.  
Give the radius and diameter of each circle.

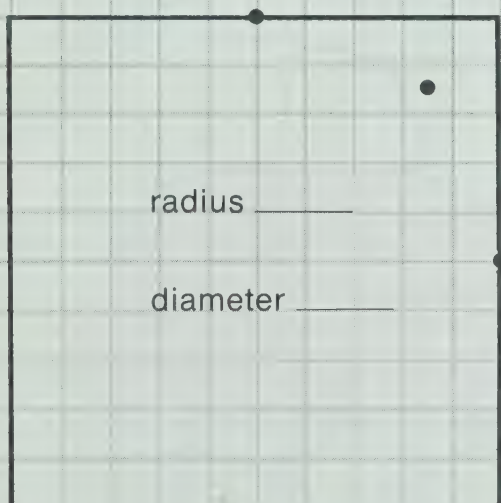
1.



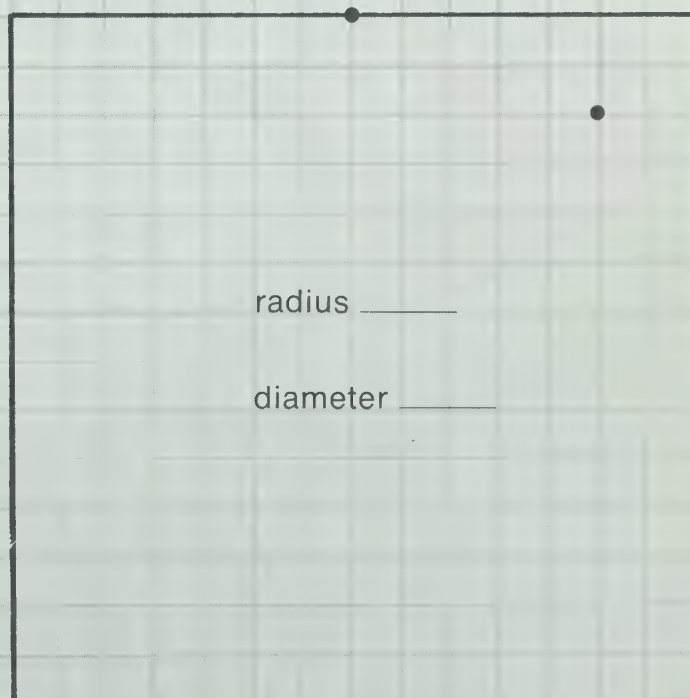
2.



3.



4.

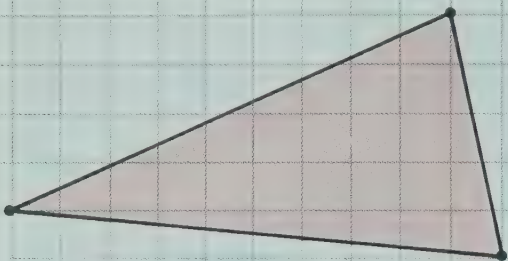




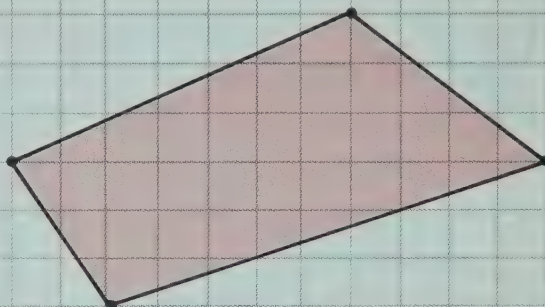
## ● Drawing Congruent Figures

Draw a figure so that it is congruent to the shaded figure.

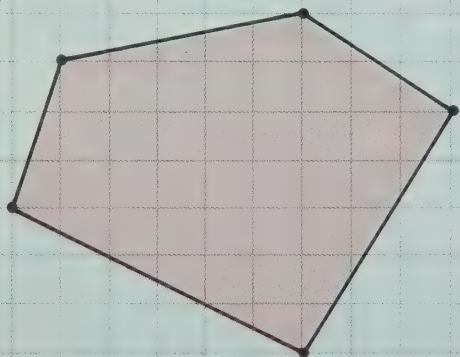
1.



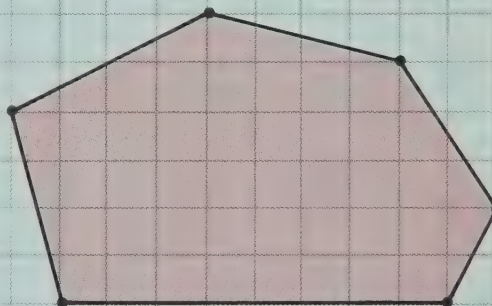
2.



3.

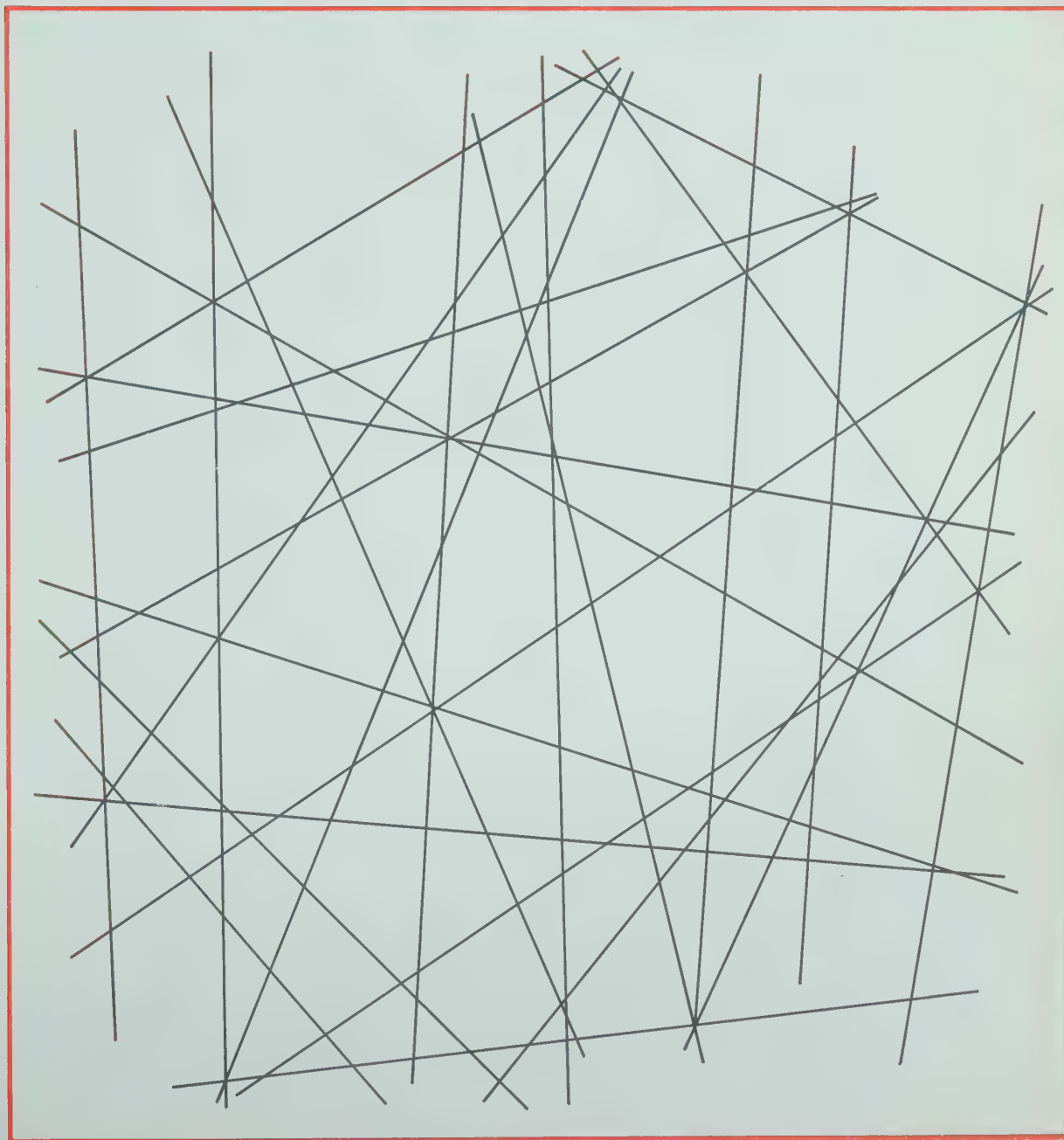
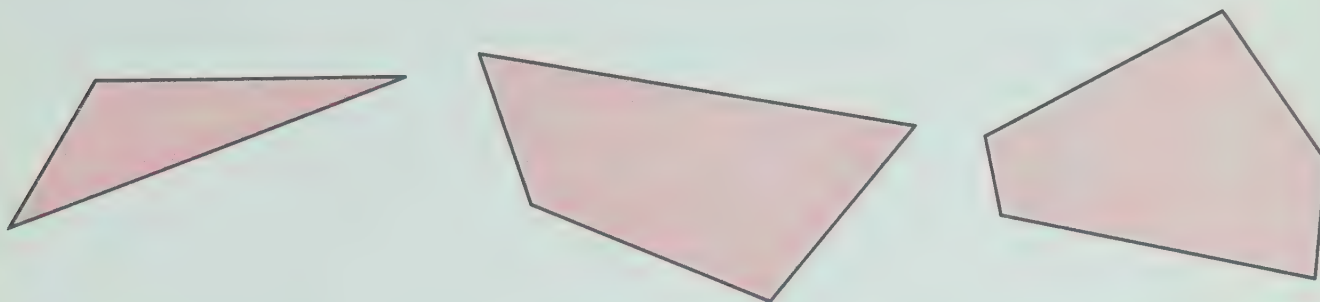


4.



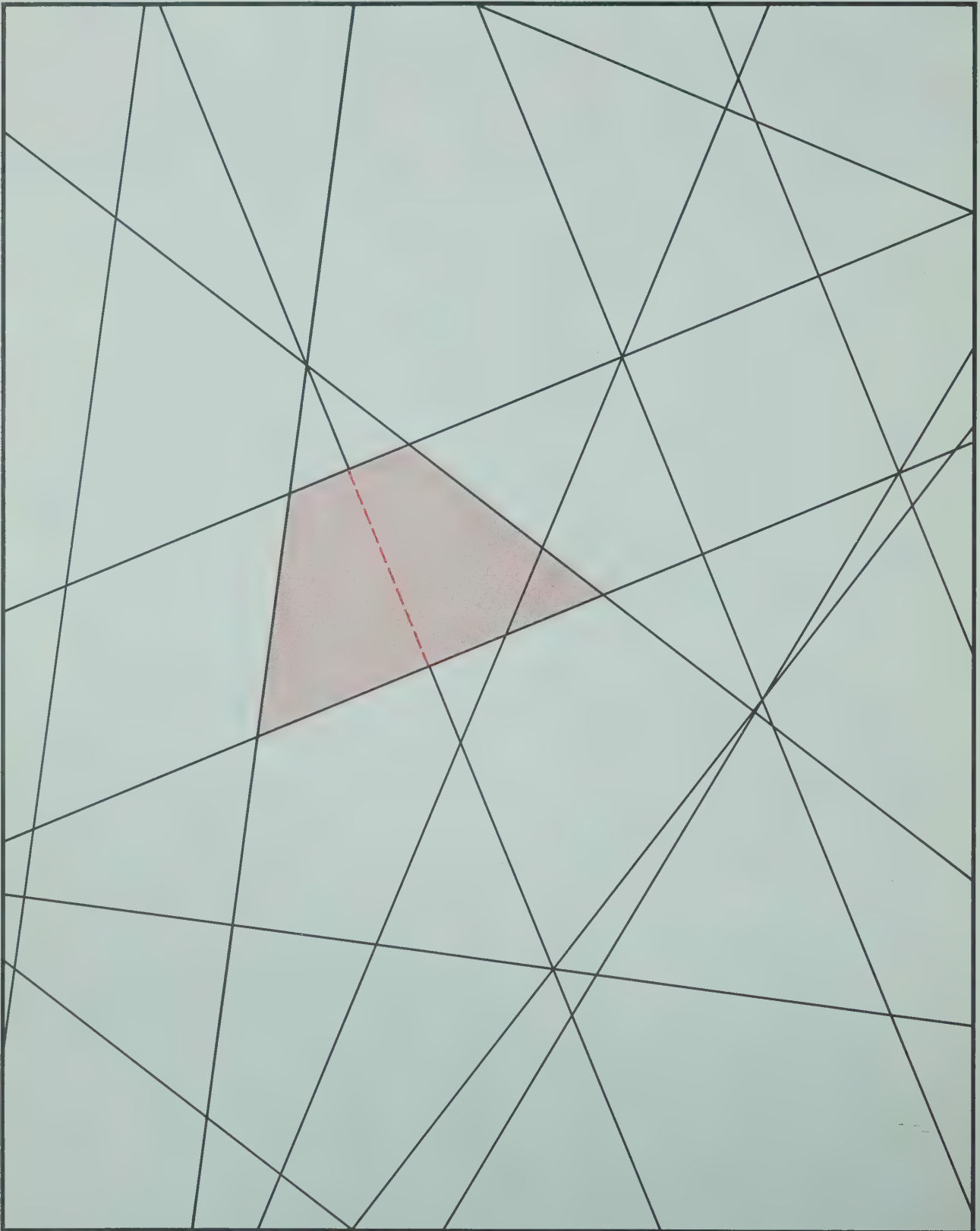
## ● Congruent Figures

There are two figures "hidden" in the box below that are each congruent to the colored figures. How many can you find and color?



## ● Symmetrical Figures

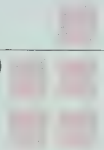



There are at least 5 symmetrical figures hidden below. See how many you can find. Color them and draw a line of symmetry. One is shown as an example.






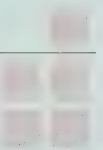
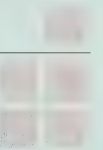
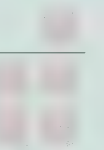
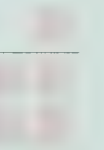
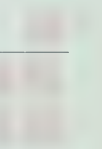
For each divisor make up as many problems as you can that have different remainders. You may not be able to complete all rows.

### 1. Dividing by 4







4)  4)  4)  4)  4)  4) 

All different →


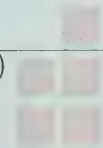
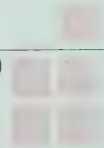
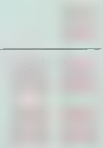
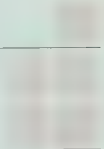
### 2. Dividing by 5

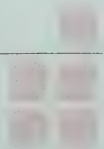
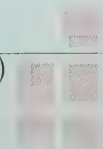
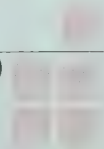


5)  5)  5)  5)  5)  5) 

### 3. Dividing by 6

6)  6)  6)  6)  6)  6) 

### 4. Dividing by 8

8)  8)  8)  8)  8) 

8)  8)  8)  8)  8) 

## ● Estimating Quotients

1. Study each problem. First write your estimate of the quotient in the red box. Then find the correct quotient.

**A** Estimate

$$4 \overline{)215}$$

**B** Estimate

$$5 \overline{)325}$$

**C** Estimate

$$8 \overline{)370}$$

**D** Estimate

$$6 \overline{)424}$$

**E** Estimate

$$7 \overline{)185}$$

**F** Estimate

$$3 \overline{)164}$$

**G** Estimate

$$5 \overline{)326}$$

**H** Estimate

$$6 \overline{)176}$$

**I** Estimate

$$7 \overline{)528}$$

**J** Estimate

$$8 \overline{)476}$$

**K** Estimate

$$4 \overline{)234}$$

**L** Estimate

$$9 \overline{)375}$$

2. Give the remainder for each problem, without finding the quotient.

**A**  $2 \overline{)376}$

**B**  $2 \overline{)587}$

**C**  $5 \overline{)287}$

**D**  $5 \overline{)615}$

**E**  $5 \overline{)964}$

**F**  $5 \overline{)339}$

R = \_\_\_\_\_

R = \_\_\_\_\_

R = \_\_\_\_\_

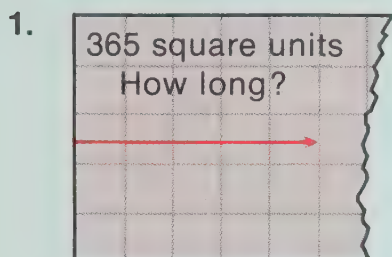
R = \_\_\_\_\_

R = \_\_\_\_\_

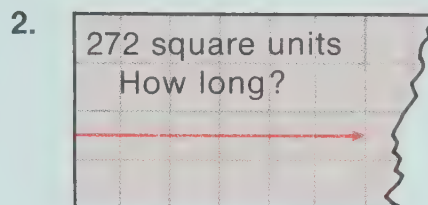
R = \_\_\_\_\_

## ● Using Estimation In Division

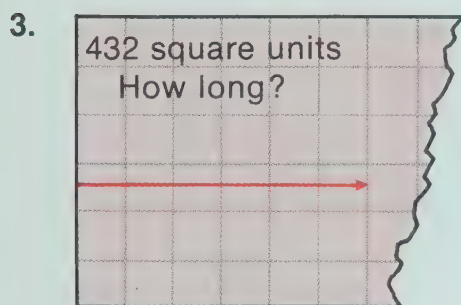
First estimate how long the rectangle would be.  
Then use division to find out.



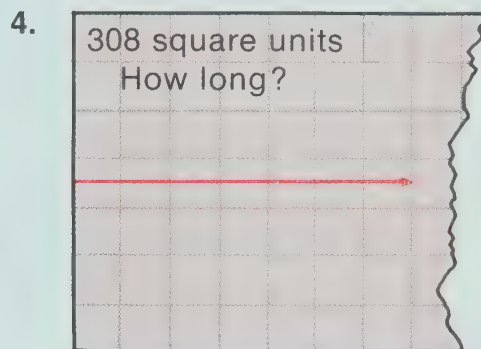
Estimate \_\_\_\_\_ Actual \_\_\_\_\_



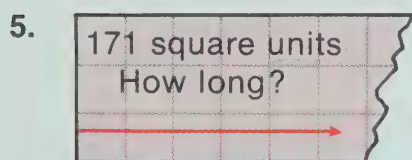
Estimate \_\_\_\_\_ Actual \_\_\_\_\_



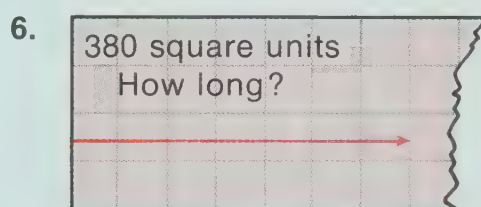
Estimate \_\_\_\_\_ Actual \_\_\_\_\_



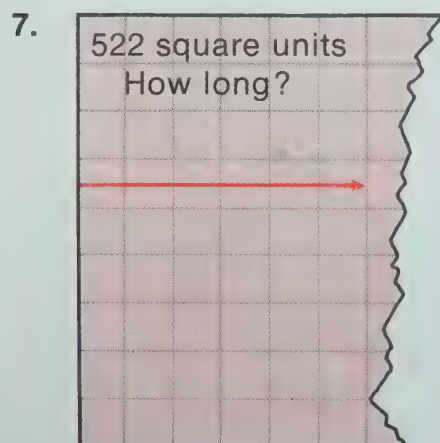
Estimate \_\_\_\_\_ Actual \_\_\_\_\_



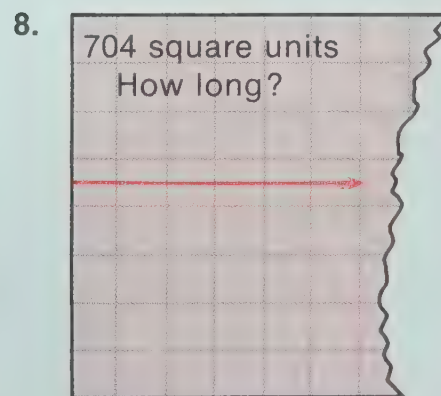
Estimate \_\_\_\_\_ Actual \_\_\_\_\_



Estimate \_\_\_\_\_ Actual \_\_\_\_\_



Estimate \_\_\_\_\_ Actual \_\_\_\_\_



Estimate \_\_\_\_\_ Actual \_\_\_\_\_



### ● Finding Missing Digits

Find the missing digits. Hint: First find the dividend.

1. 
$$\begin{array}{r} 3 \ 4 \\ 6 \overline{) \phantom{00}000000} \\ \underline{\phantom{00}000000} \\ \phantom{00}000000 \\ \underline{\phantom{00}000000} \\ \phantom{00}000000 \\ \underline{\phantom{00}000000} \\ \phantom{00}000000 \\ \underline{\phantom{00}000000} \\ \phantom{00}000000 \end{array}$$

**2.**

		4	6
4 )			
	<hr/>		
	<hr/>		
			3

3. 
$$\begin{array}{r} 52 \\ 7 \overline{) 364} \\ \underline{35} \phantom{0} \\ 14 \phantom{0} \\ \underline{14} \phantom{0} \\ 0 \end{array}$$

4. 
$$\begin{array}{r} 2 \quad 8 \\ 3 \overline{) \phantom{0000}} \\ \underline{\phantom{0000}} \\ \phantom{0000} \\ \underline{\phantom{0000}} \\ \phantom{0000} \\ \underline{\phantom{0000}} \\ \phantom{0000} \end{array}$$

5.

		2	4
9)			
<hr/>			
<hr/>			
			0

6. 
$$\begin{array}{r} 75 \\ 5 \overline{) 375} \\ \underline{35} \phantom{0} \\ 25 \phantom{0} \\ \underline{25} \phantom{0} \\ 0 \end{array}$$





































7. 
$$\begin{array}{r} 51 \\ 6 \overline{) \phantom{0000}} \\ \phantom{00} \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \phantom{00} \end{array}$$

8. 
$$\begin{array}{r} 15 \\ 8 \overline{) \phantom{000}} \\ \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \\ \phantom{00} \phantom{00} \phantom{00} \end{array}$$

9. 
$$\begin{array}{r} 21 \\ 7 \overline{) 147} \\ \underline{14} \phantom{0} \\ 7 \phantom{0} \\ \underline{7} \phantom{0} \\ 0 \end{array}$$





























[illegible]

11.

	4	6
9)		
		
		
		
		
		
		
		
		
		
		
		
		
		
		
		
		
		

2

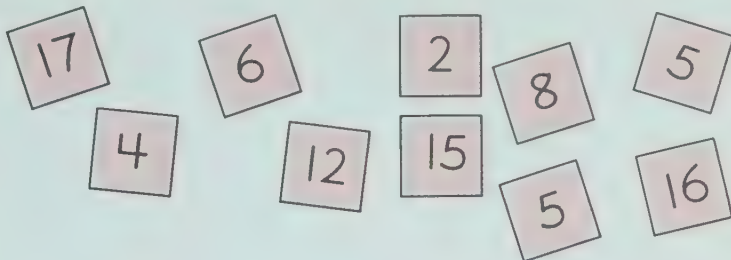
12.

	8	9
3)		
		
		
		
		
		
		
		
		
		
		
		
		
		

0

## ● Finding Averages

Use this set of number cards for the problems below. Write your answers on the blank cards.



1. Find 3 cards so the average is 5.

2. Find 4 cards so the average is 13.

3. Find 3 cards so the average is 6.

4. Find 5 cards so the average is 7.

5. Find 4 cards so the average is 12.

6. Find 6 cards so the average is 8.

7. Suppose you had these cards—  
 6  8  2 What card could you choose so the average of all 4 would be 7.

8. Suppose you had these cards  12  8  6  
 What 2 cards could you choose so the average of all 5 would be 9.

## 3-Digit Quotients

First write your estimate of the quotient in the colored box.  
Then find the quotient. Next find the difference between  
your estimate and the quotient. Rate yourself as shown below.

1.  $4 \overline{)1388}$  Estimate

Difference

Score

2.  $3 \overline{)2562}$  Estimate

Difference

Score

3.  $5 \overline{)3920}$  Estimate

Difference

Score

4.  $6 \overline{)1590}$  Estimate

Difference

Score

5.  $9 \overline{)2916}$  Estimate

Difference

Score

6.  $7 \overline{)4536}$  Estimate

Difference

Score

7.  $8 \overline{)2552}$  Estimate

Difference

Score

8.  $6 \overline{)5502}$  Estimate

Difference

Score

9.  $5 \overline{)4275}$  Estimate

Difference

Score

Score each difference as follows:

- 10 or less—5 points
- Between 10 and 50—3 points
- 50 to 100—1 point
- over 100—0 points

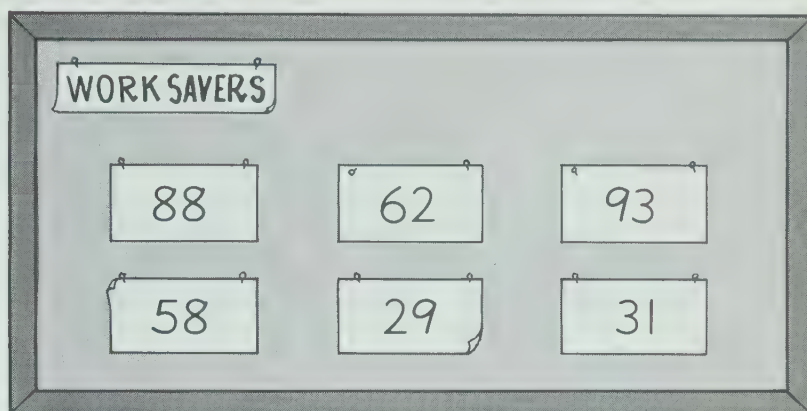
Add your scores and rate yourself.

- 35-45 Fantastic
- 25-34 Excellent
- 15-24 Good
- 0-14 Keep trying



## ● Dividing by Multiples of 10

1. Find the quotients. Don't work any harder than you have to. All the answers are on the bulletin board. The remainder may or may not be zero.



**A**  $60 \overline{)3500}$

**B**  $40 \overline{)2497}$

**C**  $30 \overline{)2640}$

**D**  $20 \overline{)1770}$

**E**  $50 \overline{)1551}$

**F**  $40 \overline{)2320}$

**G**  $20 \overline{)1864}$

**H**  $70 \overline{)2035}$

**I**  $50 \overline{)1491}$

**J**  $30 \overline{)2800}$

**K**  $70 \overline{)2187}$

**L**  $60 \overline{)3737}$

2. Make up some problems of your own. The divisor should be a multiple of ten. The quotient is already given.

**A**  $\overline{)58}$

**B**  $\overline{)39}$

**C**  $\overline{)84}$

**D**  $\overline{)75}$

**E**  $\overline{)63}$

**F**  $\overline{)71}$

**G**  $\overline{)28}$

**H**  $\overline{)96}$

## ● Missing Digit Problems

Find the missing digits.

1.  $\begin{array}{r} 77 \\ 3 \overline{) 350} \\ 350 \\ \hline 1 \end{array}$

2.  $\begin{array}{r} 9 \square \\ 7 \overline{) 720} \\ 720 \\ \hline 9 \\ 8 \\ \hline 1 \end{array}$

3.  $\begin{array}{r} 993 \\ 6 \overline{) 5900} \\ 5400 \\ \hline \square 63 \\ 540 \\ \hline \square \square \\ 18 \end{array}$

4.  $\begin{array}{r} \square \square \square \\ 2 \overline{) 2615} \\ 2400 \\ \hline 215 \\ 200 \\ \hline 15 \\ 12 \\ \hline 3 \end{array}$

5.  $\begin{array}{r} 3 \square \square \\ 7 \overline{) 2492} \\ 2100 \\ \hline \square \square \square \\ 350 \\ \hline \square \square \\ 42 \\ \hline 0 \end{array}$

6.  $\begin{array}{r} 8 \square \\ 30 \overline{) \square \square \square \square} \\ 2400 \\ \hline 12 \square \\ 120 \\ \hline 5 \end{array}$

7.  $\begin{array}{r} 65 \\ 3 \overline{) 3027} \\ 2760 \\ \hline \square \square \square \\ 230 \\ \hline 37 \end{array}$

8.  $\begin{array}{r} \square 3 \\ 7 \overline{) 5276} \\ 5040 \\ \hline \square \square \square \\ 216 \\ \hline 20 \end{array}$

9.  $\begin{array}{r} 6 \square \\ 35 \overline{) \square \square \square \square} \\ 2100 \\ \hline \square \square \square \\ 175 \\ \hline 0 \end{array}$

The chart below gives special names we will use on this page for special sets of numbers. Complete the chart. Then complete the tables and statements.

pink white gray

[illegible]

+	0	3	6	9
0				
3				
6				
9				

Table 1

×	0	3	6	9
0				
3				
6				
9				

Table 2

+	2	5	8	11
1				
4				
7				
10				

Table 3

×	1	4	7	10
0				
3				
6				
9				

Table 4

1. In Table 1, the sum of a “pink” number and a “pink” number is a \_\_\_\_\_ number.
2. In Table 2, the product of a “pink” number and a “pink” number is a \_\_\_\_\_ number.
3. In Table 3, the sum of a “white” number and a “gray” number is a \_\_\_\_\_ number.
4. In Table 4, the product of a “pink” number and a “white” number is a \_\_\_\_\_ number.



## ● Factors and Products

All but two of the numbers below have at least one factor greater than 1 and less than the number itself. Give one or more such factors for each number that has them.

1. **38**

Factors \_\_\_\_\_

2. **39**

Factors \_\_\_\_\_

3. **37**

Factors \_\_\_\_\_

4. **51**

Factors \_\_\_\_\_

5. **85**

Factors \_\_\_\_\_

6. **91**

Factors \_\_\_\_\_

7. **77**

Factors \_\_\_\_\_

8. **78**

Factors \_\_\_\_\_

9. **79**

Factors \_\_\_\_\_

10. **143**

Factors \_\_\_\_\_

11. **119**

Factors \_\_\_\_\_

12. **221**

Factors \_\_\_\_\_

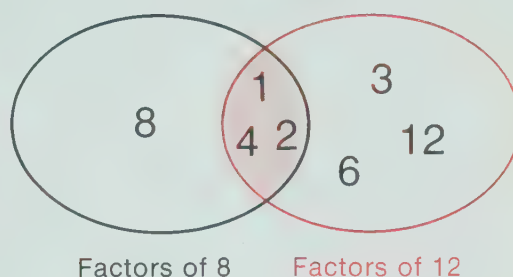
## ● Greatest Common Factor

Study the example below of a **Venn Diagram**. Notice the shaded region is common to both sets. It contains the **common** factors of the two numbers.

The factors of 8: {1, 2, 4, 8}  
 The factors of 12: {1, 2, 3, 4, 6, 12}



**Venn Diagram**

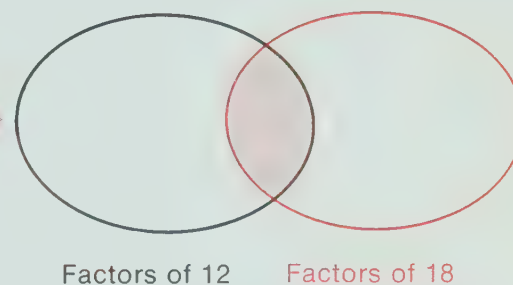


List each set of factors. Then put them in the **Venn Diagram**. Give the greatest common factor (GCF) of the 2 numbers.

1. **A** Factors of 12: \_\_\_\_\_

**B** Factors of 18: \_\_\_\_\_

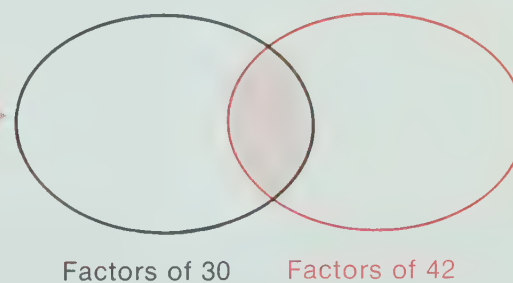
**C** The GCF of 12 and 18 is \_\_\_\_\_.



2. **A** Factors of 30: \_\_\_\_\_

**B** Factors of 42: \_\_\_\_\_

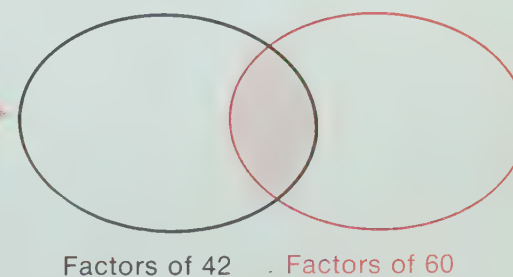
**C** The GCF of 30 and 42 is \_\_\_\_\_.



3. **A** Factors of 42: \_\_\_\_\_

**B** Factors of 60: \_\_\_\_\_

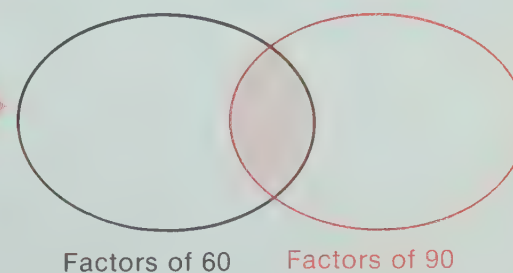
**C** The GCF of 42 and 60 is \_\_\_\_\_.



4. **A** Factors of 60: \_\_\_\_\_

**B** Factors of 90: \_\_\_\_\_

**C** The GCF of 60 and 90 is \_\_\_\_\_.



## ● Prime Numbers

1. Draw rectangles (or squares) for each of these areas. (No single rows or columns allowed.) Write the number of units inside the figure.

**A** 12 square units

**B** 10 square units

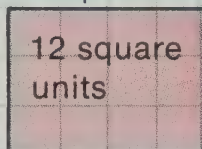
**C** 24 square units

**D** 40 square units

**E** 25 square units

**F** 27 square units

Example for **A**



2. The prime numbers are not areas for rectangles like those above.  
Draw rectangles for these numbers that are not prime.

**A** 11

**B** 13

**C** 15

**D** 17

**E** 19

**F** 21

**G** 23

3. Could you use a rectangle to show whether or not 51 is prime?



## ● Number Puzzlers

### 1. Try these puzzles.

**A** I'm a very odd teenager. In fact, I'm the only odd teenager

who isn't prime. Who am I? \_\_\_\_\_

**B** We're the oldest teenage primes. They call us twins because we differ

by just 2. Who are we? \_\_\_\_\_

**C** We're the only two primes that differ by just 1. We're side-

by-side. Who are we? \_\_\_\_\_

**D** We're the youngest pair of twins you'll ever find. Remember we're prime and differ by 2. Who are

we? \_\_\_\_\_

### 2. It is thought that every even number greater than 2 is the sum of two primes. How many pairs of primes can you find below?

$$4 = \underline{2} + \underline{2}$$

$$6 = \underline{3} + \underline{3}$$

$$8 = \underline{3} + \underline{5}$$

$$10 = \underline{\quad} + \underline{\quad}$$

$$12 = \underline{\quad} + \underline{\quad}$$

$$14 = \underline{\quad} + \underline{\quad}$$

$$16 = \underline{\quad} + \underline{\quad}$$

$$18 = \underline{\quad} + \underline{\quad}$$

$$20 = \underline{\quad} + \underline{\quad}$$

$$22 = \underline{\quad} + \underline{\quad}$$

$$24 = \underline{\quad} + \underline{\quad}$$

$$26 = \underline{\quad} + \underline{\quad}$$

$$28 = \underline{\quad} + \underline{\quad}$$

$$30 = \underline{\quad} + \underline{\quad}$$

$$32 = \underline{\quad} + \underline{\quad}$$

$$34 = \underline{\quad} + \underline{\quad}$$

$$36 = \underline{\quad} + \underline{\quad}$$

$$38 = \underline{\quad} + \underline{\quad}$$

$$40 = \underline{\quad} + \underline{\quad}$$

$$42 = \underline{\quad} + \underline{\quad}$$

$$44 = \underline{\quad} + \underline{\quad}$$

$$46 = \underline{\quad} + \underline{\quad}$$

$$48 = \underline{\quad} + \underline{\quad}$$

$$50 = \underline{\quad} + \underline{\quad}$$

$$52 = \underline{\quad} + \underline{\quad}$$

$$54 = \underline{\quad} + \underline{\quad}$$

$$56 = \underline{\quad} + \underline{\quad}$$

$$58 = \underline{\quad} + \underline{\quad}$$

$$60 = \underline{\quad} + \underline{\quad}$$

$$62 = \underline{\quad} + \underline{\quad}$$

$$64 = \underline{\quad} + \underline{\quad}$$

$$66 = \underline{\quad} + \underline{\quad}$$

$$68 = \underline{\quad} + \underline{\quad}$$

$$70 = \underline{\quad} + \underline{\quad}$$

$$72 = \underline{\quad} + \underline{\quad}$$

$$74 = \underline{\quad} + \underline{\quad}$$

## ● A Number Theory Puzzle

### ACROSS

1. First 2-digit multiple of 7
3. Last prime before 41
5.  $10,000 + 1000 + 100 + 10 + 1$
9. Hundreds and tens places in 2035
10. Factors: 1, 2, 4, 8, 16
11. 6 sixes
12.  $10^2 - 10$
13. Smallest 2-digit number
14. One of it's 3 factors is 7
16. First prime  $< 60$
17. Between 29 and it's twin.
18. Smallest 2-digit prime.
20. 6, 7, 5, 7, 4, 7, —, —, —, —.
22. A product of primes,  $3 \times 3 \times 7 \times 7$

26. 2, two, 11, 2, two
29. First 4 multiples of 3, reverse order.
30. A thousand more than 1135.
32. First 5 even numbers.
33.  $10^2 + 94$
34. 1000 more than 48 down.
37. Twin prime with 43.
39. Only prime in the nineties.
41. Greatest common factor of 30 and 40.
42. Smallest teen prime.
43. Twin prime with 11.
45. Prime factors: 7 and 13.
46. Last 2-digit multiple of 10.
47. Prime factors: 5 and 11.
49. Teen number whose only prime factor is 2.
50. Even digits, reverse order.
51. 0, 12, 24, 36, 48, 60, ?
52. Twin prime with 17.

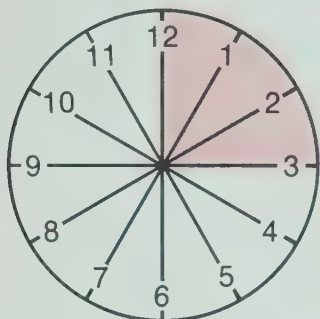
1	2		3	4			5	6		7	8
9			10				11			12	
13				14	15		16			17	
	18	19		20		21					
									22	23	24
25		26	27		28			29			
30	31				32						
33											
				34		35	36		37	38	
39	40		41			42				43	44
45			46				47	48		49	
50							51			52	

### DOWN

1. First 3-digit prime.
2. It's prime factors are 23, 11, and 17.
3. First prime after 29.
4. Largest number with 3, 4, 6, and 7.
5. First 4 odd numbers.
6. One of it's 3 factors is 13.
7.  $(2 \times 10^2) - 7$
8. Smallest 3-digit number.
15. Largest 2-digit prime.
19. Smallest number with the digits 0, 1, 2, 3, 4.
21. Smallest prime in all 4 places.
22. forty-six thousand, eight hundred four.
23. Twin prime with 41.
24. Prime factors: 2, 2, 5, 5.
25. One of it's 3 factors is 11.
27. One of it's 3 factors is 5.
28. Prime factors: 2, 2, 2, 5, 5, 5.
29. 3 thirty-twos
31. Largest teen prime.
34. Smallest 4-digit number.
35. Prime factors: 3 and 17.
36. First 4 primes.
38. 11 hundreds and 11.
39. 1000 — smallest prime.
40. One minute past quarter after 7.
41.  $200 - (2 \times 2 \times 2)$
44. 0, —, —, —, 12, 15, 18, 21.
48.  $13 \times 2 \times 2$

There are 60 minutes in an hour. Color the fractional part of the clock (1 hour) indicated by the number of minutes. Then give the fraction to tell what part you shaded.

EXAMPLE:



15 minutes

Part of an hour.  $\frac{1}{4}$

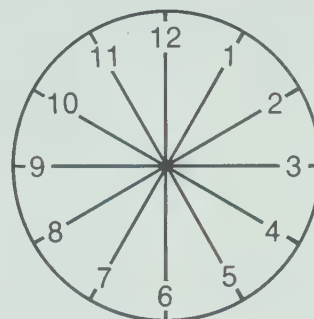
1.



30 minutes

Part of an hour. \_\_\_\_\_

2.



45 minutes

Part of an hour. \_\_\_\_\_

3.



10 minutes

Part of an hour. \_\_\_\_\_

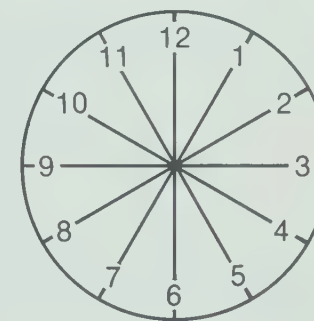
4.



20 minutes

Part of an hour. \_\_\_\_\_

5.



50 minutes

Part of an hour. \_\_\_\_\_

6.



5 minutes

Part of an hour. \_\_\_\_\_

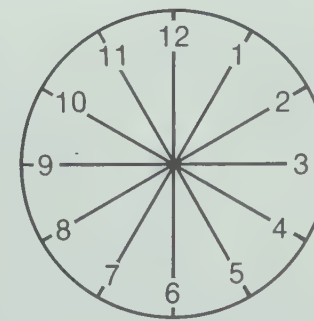
7.



25 minutes

Part of an hour. \_\_\_\_\_

8.



60 minutes

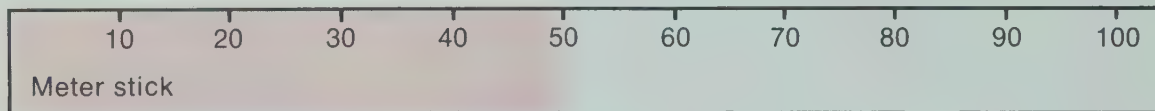
Part of an hour. \_\_\_\_\_



## Fractional Parts of a Meter

There are 100 centimeters in a meter. Think of the rulers below as meter sticks reduced in size. Shade the given fractional part. Then answer the questions.

EXAMPLE:

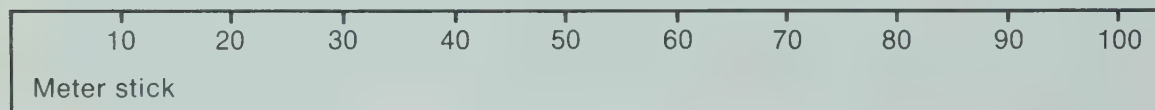


Shade  $\frac{1}{2}$

How many centimeters did you shade? 50

What fractional part (in hundredths) did you shade?  $\frac{50}{100}$

1.

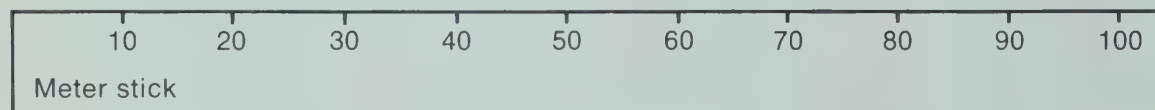


Shade  $\frac{1}{4}$

How many centimeters did you shade? \_\_\_\_\_

What fractional part (in hundredths) did you shade? \_\_\_\_\_

2.

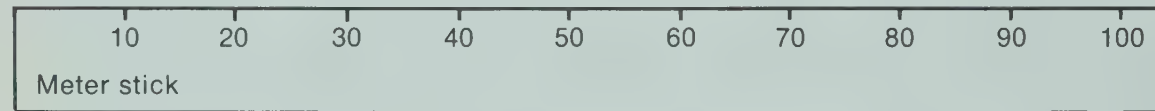


Shade  $\frac{3}{4}$

How many centimeters did you shade? \_\_\_\_\_

What fractional part (in hundredths) did you shade? \_\_\_\_\_

3.

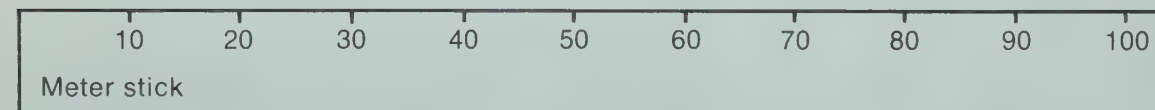


Shade  $\frac{1}{10}$

How many centimeters did you shade? \_\_\_\_\_

What fractional part (in hundredths) did you shade? \_\_\_\_\_

4.

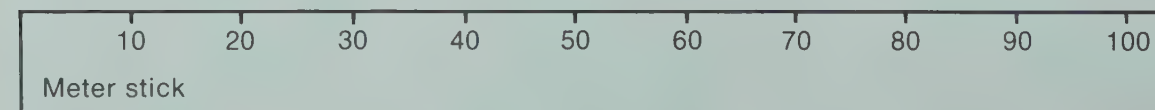


Shade  $\frac{1}{5}$

How many centimeters did you shade? \_\_\_\_\_

What fractional part (in hundredths) did you shade? \_\_\_\_\_

5.



Shade  $\frac{3}{5}$

How many centimeters did you shade? \_\_\_\_\_

What fractional part (in hundredths) did you shade? \_\_\_\_\_

## ● Finding Missing Fractions

Give the missing fractions. Then color a fractional part of the rod for the set of equivalent fractions. The rod is divided into 10ths to help you color.

1.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{7}{28}, \frac{8}{32}, \frac{9}{36}, \frac{\quad}{\quad}, \dots$

--	--	--	--	--	--	--	--	--	--

2.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{18}{30}, \frac{21}{35}, \frac{24}{40}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \dots$

--	--	--	--	--	--	--	--	--	--

3.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{24}{32}, \frac{27}{36}, \frac{30}{40}, \dots$

--	--	--	--	--	--	--	--	--	--

4.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{25}{40}, \frac{30}{48}, \frac{35}{56}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \dots$

--	--	--	--	--	--	--	--	--	--

5.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{56}{80}, \frac{63}{90}, \frac{70}{100}, \dots$

--	--	--	--	--	--	--	--	--	--

6.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{12}{18}, \frac{14}{21}, \frac{16}{24}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \dots$

--	--	--	--	--	--	--	--	--	--

7.  $\frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{\quad}{\quad}, \frac{9}{18}, \frac{\quad}{\quad}, \dots$

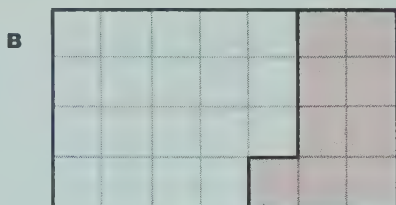
--	--	--	--	--	--	--	--	--	--

## Tenths and Hundredths

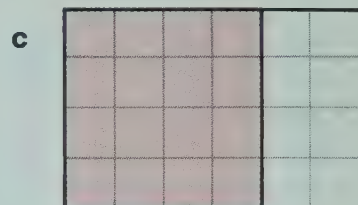
1. Much of your work with fractions will use tenths and hundredths.  
Estimate the numerator of each fraction.



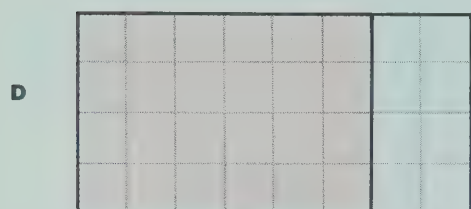
About  $\frac{42}{100}$  is shaded.



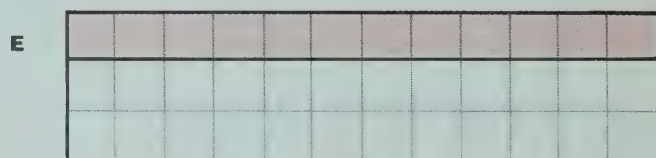
About  $\frac{42}{100}$  is shaded.



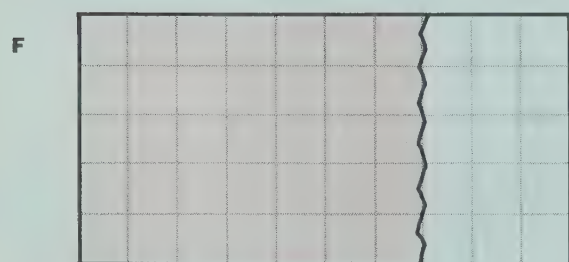
About  $\frac{42}{100}$  is shaded.



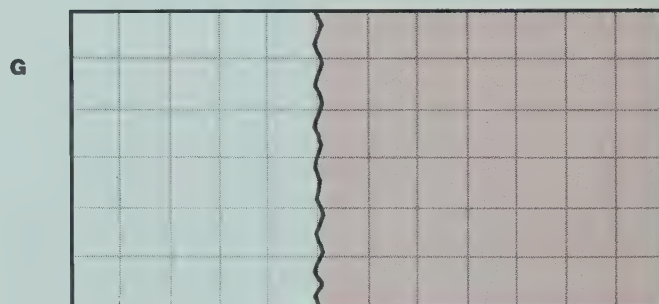
About  $\frac{42}{100}$  is shaded.



About  $\frac{42}{100}$  is shaded.

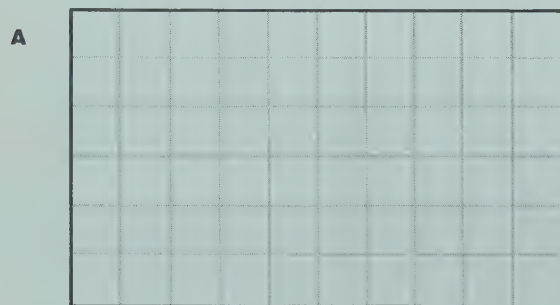


About  $\frac{42}{100}$  is shaded.



About  $\frac{42}{100}$  is shaded.

2. Shade the given amount as close as you can.



Shade about  $\frac{4}{10}$ .



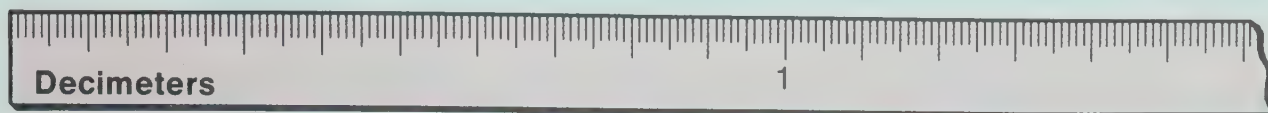
Shade about  $\frac{75}{100}$ .



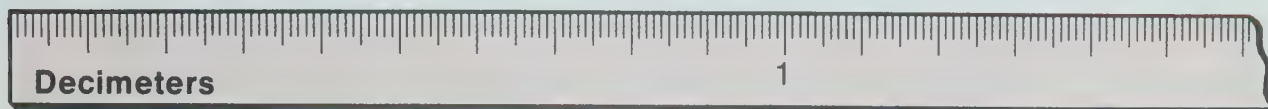
## ● Using Improper Fractions

The unit for the ruler below is the decimeter (10 centimeters).  
See if you can draw the figures suggested.

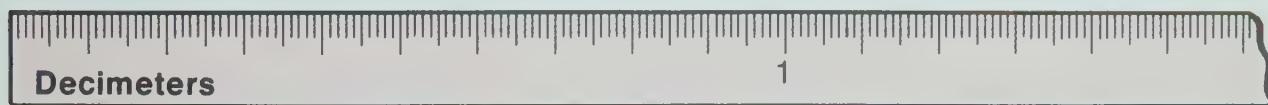
1. Draw a pencil that is  $\frac{12}{10}$  decimeters long.



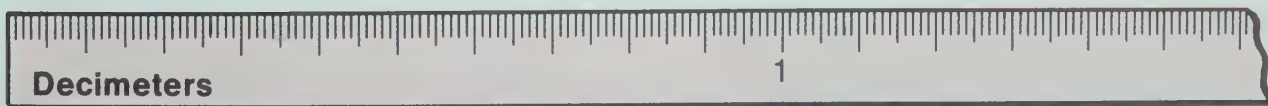
2. Draw a ball point pen that is  $\frac{13}{10}$  decimeters long.



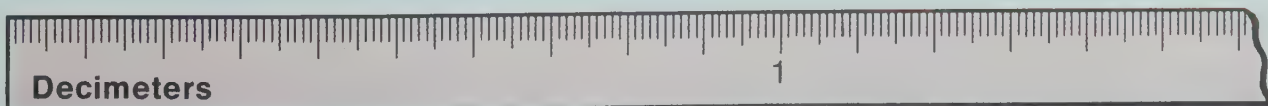
3. Draw an ice cream stick that is  $\frac{3}{2}$  decimeters long.



4. Draw a drinking straw that is  $\frac{110}{100}$  decimeters long.



5. Draw a tooth brush that is  $\frac{6}{5}$  decimeters long.



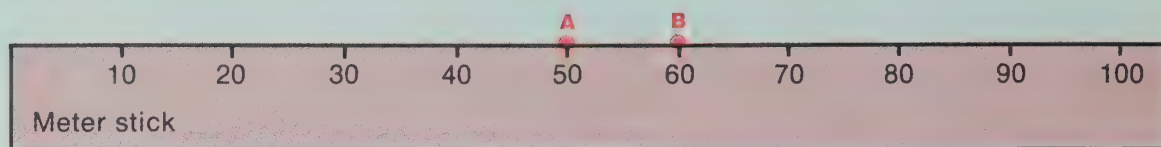
## ● Exploring Fractions that are not Equivalent

Can you find a way to mark points on the meter stick for each length.  
After you do, ring the greater length.

EXAMPLE:

A  $\frac{1}{2}$  meter

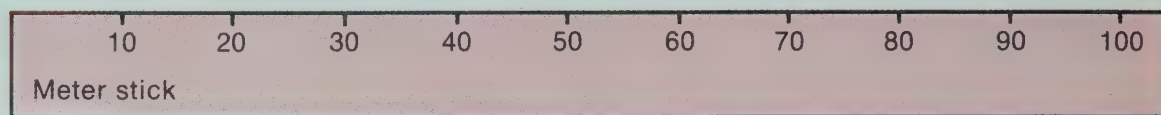
B  $\frac{6}{10}$  meter



1.

A  $\frac{1}{4}$  meter

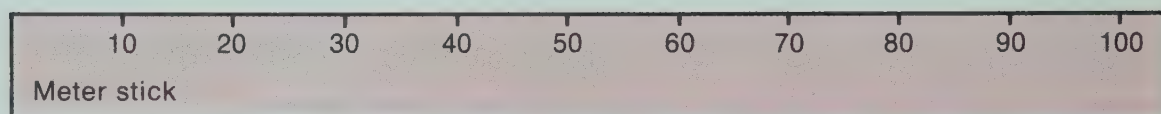
B  $\frac{3}{10}$  meter



2.

A  $\frac{7}{10}$  meter

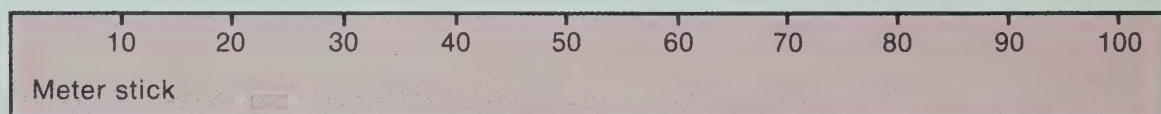
B  $\frac{3}{4}$  meter



3.

A  $\frac{2}{5}$  meter

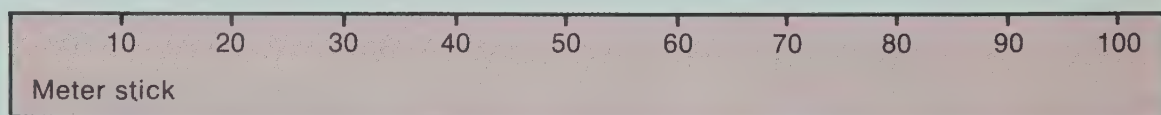
B  $\frac{3}{10}$  meter



4.

A  $\frac{3}{4}$  meter

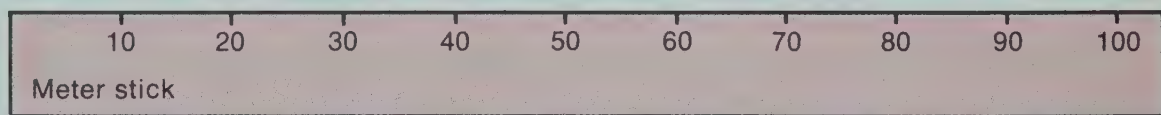
B  $\frac{8}{10}$  meter



5.

A  $\frac{3}{4}$  meter

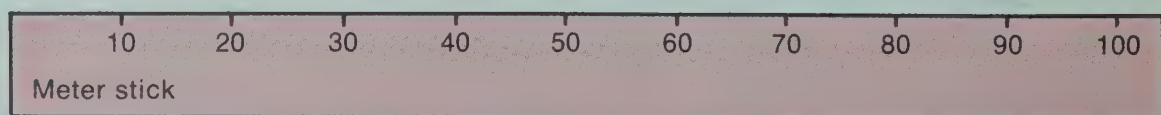
B  $\frac{2}{3}$  meter



6.

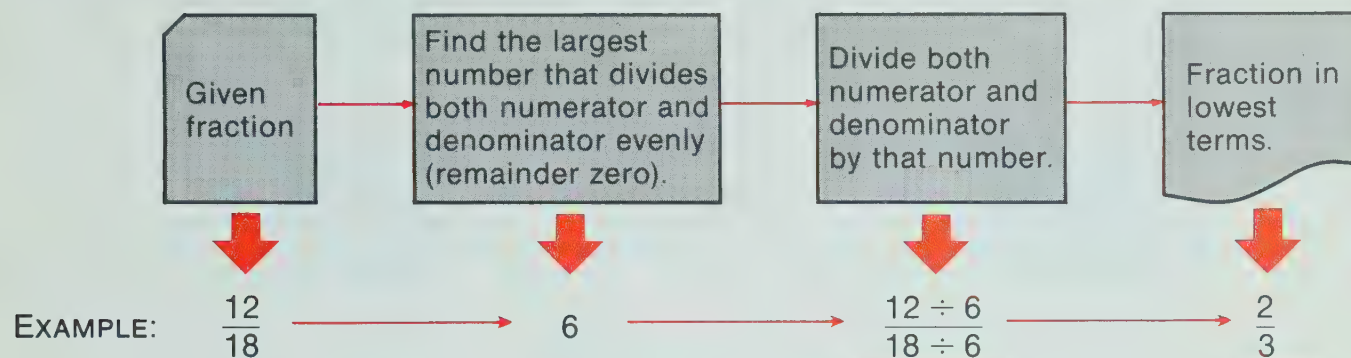
A  $\frac{2}{3}$  meter

B  $\frac{5}{8}$  meter



## ● Finding Lowest-terms Fractions

1. The flow chart below shows how to find a lowest-terms fraction that is equivalent to the given fraction.



**A** Now you try one.

$$\frac{12}{20}$$

$$\frac{\quad}{\quad}$$

$$\frac{\quad}{\quad}$$

$$\frac{\quad}{\quad}$$

If you did the work correctly the lowest-terms fraction should be  $\frac{3}{5}$ .

**B** Try another.

$$\frac{10}{16}$$

$$\frac{\quad}{\quad}$$

$$\frac{\quad}{\quad}$$

$$\frac{\quad}{\quad}$$

This time you should get  $\frac{5}{8}$ .

2. Now find the lowest-terms fraction for each of these fractions. The answers are in the answer box.

**A**  $\frac{6}{8}$

**B**  $\frac{8}{12}$

**C**  $\frac{9}{18}$

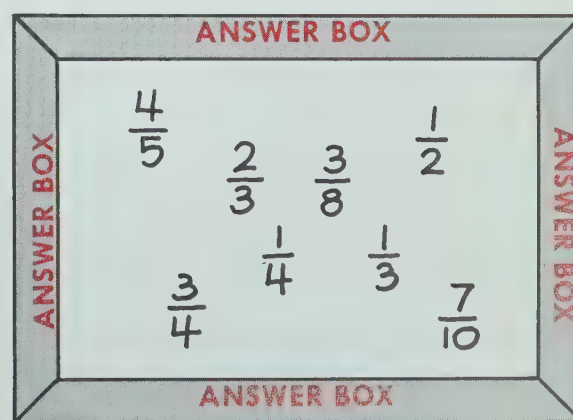
**D**  $\frac{21}{30}$

**E**  $\frac{12}{32}$

**F**  $\frac{5}{15}$

**G**  $\frac{6}{24}$

**H**  $\frac{24}{30}$

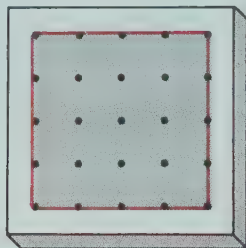




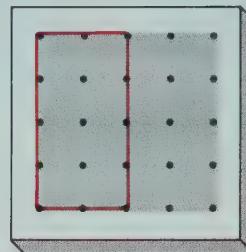
## ● Fractions and Area

1. Think of the figures below as boards with 25 nails driven in part way.  
Think of the colored outlines as rubber bands around the nails.

If this rubber band  
encloses an area of 1,

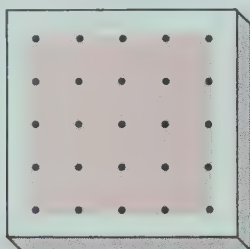


what area does this  
rubber band enclose?

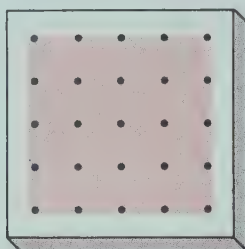


2. Think of the shaded part as having area 1. Show an  
area on the nail board for each fraction.

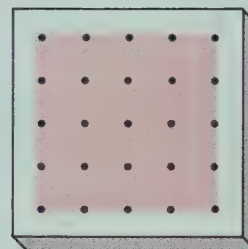
A  $\frac{1}{4}$



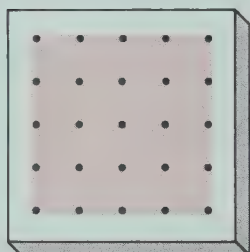
B  $\frac{1}{8}$



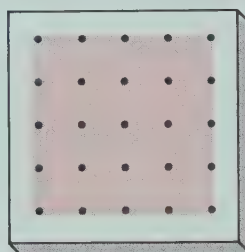
C  $\frac{1}{16}$



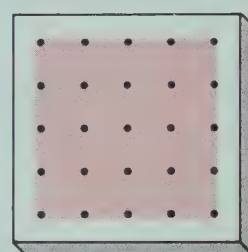
D  $\frac{3}{4}$



E  $\frac{5}{8}$

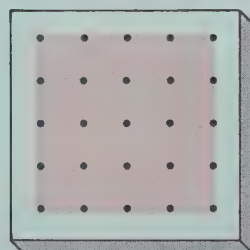
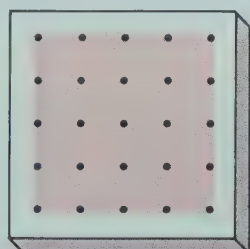


F  $\frac{7}{16}$

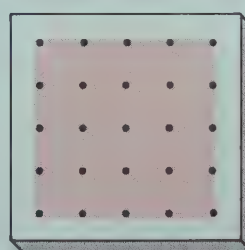
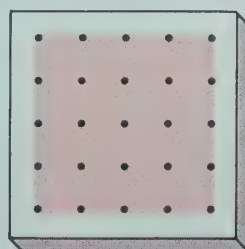


3. Show each fraction with as many different shaped regions as you can.  
You may want to use the “extra” nailboards to show your answers.

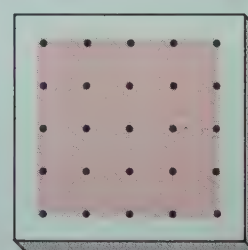
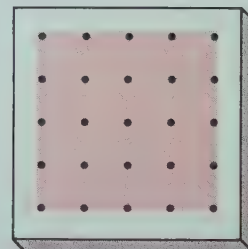
A  $\frac{1}{4}$



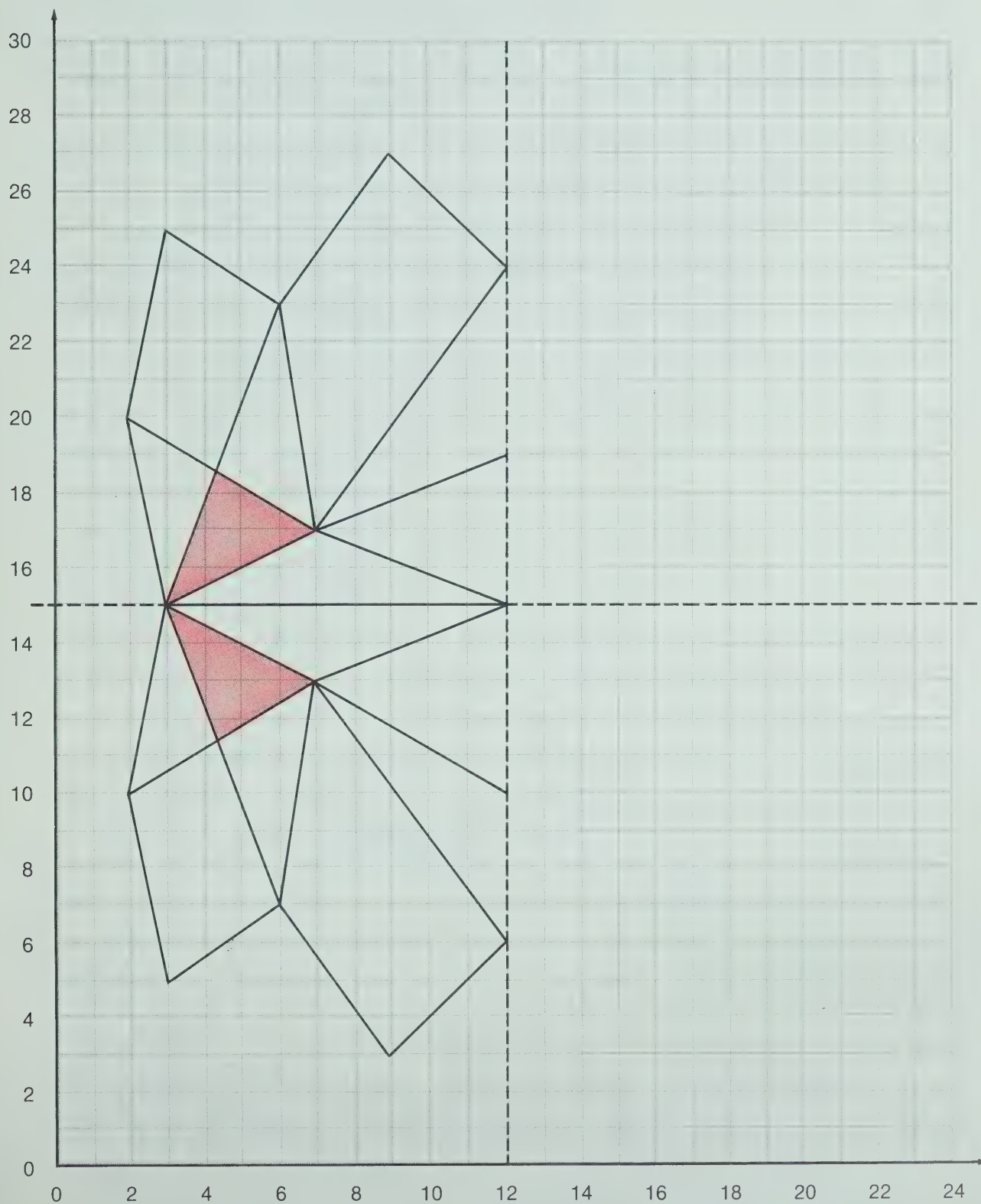
B  $\frac{1}{8}$



C  $\frac{1}{16}$



Use coordinates to help you draw the other half of this symmetrical design. Can you complete coloring the design so it can be folded along either dashed line and the colors will “match.”



Try making a symmetrical design of your own on another sheet of graph paper

## ● Using Coordinates to Sketch Circles

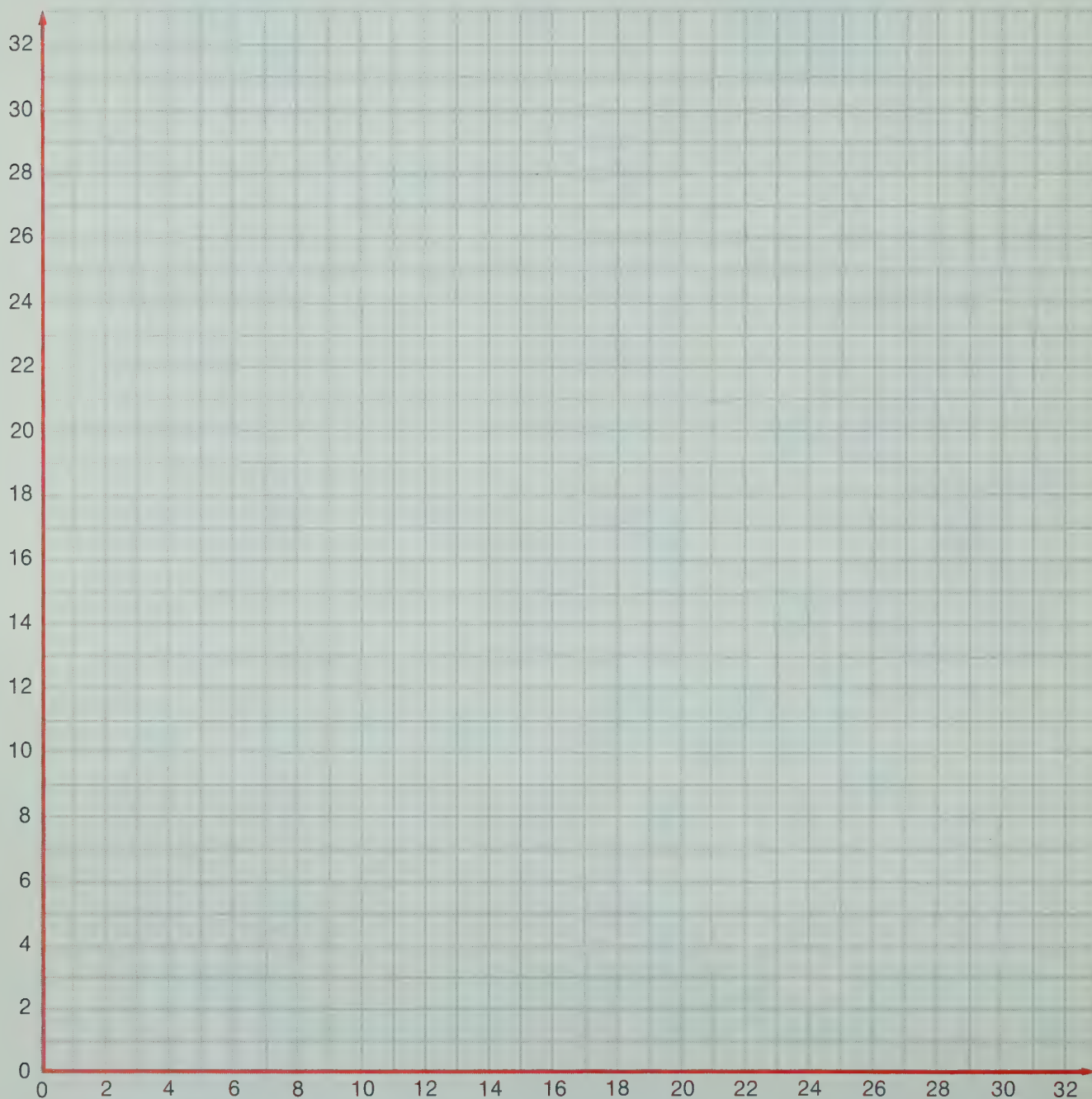
Use the “coordinate clues” below to help you sketch two circles.  
Remember, circles are symmetrical figures.

### First Circle

- Clue 1 Center:  $(12, 12)$   
Clue 2 Radius: 10  
Clue 3 Passes through  $(18, 4)$  and  $(20, 6)$

### Second Circle

- Clue 1 Center:  $(12, 23)$   
Clue 2 Radius: 8  
Clue 3 Passes through (approximate):  
 $(5, 27)$  and  $(8, 30)$



If you made your sketches carefully, the two circles should intersect at about  $(5, 19)$  and  $(19, 19)$ .

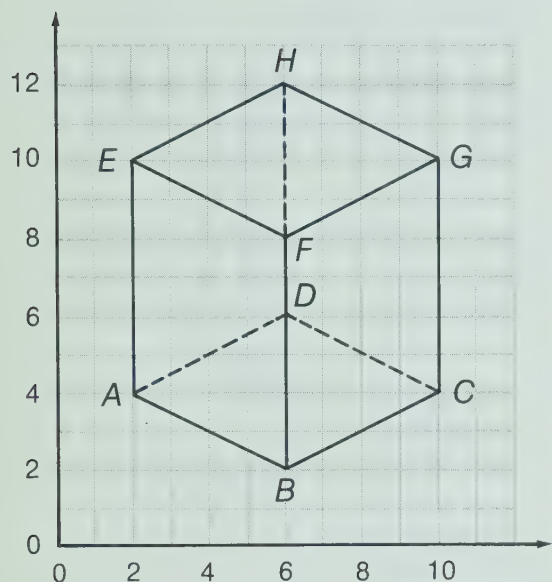


## ● Stretching and Shrinking with Coordinates

Give the coordinates for the vertices on the cube and pyramid.

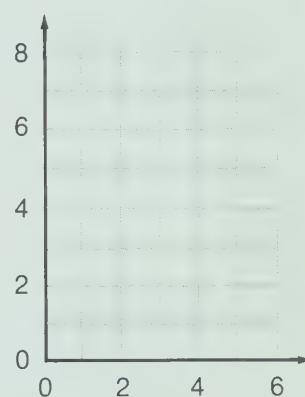
Divide all the cube coordinates by 2 to get a new set of coordinates. Double the coordinates of the pyramid.

Graph the new sets and connect the points to get a smaller cube and larger pyramid.

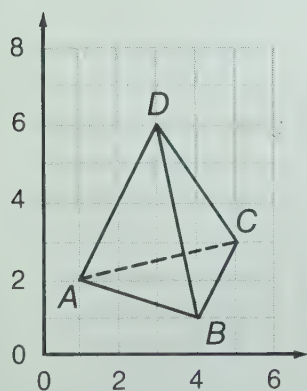


Cube coordinates		half
A: (2, 4)	→	(1, 2)
B: (6, 2)	→	(3, 1)
C: (10, 4)	→	( , )
D: ( , )	→	( , )
E: ( , )	→	( , )
F: ( , )	→	( , )
G: ( , )	→	( , )
H: ( , )	→	( , )

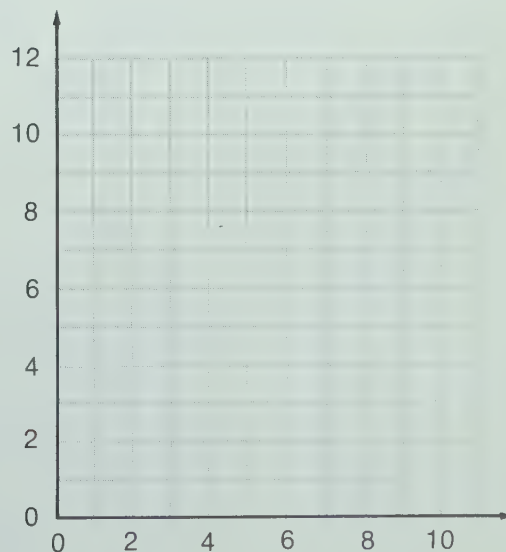
Smaller Cube



Larger Pyramid



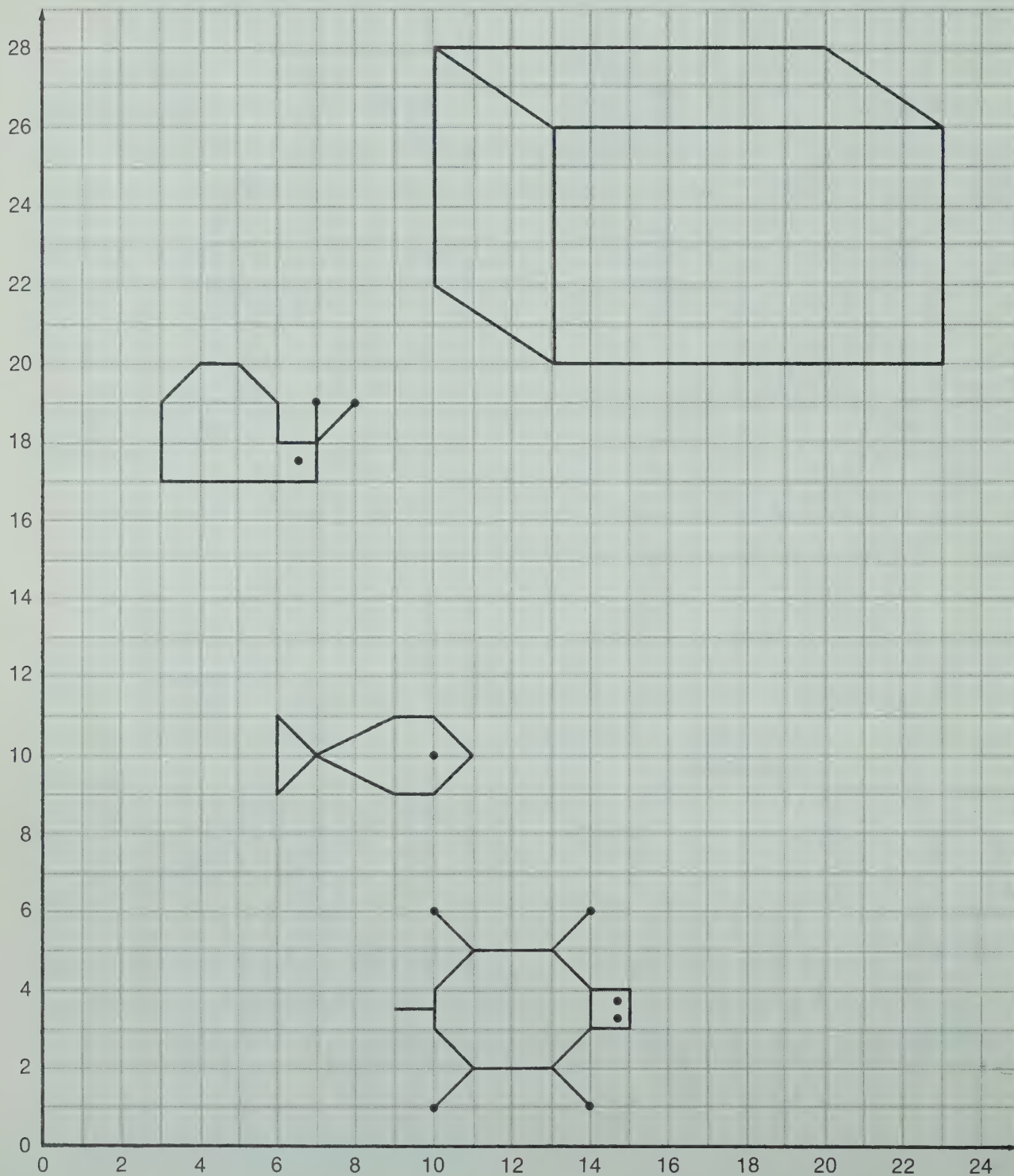
Pyramid coordinates		double
A: ( , )	→	( , )
B: ( , )	→	( , )
C: ( , )	→	( , )
D: ( , )	→	( , )



## ● Moving Figures

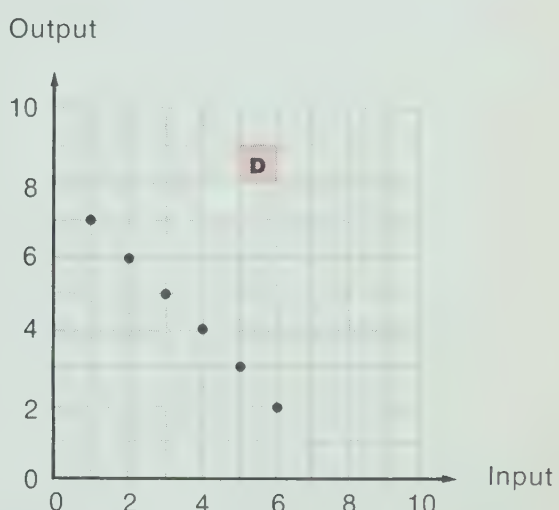
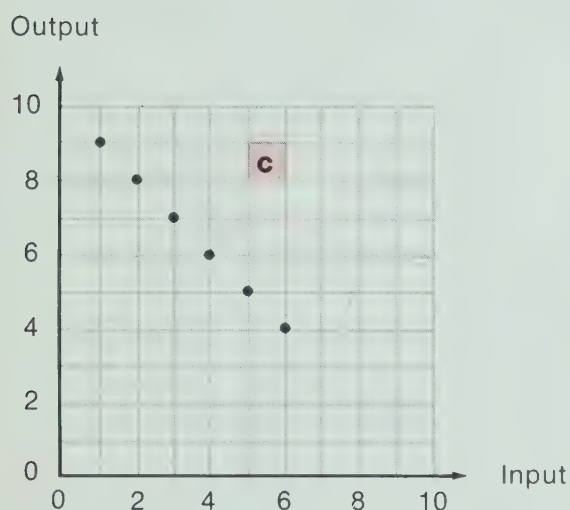
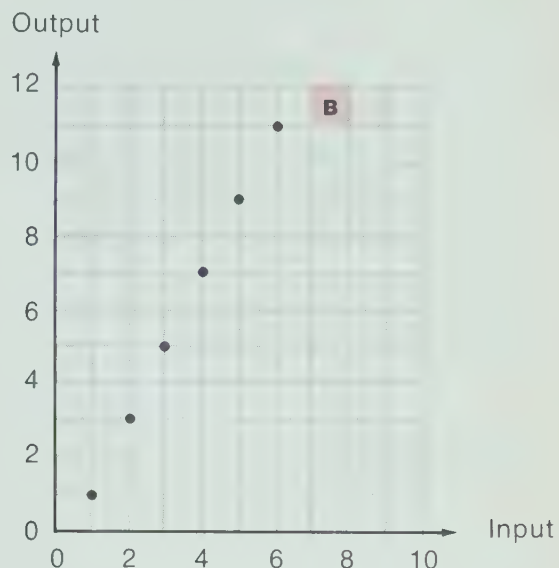
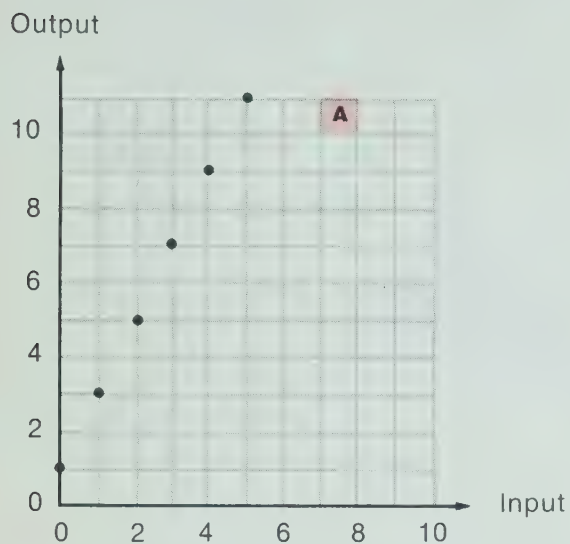
First, tell what moves you would make to put the fish, snail, and turtle in the tank. Then put them in the tank.

Moves { Fish \_\_\_\_\_  
 Snail \_\_\_\_\_  
 Turtle \_\_\_\_\_



## Finding Function Rules

Complete an input-output card for each point on the graph.  
Then give a function rule for the set of cards.



Cards for **A**

Function Rule

Input	Output
( 0 , 1 )	
( 1 , 3 )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	

Cards for **B**

Function Rule

Input	Output
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	

Cards for **C**

Function Rule

Input	Output
( 1 , 9 )	
( 2 ,   )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	

Cards for **D**

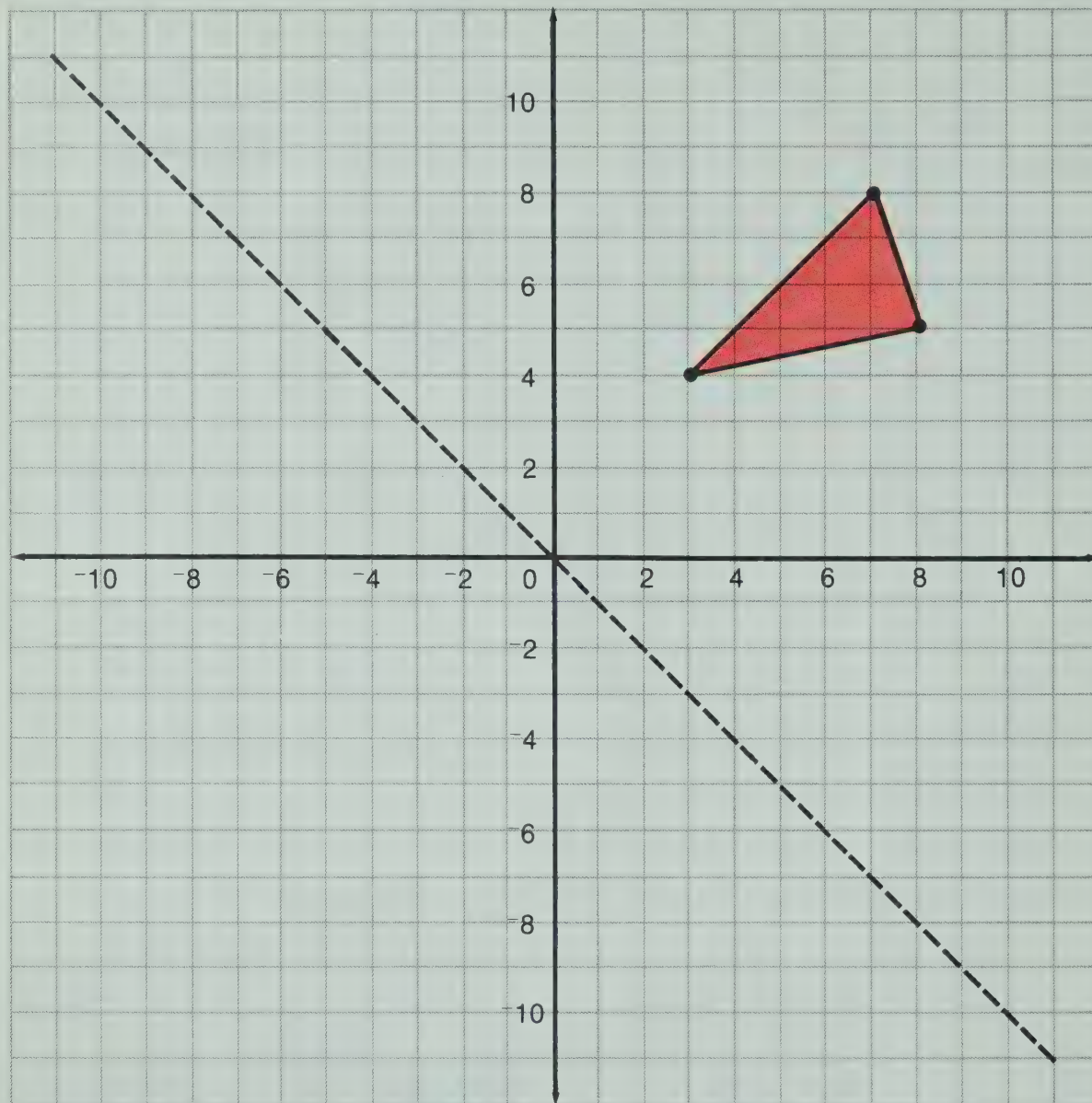
Function Rule

Input	Output
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	
(   ,   )	



## ● Positive and Negative Coordinates

Imagine the red triangle is covered with wet paint. If you folded the paper it would leave a mark on the other side of the fold.



1. Show the mark the red triangle will leave when you fold the paper along the given lines. Give the coordinates of the vertices of each triangle.

**A** The horizontal number line. \_\_\_\_\_

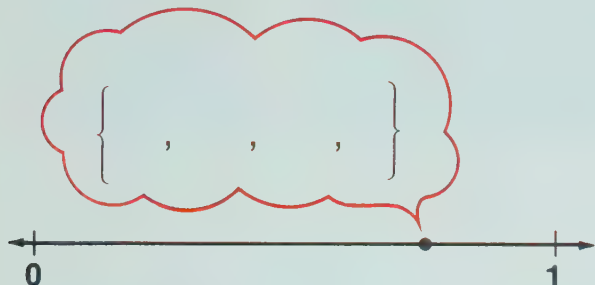
**B** The vertical number line. \_\_\_\_\_

**C** The dashed line. \_\_\_\_\_

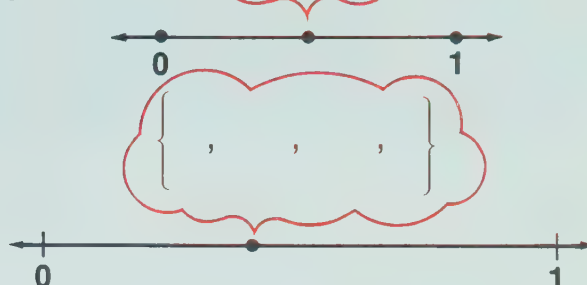
Give a set of 4 equivalent fractions for the number indicated by the arrow. You may find it helpful to cut out the two rulers at the bottom of the page.

$$\left\{ \frac{1}{2}, \frac{2}{4}, \frac{3}{6}, \frac{4}{8} \right\}$$

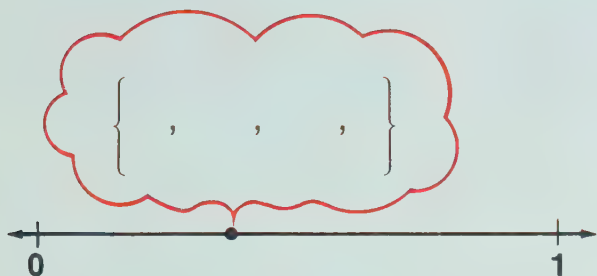
1.



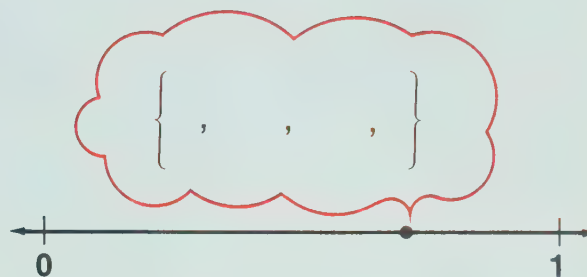
2.



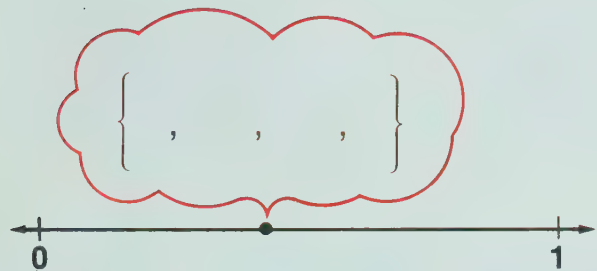
3.



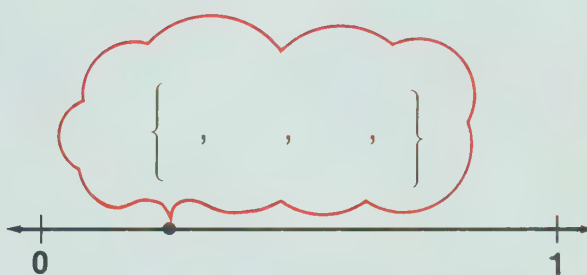
4.



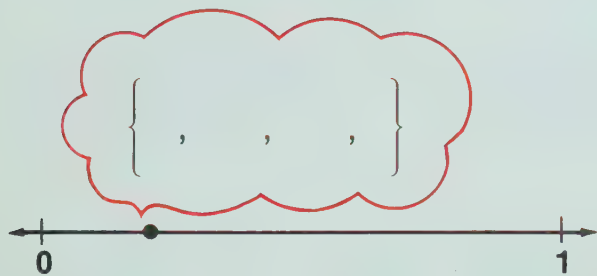
5.



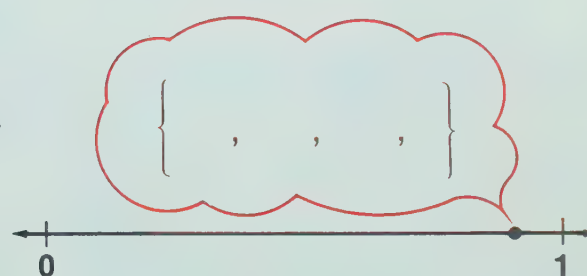
6.



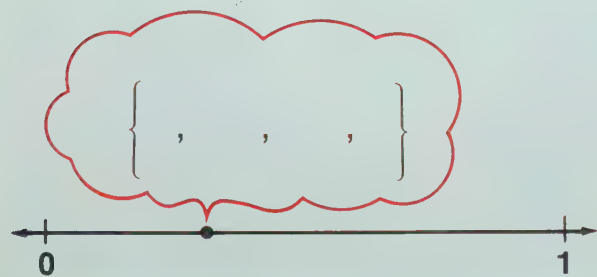
7.



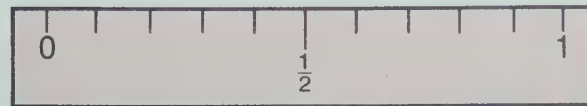
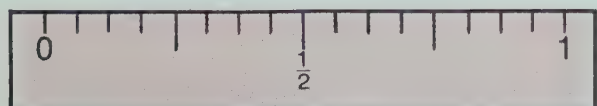
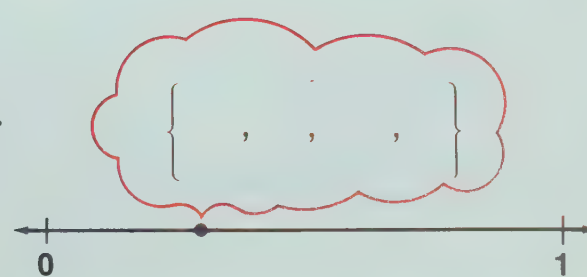
8.



9.

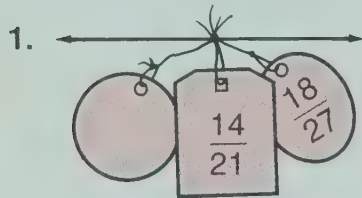


10.

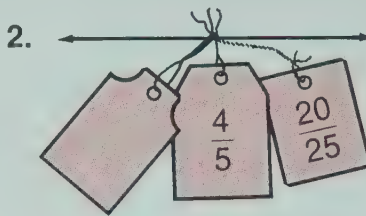


## Fractional Number Names

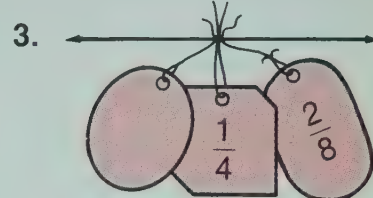
Complete each blank name tag according to directions.



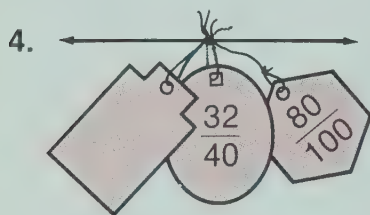
lowest  
terms



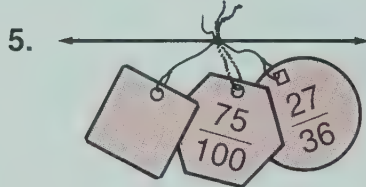
tenths



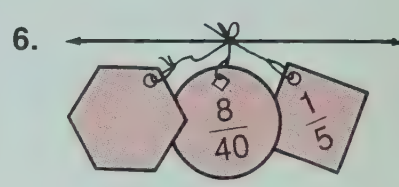
hundredths



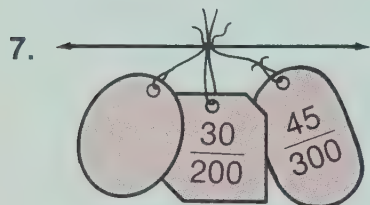
tenths



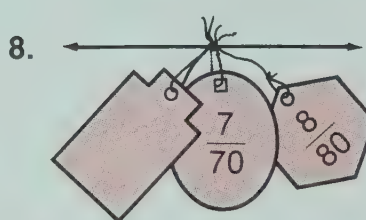
lowest  
terms



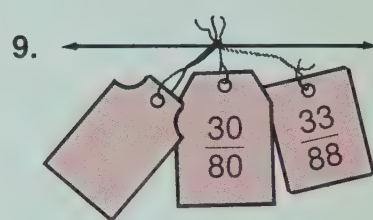
tenths



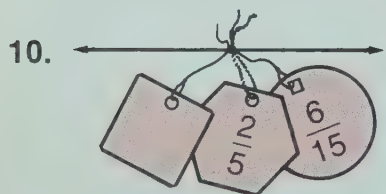
hundredths



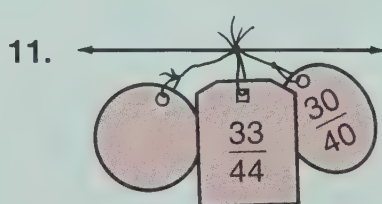
tenths



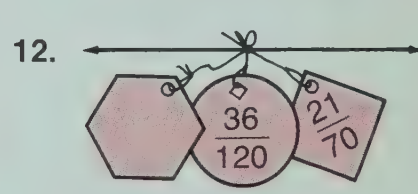
lowest  
terms



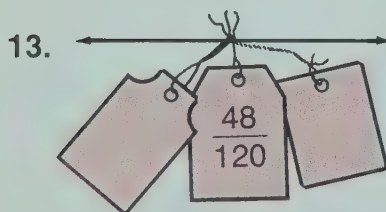
hundredths



hundredths

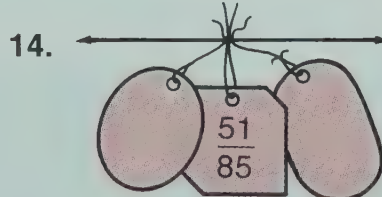


tenths



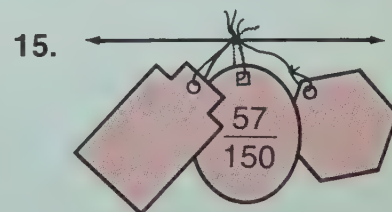
lowest  
terms

tenths



tenths

hundredths



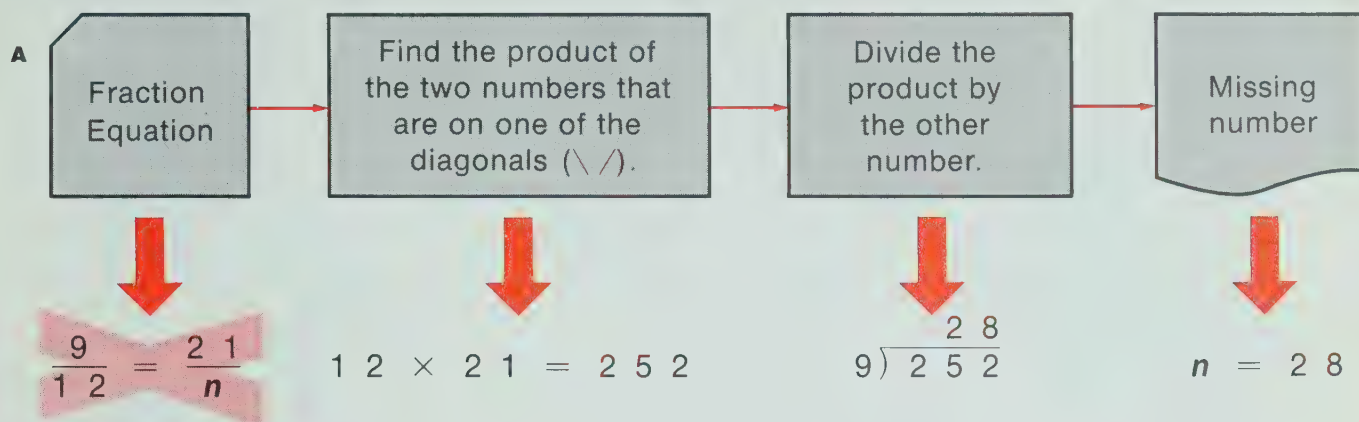
hundredths

lowest  
terms



## ● Solving Equivalent Fraction Equations

1. Study the flow chart for solving equivalent fraction equations.



**B** Now you finish this one.

$$\frac{6}{9} = \frac{n}{4\ 5}$$

$$6 \times 4\ 5 = 2\ 7\ 0$$

$$9 \overline{) 2\ 7\ 0}$$

$$n =$$

**C** Now try this one on your own.

$$\frac{9}{1\ 5} = \frac{2\ 4}{n}$$

$$1\ 5 \times 2\ 4 =$$

$$\overline{) }$$

$$n =$$

2. Solve the equivalent fraction equations. The answers are somewhere in the answer box.

**A**  $\frac{6}{1\ 6} = \frac{1\ 2}{n}$

**B**  $\frac{1\ 4}{2\ 1} = \frac{n}{9}$

**C**  $\frac{n}{2\ 5} = \frac{8}{1\ 0}$

**D**  $\frac{5}{n} = \frac{4\ 5}{5\ 4}$

**E**  $\frac{6}{2\ 0} = \frac{n}{9\ 0}$

**F**  $\frac{5}{1\ 2} = \frac{3\ 5}{n}$

**G**  $\frac{6}{2\ 4} = \frac{1\ 1}{n}$

**H**  $\frac{1\ 4}{1\ 6} = \frac{2\ 8}{n}$

**I**  $\frac{n}{3\ 0} = \frac{1\ 2}{3\ 6}$

**J**  $\frac{2\ 1}{n} = \frac{2\ 7}{3\ 6}$

**ANSWER BOX**

32	44	20
	27	10
84	28	6

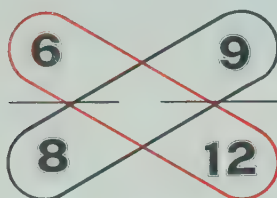
**ANSWER BOX**

## ● Which Number is Greater?

Study the three examples for 2 fractional numbers.

### EXAMPLE 1

When the cross products are the same,



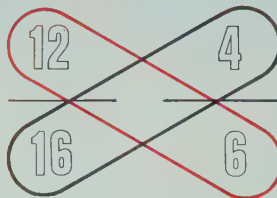
$$72 = 72$$

the fractions are equivalent and we write

$$\frac{6}{8} = \frac{9}{12}$$

### EXAMPLE 2

When the "red product" is greater,



$$72 > 64$$

the first number is greater and we write

$$\frac{12}{16} > \frac{4}{6}$$

### EXAMPLE 3

When the "black product" is greater,



$$15 < 16$$

the second number is greater and we write

$$\frac{3}{8} < \frac{2}{5}$$

1. Put =, >, or < in each

A  $\frac{1}{2}$   $\frac{3}{8}$

B  $\frac{1}{2}$   $\frac{4}{7}$

C  $\frac{2}{3}$   $\frac{3}{4}$

D  $\frac{5}{6}$   $\frac{3}{4}$

E  $\frac{5}{6}$   $\frac{5}{8}$

F  $\frac{7}{8}$   $\frac{8}{10}$

G  $\frac{10}{12}$   $\frac{15}{18}$

H  $\frac{6}{7}$   $\frac{9}{10}$

I  $\frac{5}{8}$   $\frac{3}{4}$

J  $\frac{1}{8}$   $\frac{1}{7}$

K  $\frac{2}{8}$   $\frac{1}{7}$

L  $\frac{2}{8}$   $\frac{2}{7}$

M  $\frac{1}{4}$   $\frac{1}{3}$

N  $\frac{2}{4}$   $\frac{1}{3}$

O  $\frac{2}{4}$   $\frac{2}{3}$

Answers are given below in terms of which number (if either) is greater.

A first

B second

C second

D first

E first

F first

G equivalent

H second

I second

J second

K first

L second

M second

N first

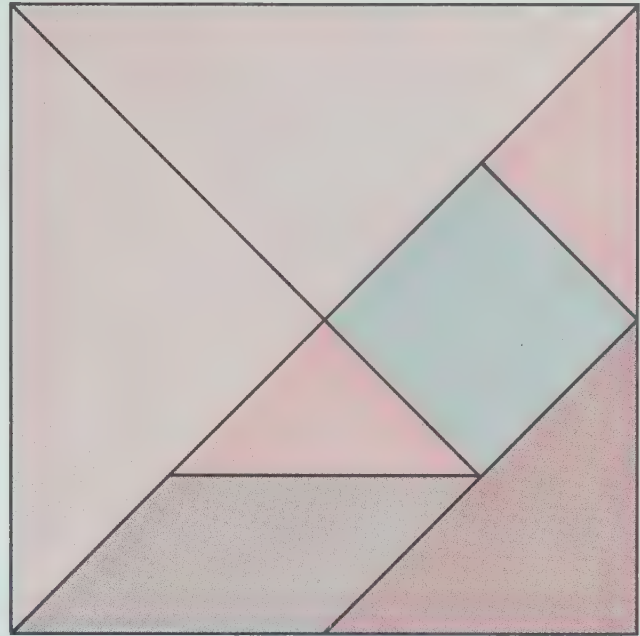
O second

2. Can you arrange these numbers in order from smallest to largest?

$$\frac{1}{2}, \frac{1}{4}, \frac{2}{5}, \frac{3}{8}, \frac{2}{3}, \frac{5}{6}, \frac{7}{8}, \frac{1}{3}, \frac{4}{7}$$

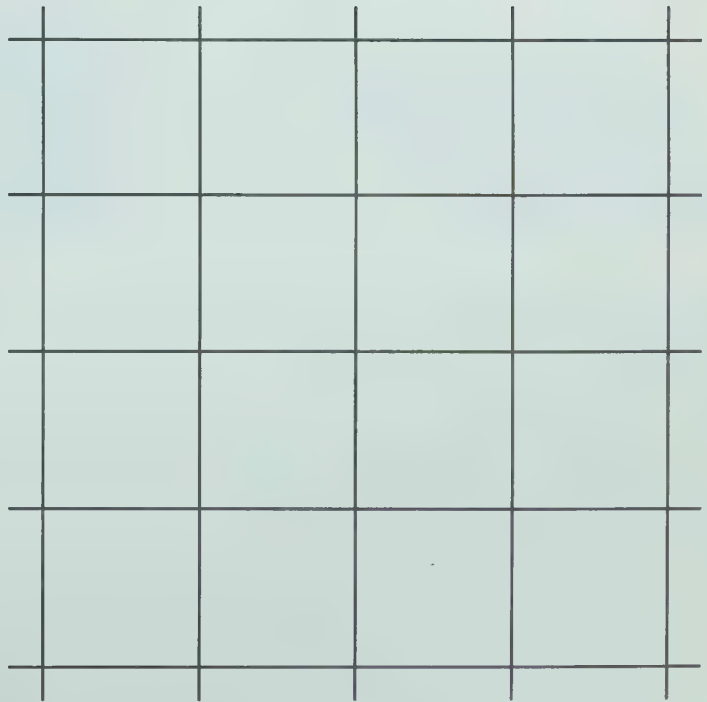
## ● Fractional Numbers and Area

Trace this figure and cut out the seven **tangram** pieces.



Use the small squares on the grid as units. Place your tangram pieces on the grid to help you answer these questions.

1. The area of each large triangle is \_\_\_\_\_.
2. The area of each small triangle is \_\_\_\_\_.
3. The area of the other triangle is \_\_\_\_\_.
4. The area of the square is \_\_\_\_\_.
5. The area of the parallelogram is \_\_\_\_\_.



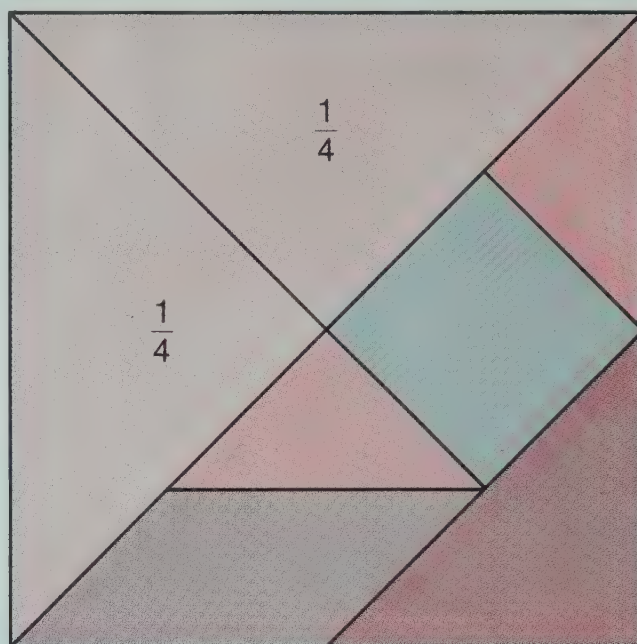
If your answers are correct, the sum of the numbers in the 5 questions should be 11. Save your tangram pieces for page 94.



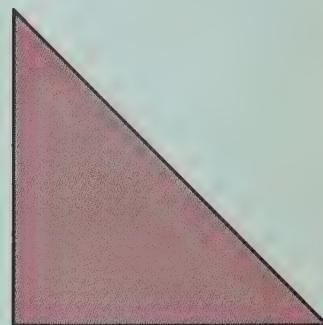
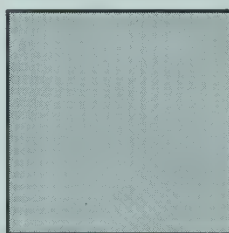
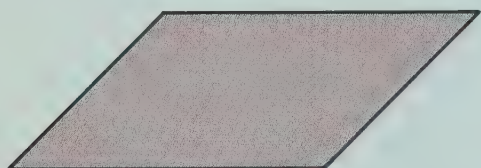
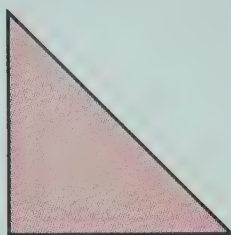
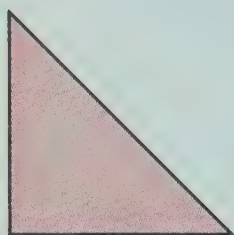
## ● Adding Fractional Numbers

Suppose the area of the large tangram square is 1. Do you see that the area of each large triangle is  $\frac{1}{4}$ ?

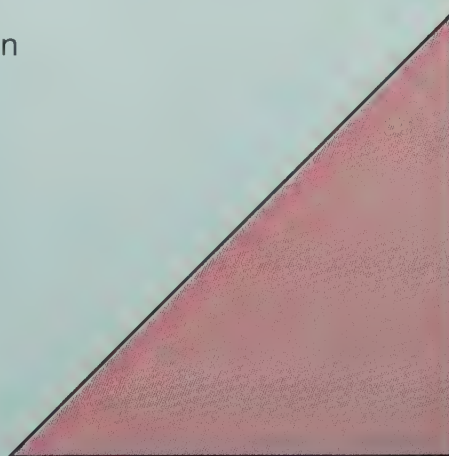
Can you find the area of each of the other tangram pieces? Write your answer on the tangram pieces pictured below. Your tangram pieces from the last lesson should help you.



Area 1



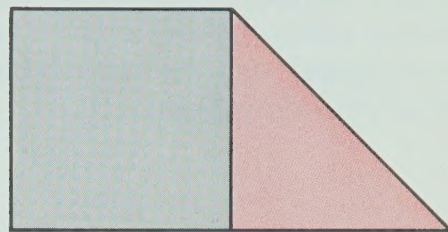
- Can you place your two small tangram pieces so they just "fit" on top of the  
**A** parallelogram?      **B** square?      **C** middle-sized triangle?
- Can you find 3 small pieces that will just fit on one of the large triangles?  
 Show how you did it on this triangle.



## ● More About Addition

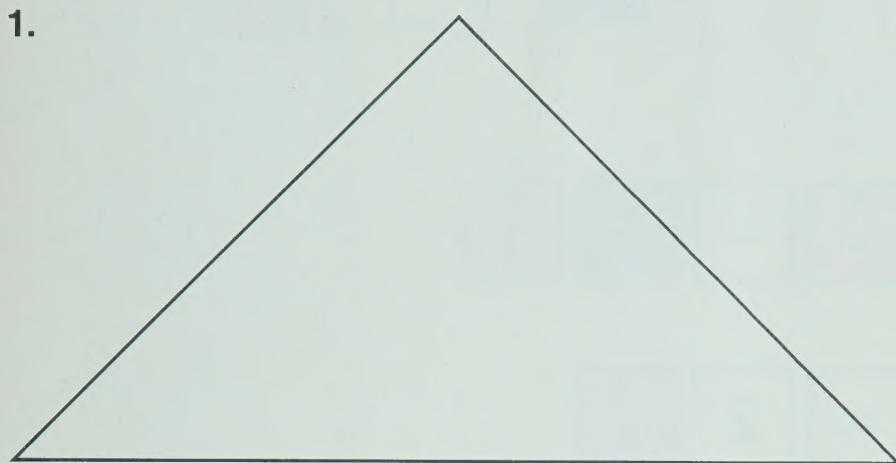
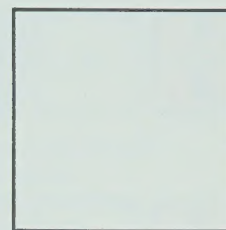
Write the fractional area that you found in the last lesson on each of your tangram pieces. Find the area of each figure by placing tangram pieces over them. Write an equation to show how you did it. Write the area inside the figure.

EXAMPLE



$$\frac{1}{8} + \frac{1}{16} = \frac{3}{16}$$

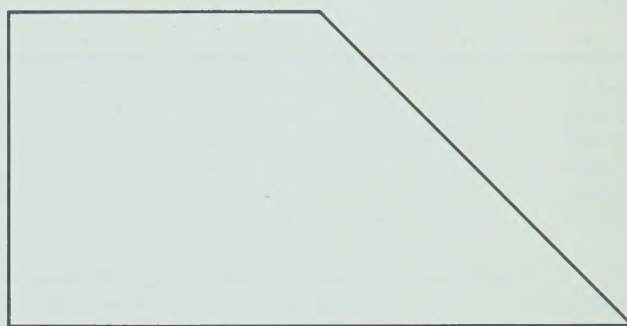
2.



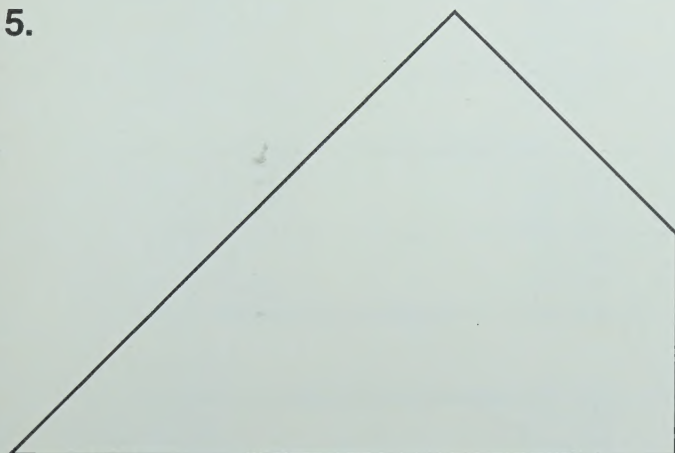
3.



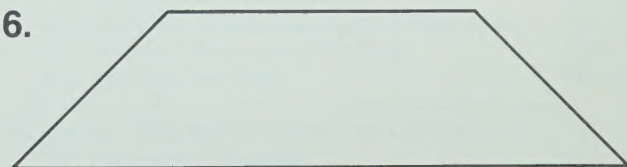
4.



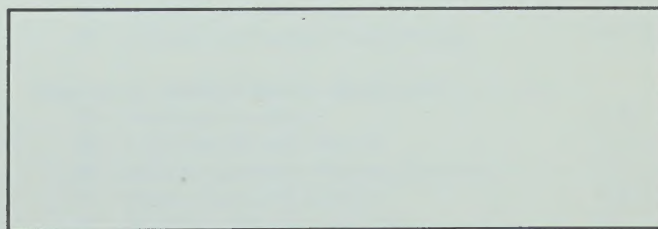
5.



6.



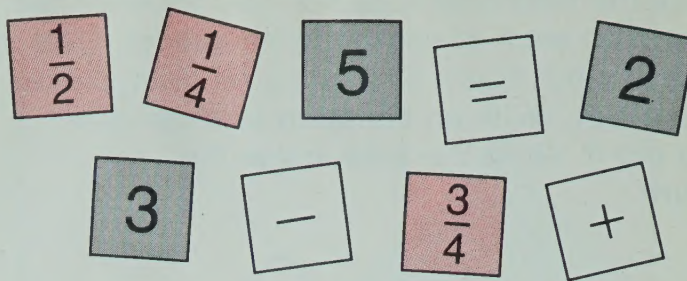
7.





# ●Writing Fractional Num

Make slips of paper with these numerals and signs on them. How many different equations can you "write" with your slips of paper? Use the record below to show your equations.



EXAMPLES:

$$2 \frac{1}{4} + 3 \frac{1}{2} = 5 \frac{3}{4}$$

$$3 \frac{1}{4} - \frac{1}{2} = 2 \frac{3}{4}$$

Record

_____	_____
_____	_____
_____	_____
_____	_____
_____	_____
_____	_____
_____	_____
_____	_____
_____	_____
_____	_____





Use with  
pages

## Chapter 1 NUMBERS AND MEASUREMENT

1	Finding Length	4-13
2	Making a Ruler	4-13
3	Finding the Distance Around	14-17
4	Distance on a Map	18-19
5	Area	20-25
6	Volume	26-27

## Chapter 2 NUMBERS AND NUMERALS

7	Place Value	34-45
8	Order of Numbers	34-45
9	Sequences with Large Numbers	44-49
10	Large Numbers	50-55
11	Which Number Is Larger?	50-55
12	Using Powers of 10 in Place Value	50-55

## Chapter 3 ADDITION AND SUBTRACTION

13	Function Tables	58-65
14	Adding and Checking	66-67
15	Finding Sums	68-73
16	Magic Squares	70-71
17	Subtracting	82-90
18	Reconstruction Problems	82-90
19	Solving Problems	90-93
20	Writing Your Own Problems	90-93

## Chapter 4 GEOMETRY

21	Cutting Cubes	98-101
22	Segments, Rays, and Angles	102-103
23	Parallel Lines	104-105
24	Space Figures	106-107
25	Polygons	110-111
26	Symmetric Figures	112-113

## Chapter 5 MULTIPLICATION AND DIVISION

27	Sequences and Equations	116-121
28	Using Logic to Find Products	122-125
29	Multiplication Facts	126-129
30	Multiplication Tables	130-132
31	Finding Missing Factors	134-137
32	Division and Sets	138-141
33	Problem Solving	143-147
34	Pairing and Multiplication	148-151

## Chapter 6 SPECIAL PRODUCTS AND QUOTIENTS

35	Finding Special Products	156-159
36	Finding Missing Factors	160-161
37	Finding Special Quotients	162-163
38	Factors with Zeros	164-165
39	Finding Special Quotients	164-165
40	Finding Special Products and Quotients	164-167

## Chapter 7 ESTIMATION

41	Finding Multiples of 10 and 100 for Estimates	170-171
42	Estimating Totals	172-173
43	Estimating Products	174-175
44	Estimating Quotients	176-177
45	Estimating	170-177
46	Estimation for Fun	178-179

## Chapter 8 MULTIPLYING

47	Multiplying with One 2-Digit Factor	182-185
48	Multiplying with a 3-Digit Factor	186-189
49	Finding Missing Digits	190-193
50	Finding Products — 2 and 3-Digit Factors	190-193
51	Multiplication and Measurement	194-195
52	Solving Problems	196-197
53	Larger Products	198-199
54	Solving Problems	200-201

## Chapter 9 GEOMETRY

55	Cross Sections of Cones and Cylinders	206-207
56	Sketching Circles	208-211
57	Circles and Tangents	212-213
58	Drawing Congruent Figures	214-215
59	Congruent Figures	214-215
60	Symmetrical Figures	216-217

## Chapter 10 DIVIDING

61	Finding Different Remainders	220-223
62	Estimating Quotients	224-227
63	Using Estimation In Division	228-229
64	Finding Missing Digits	230-231
65	Finding Averages	232-233
66	3-Digit Quotients	234-237
67	Dividing by Multiples of 10	240-241
68	Missing Digit Problems	242-245

## Chapter 11 NUMBER THEORY

69	Special Sets of Numbers	250-251
70	Factors and Products	252-253
71	Greatest Common Factor	254-255
72	Prime Numbers	256-257
73	Number Puzzlers	258-259
74	A Number Theory Puzzle	258-259

## Chapter 12 FRACTIONS

75	Fractional Parts of an Hour	262-267
76	Fractional Parts of a Meter	268-273
77	Finding Missing Fractions	274-277
78	Tenths and Hundredths	278-279
79	Using Improper Fractions	282-285
80	Exploring Fractions that are not Equivalent	286-287
81	Finding Lowest-terms Fractions	288-289
82	Fractions and Area	290-291

## Chapter 13 GEOMETRY AND GRAPHING

83	Symmetrical Designs	296-301
84	Using Coordinates to Sketch Circles	302-303
85	Stretching and Shrinking with Coordinates	304-305
86	Moving Figures	306-307
87	Finding Function Rules	310-311
88	Positive and Negative Coordinates	312-313

## Chapter 14 FRACTIONAL NUMBERS

89	Fractional Numbers	316-321
90	Fractional Number Names	322-325
91	Solving Equivalent Fraction Equations	328-329
92	Which Number is Greater?	330-331
93	Fractional Numbers and Area	332-341
94	Adding Fractional Numbers	332-341
95	More About Addition	332-341
96	Writing Fractional Number Equations	340-341



C1597



EICHOLZ ■ O'DAFFER ■ FLEENOR



ADDISON-WESLEY PUBLISHING COMPANY